



MACHINING -LEVEL II

**Based on Version 2 February 2017
Occupational Standard (OS)
Training Module –Learning Guide 14-
03**

Unit of Competence: Perform mensuration and calculation

Module Title: Performing mensuration and calculations

TTLM Code: IND MAC2 TTLM05 1019v1

October 2019



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This module includes the following Learning Guides

LG 14: Select measuring Instruments

LG Code: IND MAC2 M05 LO1-LG-14

LG 15: Carry-out measurements and calculations

LG Code: IND MAC2 M05 LO2-LG-15

LG 16: Carry-out measurements and calculations.

LG Code: IND MAC2 M05 LO3-LG-16



This learning guide is developed to provide you the necessary information regarding the following **content coverage** and topics:

- classify and interpret geometric shapes`
- Select and identify measuring tools
- Use alternative measuring tools

This guide will also assist you to attain the learning outcome stated in the cover page. Specifically, **upon completion of this Learning Guide, you will be able to:**

- Identify, classify and interpret Object or component to be measured according to the appropriate regular geometric shape and drawing standard
- Select/identify measuring tools as per object to be measured or work requirement
- Use alternative measuring tools without sacrificing cost and quality of work

Learning Instructions:

1. Read the specific objectives of this Learning Guide.
2. Follow the instructions described below.
3. Read the information written in the “Information Sheets”. Try to understand what are being discussed. Ask your trainer for assistance if you have hard time understanding them.
4. Accomplish the “Self-checks” which are placed following all information sheets.
5. Ask from your trainer the key to correction (key answers) or you can request your trainer to correct your work. (You are to get the key answer only after you finished answering the Self-checks).
6. If you earned a satisfactory evaluation proceed to “Operation sheets
7. Perform “the Learning activity performance test” which is placed following “Operation sheets” ,
8. If your performance is satisfactory proceed to the next learning guide,
9. If your performance is unsatisfactory, see your trainer for further instructions or go back to “Operation sheets”.



1.1. Geometric Shapes

1.1.1. definition of geometric Shapes

Geometric Shapes can be defined as figure or area closed by a boundary which is created by combining the specific amount of curves, points, and lines. Different geometric shapes are Triangle, Circle, Square, etc

Such shapes are called polygons and include triangles, squares, and pentagons. Other shapes may be bounded by curves such as the circle or the ellipse

1.1.2. Classify

Classify. To arrange in groups, by some property. These shapes are classified by the number of sides. Simple shapes can often be classified into basic geometric objects such as a point, a line, a curve, a plane, a plane figure (e.g. square or circle), or a solid figure (e.g. cube or sphere)

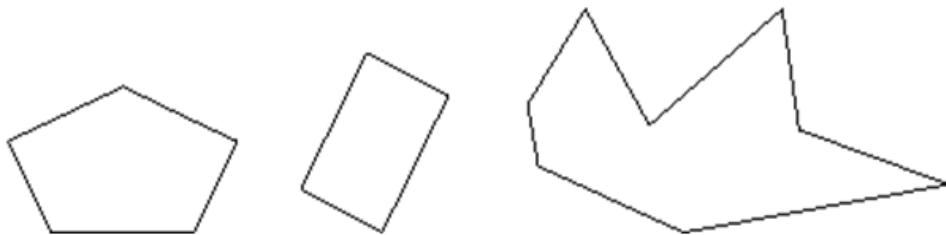
Many of these shapes, or polygons, can be described as flat closed figures with 3 or more sides. Polygons are two-dimensional objects, not solids. Polygons are classified and described by the number of sides, the kind of angles, and whether any of the sides are the same length (or congruent)

- **Polygon**

A polygon is a closed figure made by connecting line segments, where each line segment end connects to only one end of two other line segments.

Examples:

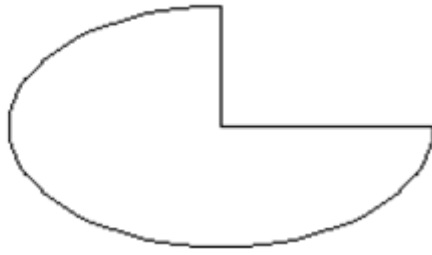
The following are examples of polygons:



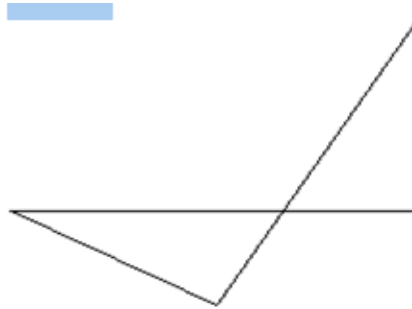
The figure below is not a polygon, since it is not a closed figure:



The figure below is not a polygon, since it is not made of line segments



The figure below is not a polygon, since its sides do not intersect in exactly two places each:

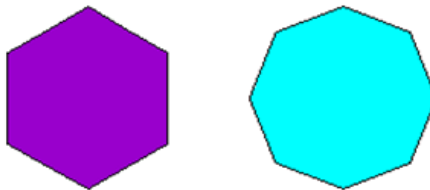


✓ Regular Polygon

A regular polygon is a polygon whose sides are all the same length, and whose angles are all the same. The sum of the angles of a polygon with n sides, where n is 3 or more, is $180^\circ \times (n - 2)$ degrees

Examples:

The following are examples of regular polygons:

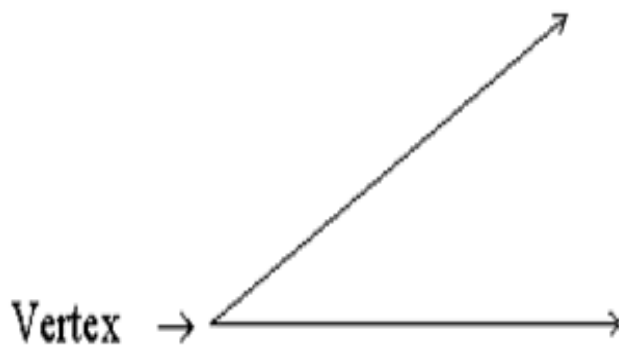


Examples:

