

Chapter 1

Digital Logic Circuit

Cont...

Computer architecture

is concerned with the way how the hardware components are connected together to form a computer system.

example, instruction set, number of bits, I/O mechanism.

The digital computer

is a digital system that performs various computational tasks.

A digital implies that the information in the computer represented by the variables that take a limited number of discrete values.

Cont...

- Digital computer use the binary number system which has two digits 0 and 1.
- A binary digit is called a bit.
- Computer design is concerned with the development of hardware for the computer.
- Its although concerned with structure and function of computer system.
- Also it is called computer implementation.

Cont...

- The computer designer is concerned with structure and function characteristics of computer system:
- **Structure:** The way in which the components are interrelated
- **Function:** The operation of each individual component as part of the structure

Cont...

- Computers can perform four basic function
 - ✓ Data processing
 - ✓ Data storage
 - ✓ Data movement
 - ✓ Control
- There are four main structural components
 - ✓ Central processing unit (CPU)
 - ✓ Main memory:
 - ✓ I/O
 - ✓ System interconnection

two functional entities of computer system

System Hardware

- consists all of the electronic component and electro mechanical devices that comprises the physical entities of the devices.
- Hardware of the computer is divided in to three major parts.
 1. **cpu** that contains
 - a. Arithmetic and logic unit for manipulating data.
 - b. number of Registers for storing data.
 - c. control circuit for fetching and executing instr.

Cont...

2.RAM it contains storage for instruction and data.

3.Input output processor (Iop)

- contains electronic circuit for communicating and controlling transfer of information between the computer and outside world.
- The IP and OP devices connected to computer includes
 - ✓ key board
 - ✓ printer
 - ✓ terminals
 - ✓ magnetic disk drive

Cont...

System software

- consists all instructions and data that the computer manipulate to perform various data processing task.
- it consists all collection of the program whose purpose is to make effective use of the computer.
- It compensate for the difference between user need and capability of computer hardware.

Cont...

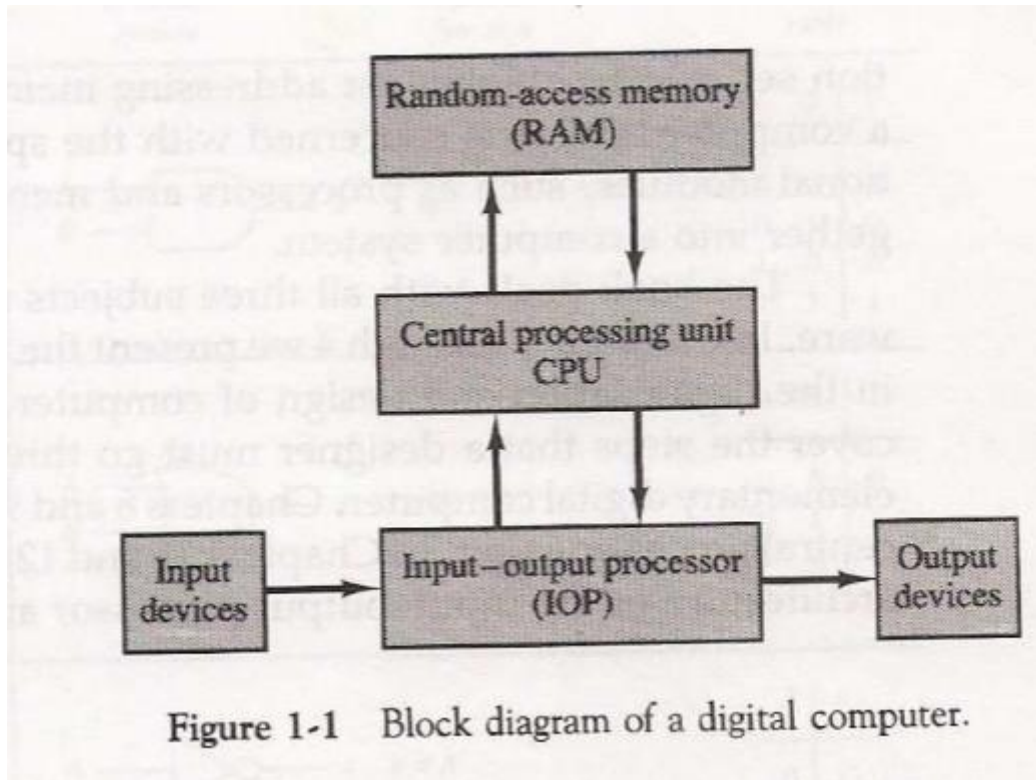


Figure 1-1 Block diagram of a digital computer.

Logic Gates

- Binary information in digital computers represented by physical quantities called signal.
- The manipulation of binary information is done by logic circuit called gate.
- **gate** is The fundamental building block of Hardware that produce signal of binary 1 or 0.
- The basic gates used in digital logic are AND, OR, NOT, NAND, NOR, and XOR.

Cont...

1.AND gate

- ✓ produce the AND logic function.
- ✓ It concatenate variables.
- ✓ the output is 1 if and only if both i
- ✓ nput A and B are 1.otherwise, the output is 0.

2.OR gate

- ✓ Produce the inclusive or function.
- ✓ The output is 1 if input A or B or both inputs are 1.
- ✓ Algebraic symbol is '+' similar to Arithmetic addition.

Cont...

3. Inverter

- ✓ the inverter circuit inverts the logic sense of a binary signal.
- ✓ It produces the NOT or complement function.

4. NAND gate

- ✓ Is the complement of AND function, is NOT-AND.

5. NOR gate

- ✓ Is the complement of OR gate.

Cont...