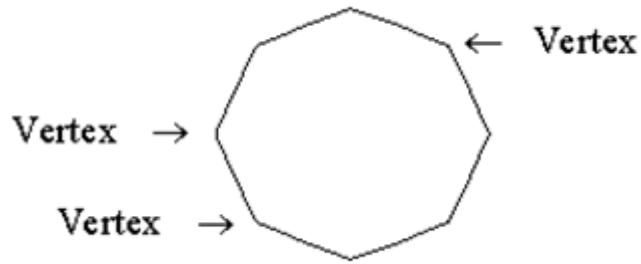
The following are not examples of regular polygons

Vertex

1) The vertex of an angle is the point where the two rays that form the angle intersect



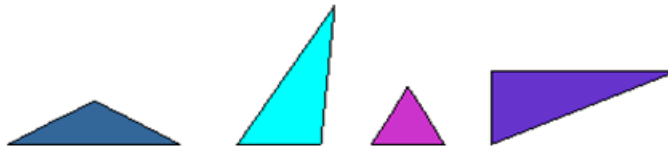
2) The vertices of a polygon are the points where its sides intersect.



✓ **Triangle**

A three-sided polygon. The sum of the angles of a triangle is 180 degrees

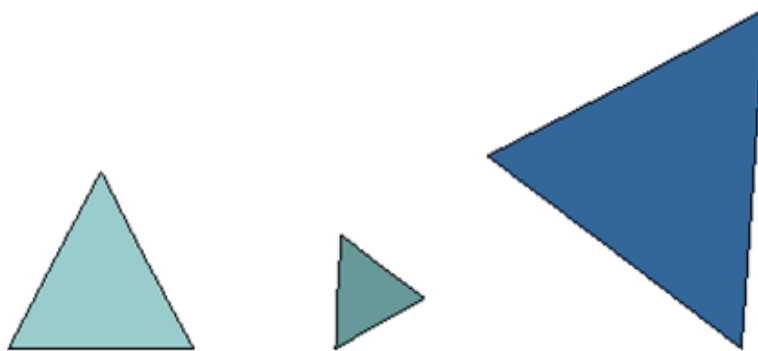
Examples:



Equilateral Triangle or Equiangular Triangle

A triangle having all three sides of equal length. The angles of an equilateral triangle all measure 60 degrees.

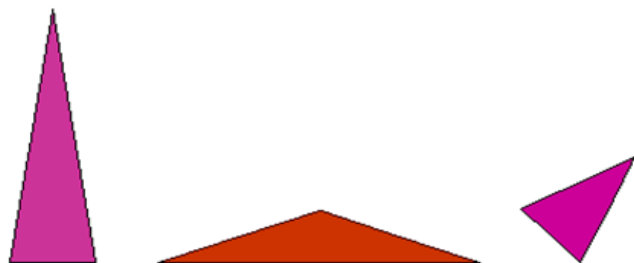
Examples:



✓ **Isosceles Triangle**

A triangle having two sides of equal length.

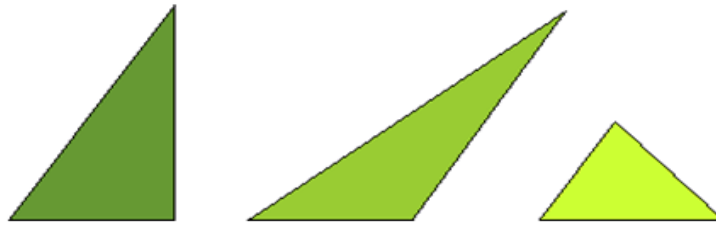
Examples:



✓ **Scalene Triangle**

A triangle having three sides of different lengths.

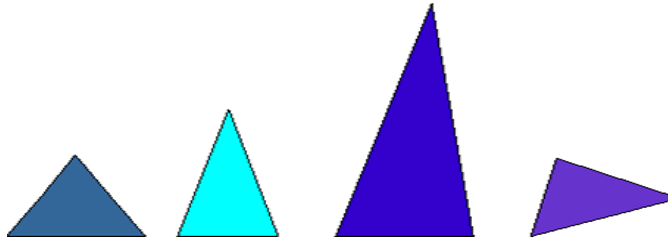
Examples:



✓ **Acute Triangle**

A triangle having three acute angles.

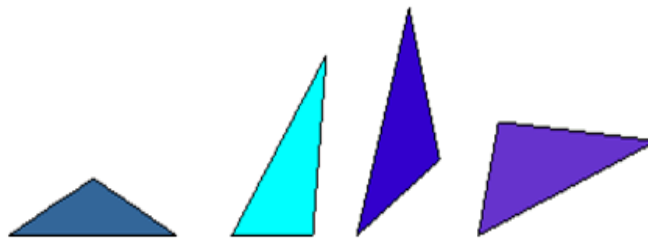
Examples:



✓ **Obtuse Triangle**

A triangle having an obtuse angle. One of the angles of the triangle measures more than 90 degrees.

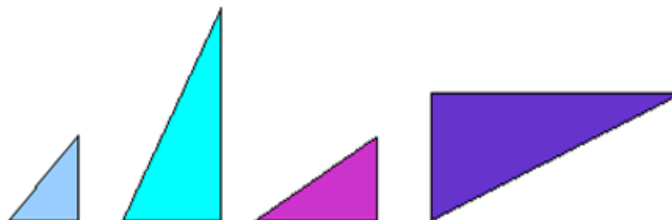
Examples:



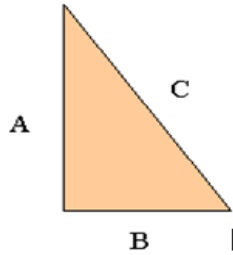
✓ **Right Triangle**

A triangle having a right angle. One of the angles of the triangle measures 90 degrees. The side opposite the right angle is called the hypotenuse. The two sides that form the right angle are called the legs. A right triangle has the special property that the sum of the squares of the lengths of the legs equals the square of the length of the hypotenuse. This is known as the Pythagorean Theorem.

Examples:

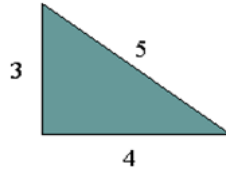


Example:



For the right triangle above, the lengths of the legs are A and B, and the hypotenuse has length C. Using the Pythagorean Theorem, we know that $A^2 + B^2 = C^2$.

Example:

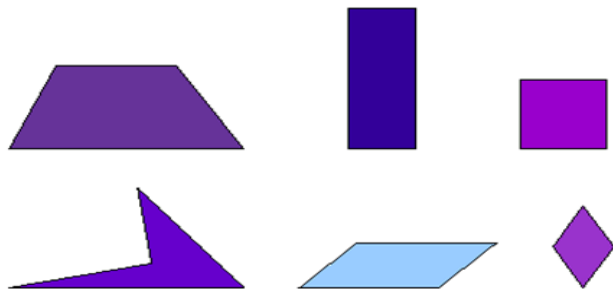


In the right triangle above, the hypotenuse has length 5, and we see that $3^2 + 4^2 = 5^2$ according to the Pythagorean Theorem.

✓ **Quadrilateral**

A four-sided polygon. The sum of the angles of a quadrilateral is 360 degrees.

Examples:



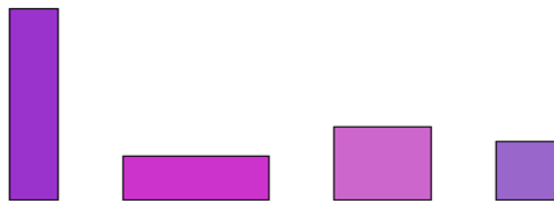
✓ **Rectangle**

A four-sided polygon having all right angles. The sum of the angles of a rectangle is 360 degrees.

Examples:

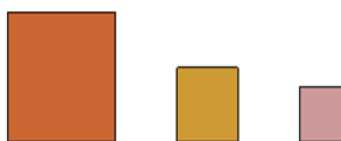
✓ **Square**

A four-sided polygon having equal-length sides. The sum of the angles of a square is 360 degrees.



polygon having equal-meeting at right angles. angles of a square is

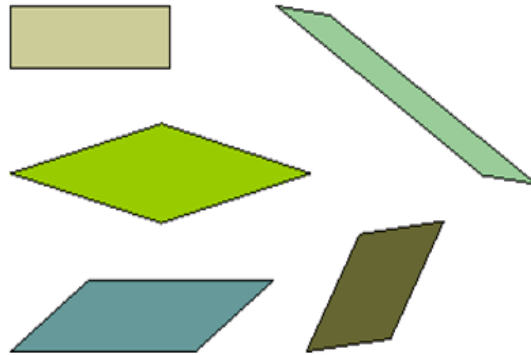
Examples:



✓ **Parallelogram**

A four-sided polygon with two pairs of parallel sides. The sum of the angles of a parallelogram is 360 degrees.

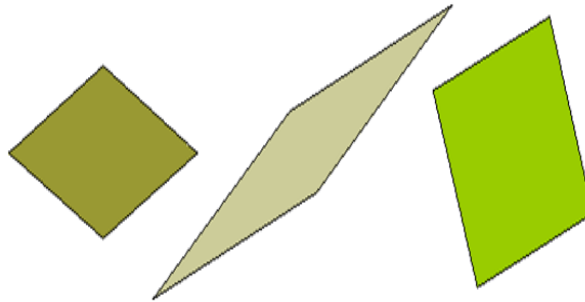
Examples:



✓ **Rhombus**

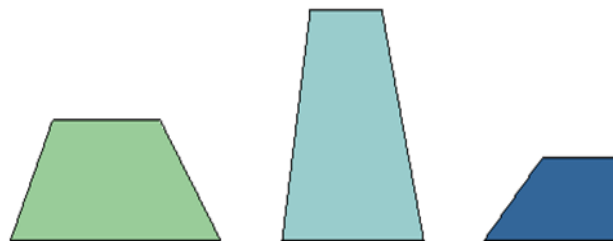
A four-sided polygon having all four sides of equal length. The sum of the angles of a rhombus is 360 degrees.

Examples:



A four-sided polygon having exactly one pair of parallel sides. The two sides that are parallel are called the bases of the trapezoid. The sum of the angles of a trapezoid is 360 degrees.

Examples:



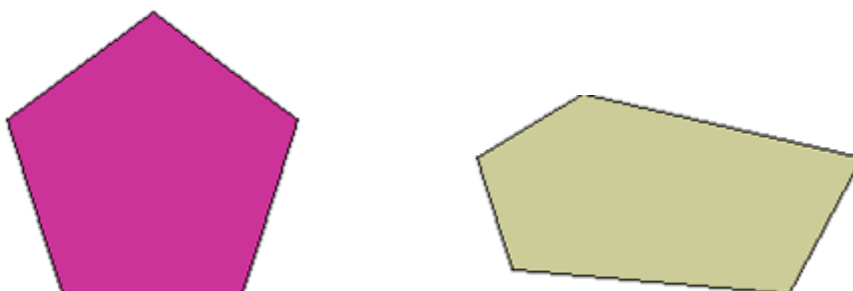
✓ **Trapezoid**

having exactly one pair of parallel sides. The two sides that are parallel are called the bases of the trapezoid. The sum of the angles of a trapezoid is 360 degrees.

✓ **Pentagon**

A five-sided polygon. The sum of the angles of a pentagon is 540 degrees.