6.Exclusive-OR(XOR)

- ✓ Is called odd function.
- ✓ The output of XOR is 1 if any input is 1, but exclude the combination when both inputs are 1.

7.Exclusive-NOR gate

- ✓ Is called equivalence
- ✓ it is complement of Exclusive –OR
- ✓ The output is 1 only if both input are 1 or both input are 0.







Cont...

$X = (A \text{ EX-OR } B)'$ or

$X = A'B' + AB$

- ✓ Inverter and Buffer are unary gates which take a single input.

Cont...

Name	Graphical Symbol	Algebraic Function	Truth Table															
AND		$F = A \cdot B$ or $F = AB$	<table border="1"> <thead> <tr> <th>A</th> <th>B</th> <th>F</th> </tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </tbody> </table>	A	B	F	0	0	0	0	1	0	1	0	0	1	1	1
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NOT		$F = \bar{A}$ or $F = A'$	<table border="1"> <thead> <tr> <th>A</th> <th>F</th> </tr> </thead> <tbody> <tr><td>0</td><td>1</td></tr> <tr><td>1</td><td>0</td></tr> </tbody> </table>	A	F	0	1	1	0									
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XOR		$F = A \oplus B$	<table border="1"> <thead> <tr> <th>A</th> <th>B</th> <th>F</th> </tr> </thead> <tbody> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </tbody> </table>	A	B	F	0	0	0	0	1	1	1	0	1	1	1	0
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Boolean Algebra

Boolean algebra

- is an algebra that deals with binary variables and logic operations.
- The possible values for a logical variable are either TRUE or FALSE.
- The logical operators of Boolean algebra are AND, OR, and NOT, which are symbolically represented by dot (\cdot), plus sign ($+$), and over bar ($\bar{\quad}$).
- Boolean algebra is used to facilitate the analyse and design of digital circuits.

Cont...

Boolean Expressions

- are made up of Boolean constants 0,1 and the three operations.

Boolean Variables

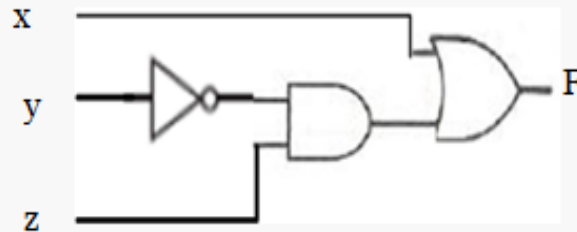
- are Boolean quantities whose values are not yet known. They can take the values 0 or 1 only.

Cont...

A Boolean function can be represented by a truth table and a logic diagram.

Example, $F = x + y'z$

x	y	z	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1



Properties(basic Identities of Boolean Algebra)

1.Idempontency

$$x+x = x$$

$$x.x = x$$

2.Identity Properties:

$$x+0=x$$

$$x.1=x$$

3.Dominance Laws:

$$x+1=1$$

$$x.0=0$$

Cont...

4. Involution Property

$$(x')' = x$$

5. Commutativity

$$x + y = y + x$$

$$y \cdot x = x \cdot y$$

6. Associativity

$$(x + y) + z = x + (y + z) = x + y + z$$

$$(x \cdot y) \cdot z = x \cdot (y \cdot z) = x \cdot y \cdot z$$

7. Complementatation

$$x + x' = 1$$

$$x \cdot x' = 0$$

Cont...

8. Distributive property

$$x.(y+z)=x.y+x.z$$

$$x+(y.z)=(x+y).(x+z)$$

9. Absorption

$$x+xy=x$$

$$x(x+y)=x$$

Cont...

10. Adsorption

$$x + x'y = x + y$$

$$x.(x' + y) = xy$$

11. De Morgan's laws

$$(x + y)' = x'y'$$

$$(xy)' = x' + y'$$

K-MAP Simplification

Rules for K-map simplification

we use sop form

1. Group may not contain zero.
2. We can group by 1, 2, 4 and 8 grouping: 2^n cells.
3. Each group should be large as possible.
4. Cell contain 1 must be grouped.
5. Groups may be overlap.
6. Opposite grouping and corner grouping are allowed.
7. There should be as few groups as possible.

Combinational Circuits

- ▶ A combinational circuit is an interconnected set of gates whose output at any time is a function only of the input at that time
- ▶ They serve as a basic building blocks for the construction of more complicated arithmetic circuits.
- ▶ a combinational circuit consists of n binary inputs and m binary outputs.
- ▶ Combinational circuits have no feedback

Cont...

- Common combinational circuit are, Adders (Half Adder & Full Adder)

Half Adder

- A digital arithmetic circuit that carries out the addition of two bits is called a **half adder**.
- It has two input variables and two outputs variables (sum & carry).

Cont...

Full Adder

- ▶ add two n-bit numbers along with a carry from a previous bitwise addition (performs addition of three bits).
- ▶ A combination of two half adders creates a *full adder*.

Cont...

Multiple-Bit Adder

- By combining a number of full adders, we can have the necessary logic to implement a multiple-bit adder.
- The output from each adder depends on the carry from the previous adder.

1.5 Sequential Circuits

- In case of combinational circuits, the value of each output depends on the values of signals applied to the inputs.
- However, in case of Sequential Circuits, the values of the outputs depend not only on the present values of the inputs but also on the past behaviour of the circuit.
- Such circuits include storage elements that store the values of logic signals. E.g flip-flops

Flip-Flops

- The simplest form of sequential circuit is the flip-flops.
- The flip-flop is a bistable device, i.e. has two stable states.
- It exists in one of two states and, in the absence of input- function as a 1-bit memory.
- E.g S-R, J-K & D flip-flops