Examples:





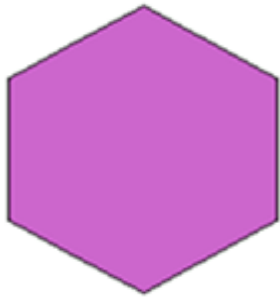
A regular pentagon

An irregular pentagon

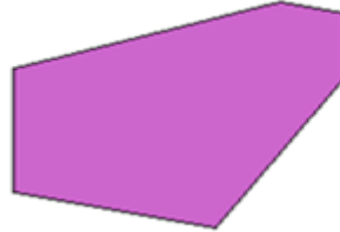
✓ Hexagon

A six sided polygon. The sum of the angle of hexagon is 720 degrees

Examples: An irregular hexagon



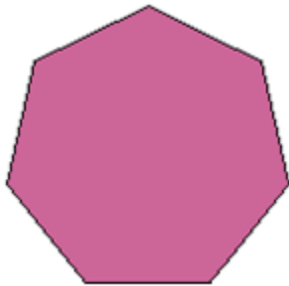
A regular hexagon



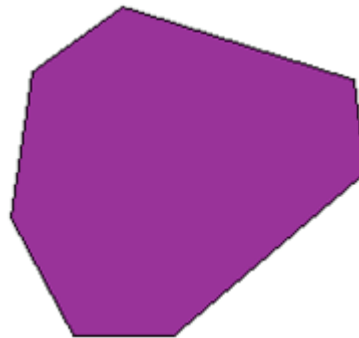
An irregular hexagon

✓ **Heptagon:** Seven-sided polygon. The sum of the angles of a heptagon is 900 degrees

Examples:



A regular heptagon

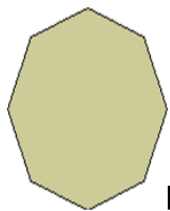


An irregular heptagon

✓ **Octagon**

An eight-sided polygon. The sum of the angles of an octagon is 1080 degrees.

Examples:



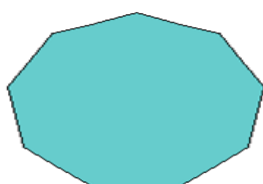
A regular octagon:

An irregular octagon:

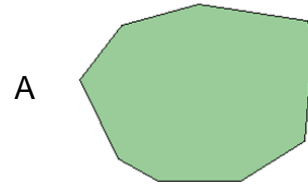
✓ **Nonagon**

Nine-sided polygon. The sum of the angles of a nonagon is 1260 degrees.

Examples:



An



A

regular nonagon
irregular



nonagon

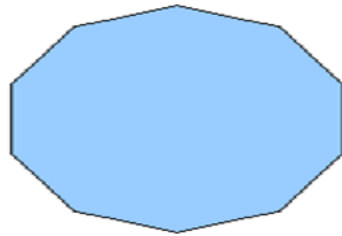
✓ **Decagon**

:

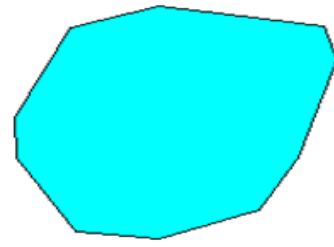
Ten-sided polygon. The sum of the angles of a decagon is 1440 degrees.

Examples:

:



A regular decagon

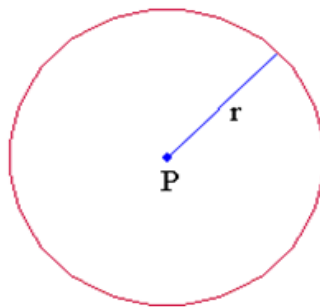


An irregular decagon

✓ **Circle**

A circle is the collection of points in a plane that are all the same distance from a fixed point. The fixed point is called the center. A line segment joining the center to any point on the circle is called a radius.

Example:



The blue line is the radius r , and the collection of red points is the circle.

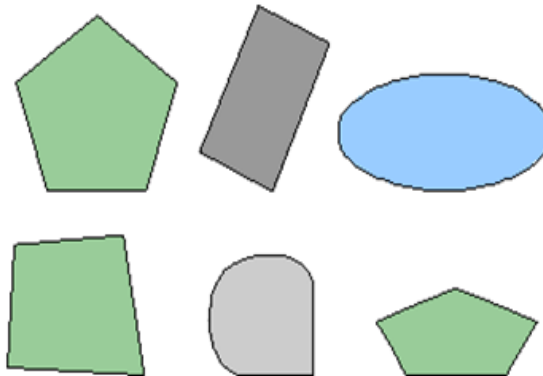


✓ **Convex**

A figure is convex if every line segment drawn between any two points inside the figure lies entirely inside the figure. A figure that is not convex is called a concave figure.

Example:

The following figures are convex.



**Self-Check-1****Written test**

Directions: choose the best answer for the following question (2 point each)

1. A polygon with six sides
 - A. hexagon
 - B. Octagon
 - C. Triangle
 - D. Square
2. A point where the two rays that form the angle intersect.
 - a. Convex
 - b. Vertex
 - c. Decagon
 - d. Circle
3. A collection of points in a plane that are all the same distance from a fixed point. The fixed point is called the center. A line segment joining the center to any point on the circle is called a radius.
 - A. Octagon
 - B. Decagon
 - C. Triangle
 - D. Circle
4. A four-sided polygon having exactly one pair of parallel sides. The sum of the angles is 360 deg.
 - A. Circle
 - B. Parallelogram
 - C. Trapezoid
 - D. Triangle
5. Square is an example of;
 - A. Circle
 - B. Parallelogram
 - C. Trapezoid
 - D. Triangle

Note: Satisfactory rating - 5 points

Unsatisfactory - below 5 points

You can ask you teacher for the copy of the correct answers.



2.1 INTRODUCTION

Linear measurement includes the measurement of lengths, diameters, heights and thickness. The basic principle of linear measurement (mechanical type) is that of comparison with standard dimensions on a suitably engraved instrument or device. Linear measuring instruments are categorized depending upon their accuracy. The two categories are non-precision instruments and precision instruments. Non-precision instruments include steel rule, caliper divider, and telescopic gauge that are used to measure to the line graduations of a rule. Precision instruments include micrometers, vernier calipers, height gauges and slip gauges. A wide variety of electrical measuring devices is also available. Electric measuring devices are mainly transducers, i.e. they transform the displacement into suitable measurable parameter like voltage and current. Some of the displacement transducers are strain gauges, linear variable differential transformers (LVDT) and potentiometers. This unit will discuss different type of linear measuring devices and comparators.

2.1.1 NON-PRECISION MEASURING INSTRUMENTS

Non-precision instruments are limited to the measurement of parts to a visible line graduation on the instrument used. There are several non-precision measuring devices. They are used where high measurement accuracy is not required. This section describes some of the non-precision measuring devices

✓ **Steel Rule**

It is the simplest and most common measuring instruments in inspection. The principle behind steel rule is of comparing an unknown length to the one previously calibrated. The rule must be graduated uniformly throughout its length. Rules are made in 150, 300, 500 and 1000 mm length. There are rules that have got some attachment and special features with them to make their use more versatile. They may be made in folded form so that they can be kept in pockets. The degree of accuracy when measurements are made by a steel rule depends upon the quality of the rule, and the skill of the user in estimating part of a millimeter

✓ **Calipers**

Calipers are used for measurement of the parts, which cannot be measured directly with the scale. Thus, they are accessories to scales. The calipers consist of two legs hinged at top, and the ends of legs span part to be inspected. This span is maintained and transferred to the scale. Calipers are of two types : **spring type** and firm **joint type**

✓ **Spring Type**

Spring type calipers are of following types

(Outside Spring Calipers , Inside Spring Calipers)

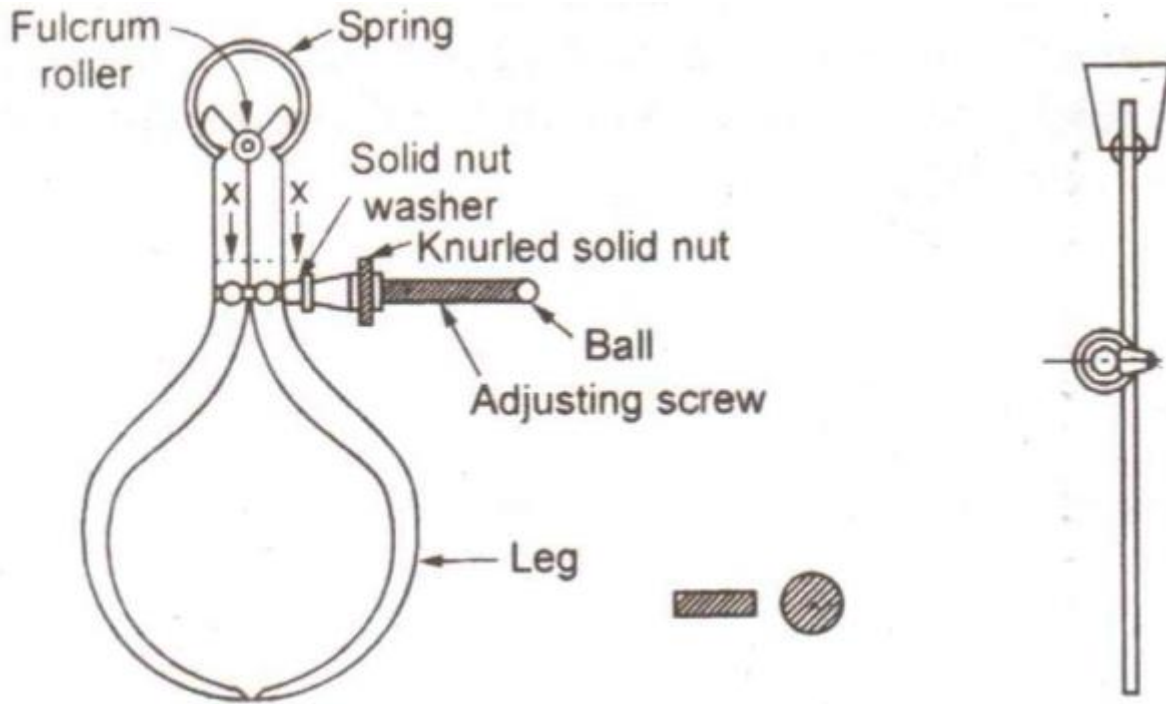


Fig 1.Outside Spring Caliper

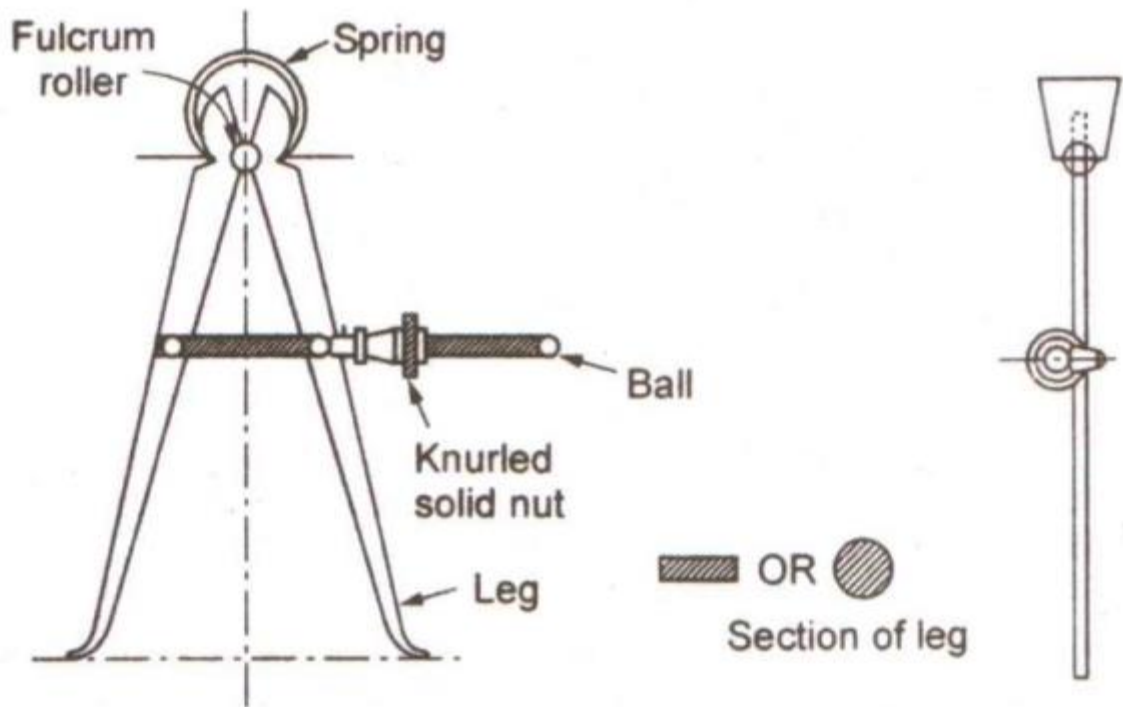
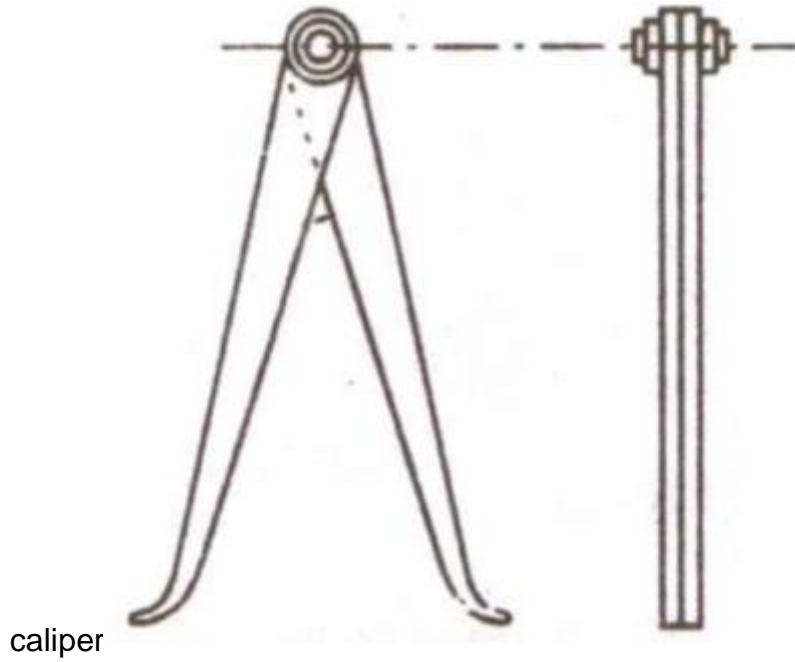


Fig 2. Inside Spring Caliper

✓ **Firm Joint Type**

Firm joint calipers are of following types :

(Outside caliper, Inside Caliper, Transfer caliper, Hermaphrodite



caliper

Fig 3.Outside Firm Joint Caliper

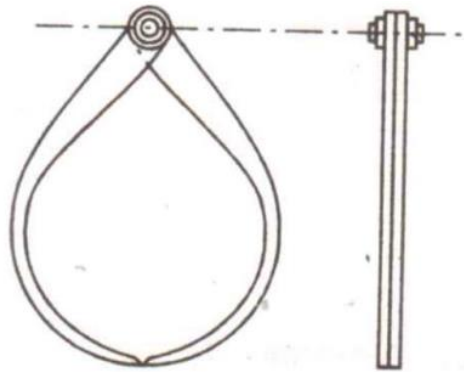


Fig 4.Inside Firm Joint Caliper

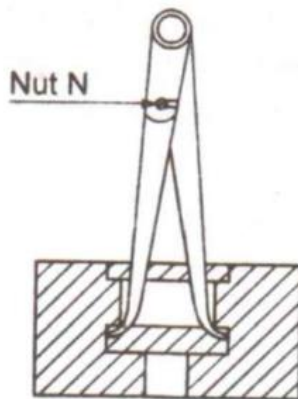


Fig 5.Transfer Caliper

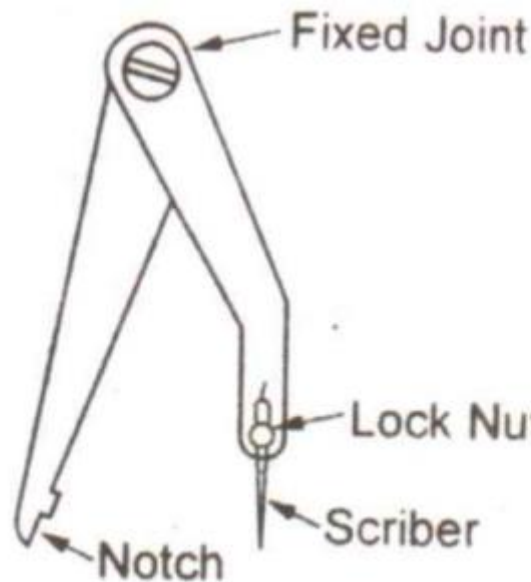


Fig 6.Hermaphrodite Caliper

✓ **Divider**

A divider is similar in construction to a caliper except that both legs are straight with sharp hardened points at the end as shown in Figure. These are used for scribing arcs and circles and general layout work. The distance between the fulcrum roller centre and the extreme working end of one of legs is known as the nominal size Dividers are available in the sizes of 100, 200, 300 mm. In practice, one point is placed in the centre position and the circle or arc may then be scribed on the job with the other point. A steel scale must be used with this instrument. Figure shows a divider.

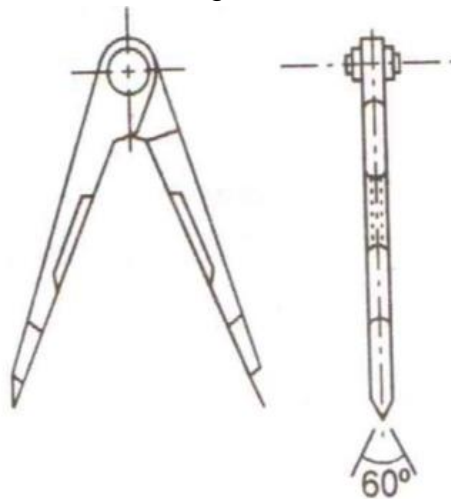


Fig 7.Divider

✓ **Telescopic Gauge**

The telescopic gauge shown in Figure is used for the measurement of internal diameter of a hole during machining operation. It consists of a handle and two plungers, one telescopic into the other and both under spring tension. Ends of the plungers have spherical contacts. The plunger can be locked in position by turning a knurled screw at the end of the handle. To measure the diameter of a hole, the plungers are first compressed and locked in position. Next, the plunger end is inserted in the hole and allowed to expand

the opposite edges. Finally, they are locked in place, taken out of the hole, and measured by an outside micrometer.

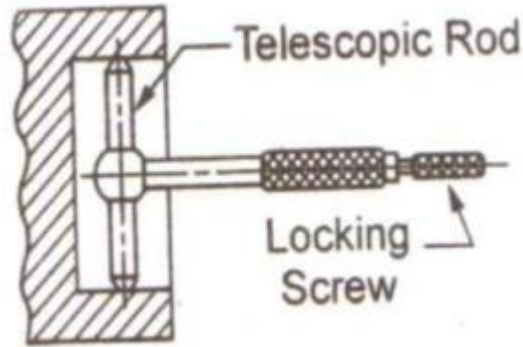


Fig 8. Telescopic Gauge

✓ **Depth Gauge**

This tool is used to measure the depth of blind holes, grooves, slots, the heights of shoulders in holes and dimensions of similar character. This is essentially a narrow steel rule to which a sliding head is clamped at the right angles to the rule as shown in Figure . The head forms a convenient marker in places where the rule must be held in a distance from the point being measured.

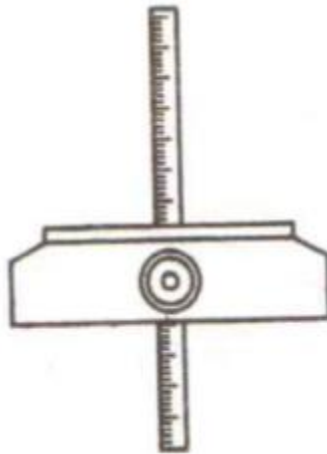


Fig 9. Depth Gauge

2.1.2 Precision measuring instruments

Since modern production processes is concerned with interchangeable products, precise dimensional control is required in industry. Precision measurement instruments use different techniques and phenomena to measure distance with accuracy. We will discuss some of the precision measuring instruments in this section.

✓ **Vernier Calipers**

Vernier calipers are precision measuring instruments that give an accuracy of 0.1 mm to 0.01 mm. The main scale carries the fixed graduations, one of two measuring jaws, a vernier head having a vernier scale engraved on. The vernier head carries the other jaw and slides on main scale. The vernier head can be locked to the main scale by the knurled screw attached to its head. Enlarged diagram of the metric vernier scale is shown in Figure 5.10

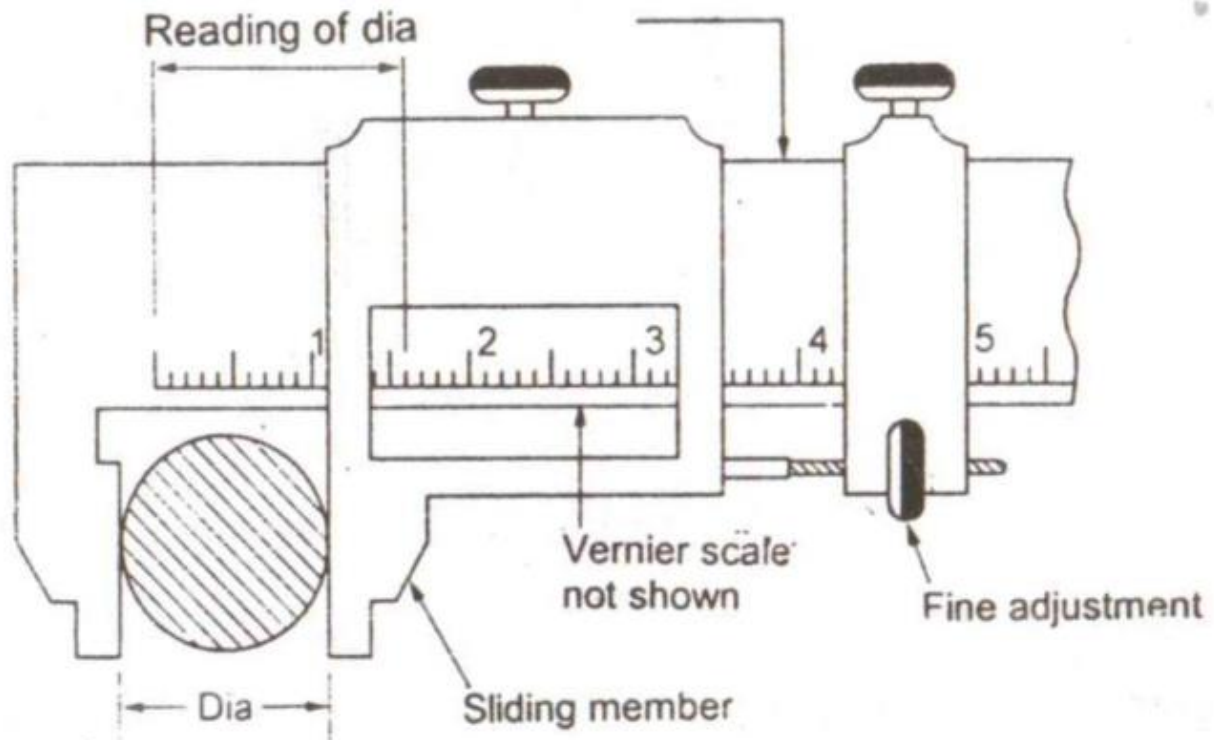


Fig 10.Vernier Caliper

To understand the working principle of a vernier caliper, let us consider that the vernier scale has got 20 divisions which equals to 19 divisions of the main scale. Thus, one smallest division of the vernier scale is slightly smaller than the smallest division of the main scale. This difference is called vernier constant for that particular vernier caliper and when it is multiplied with the smallest unit of the main scale gives the least count of that vernier. Now, 20 vernier scale divisions (VSD) = 19 main scale division (MSD)

$$\therefore 1 \text{ VSD} = \frac{19}{20} \text{ MSD}$$

$$\therefore \text{Vernier constant (VC)} = 1 \text{ MSD} - 1 \text{ VSD}$$

$$= 1 \text{ MSD} - \frac{19}{20} \text{ MSD}$$

$$= \frac{1}{20} \text{ MSD}$$

Now, if the smallest unit of the main scale be 1 mm, the least count of the vernier scale = VC × one smallest unit of the main scale

$$= \frac{1}{20} \times 1 \text{ mm}$$

$$= 0.05 \text{ mm}$$

If the smallest unit in the main scale be 0.5 mm, the least count of the vernier scale is,

$$= \frac{1}{20} \times 0.5 \text{ mm}$$

$$= 0.025 \text{ mm}$$

To read a measurement from a vernier caliper, first the main scale reading up to the zero of the vernier scale is noted down. It will give accuracy up to the smallest division of the main scale. Now, vernier number of vernier scale division from its zero, which coincides exactly with the main scale is noted. This number when multiplied with the vernier constant gives the vernier scale reading. The actual length is obtained when the vernier scale reading is added to the main scale reading

The caliper is placed on the object to be measured and the fine adjustment screw is adjusted until the jaws tightly fit against the Work piece. There are vernier calipers that incorporate arrangements for measurement of internal dimensions and depth. The vernier calipers are designed to measure both internal and external dimensions. The lower jaws of a vernier scale are used for external measurement and the upper jaws for the measurement of internal dimensions. The rectangular rod carried by the movable jaw is used for the measurement of depth

✓

Micrometers

Micrometer is one of the most widely used precision instruments. It is primarily used to measure external dimensions like diameters of shafts, thickness of parts etc. to an accuracy of 0.01 mm. The essential parts of the instruments shown in Figure 5.11, consist of

- (a) Frame
- (b) Anvil and spindle
- (c) Screwed spindle
- (d) Graduated sleeve or barrel
- (e) Thimble
- (f) Ratchet or friction stop
- (g) Spindle clamp

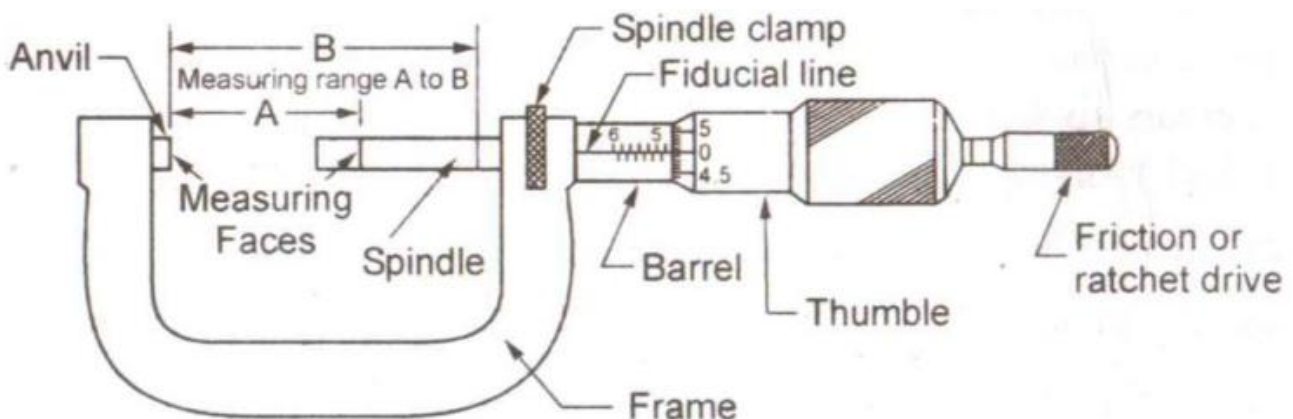


Fig 11.Micrometer

The frame is made of steel, malleable cast iron or light alloy. The anvil shall protrude from the frame for a distance of at least 3-mm in order to permit the attachment of measuring



wire support. The spindle does the actual measuring and possesses the threads of 0.5 mm pitch. The barrel has datum and fixed graduations. The thimble is a tubular cover fastened with the spindle. The beveled edge of the spindle is divided into 50 equal parts, every fifth being numbered. The ratchet is a small extension to the thimble. It slips when the pressure on the screw exceeds a certain amount. It produces uniform reading and prevents damage or distortion of the instruments. The spindle clamp is used to lock the instrument at any desired setting.

✓ **Procedure for Reading in a Micrometer**

The graduation on the barrel is in two parts divided by a line along the axis of the barrel called the reference line. The graduation above the reference is graduated in 1 mm intervals. The first and every fifth are long and numbered 0, 5, 10, 15, etc. The lower graduations are marked in 1 mm intervals but each graduation shall be placed at the middle of the two successive upper graduations to be read 0.5mm. The thimble advances a distance of 0.5 mm in one complete rotation. It is called the pitch of the micrometer. The thimble has a scale of 50 divisions around its circumference. Thus, one smallest division of the circular scale is equivalent to longitudinal movement of $0.5 \times \frac{1}{50} \text{ mm} = 0.01\text{mm}$. It is the least count of the micrometer.

The job is measured between the end of the spindle and the anvil that is fitted to the frame. When the micrometer is closed, the line marked zero on the thimble coincides with the line marked zero on the barrel. If the zero graduation does not coincide, the micrometer requires adjustment.

To take a reading from the micrometer, (1) the number of main divisions in millimeters above the reference line, (2) the number of sub-divisions below the reference line exceeding only the upper graduation, and (3) the number of divisions in the thimble have to be noted down. For example if a micrometer shows a reading of 8.78 mm when

8 divisions above the reference line	= 8.00mm
1 division below the reference line	=.5mm
28 thimble divisions	=0.28mm

8.78

The various important terms used in connection with micrometers are given below

Backlash

It is the total travel of the measuring spindle for a given micrometer

Measuring Range

It is the total travel of the measuring spindle for a given micrometer.

Cumulative Error

It is the deviation of measurement from the nominal dimension determined at any optional point of the measuring range. It includes the effect of all possible individual errors such as errors of the thread, errors of measuring faces etc. It can be determined by using slip gauges.

The following are the various types of micrometers



Inside Micrometer Caliper

The measuring tips of inside micrometer are constituted by jaws with contact surface, which are hardened and ground to a radius. Unlike the conventional micrometer, an inside micrometer does not have any U-shape frame and spindle. One of the jaws is held stationary at the end and second one moves by the movement of the thimble. A locknut is provided to check the movement of the movable jaw. This facilitates the inspection of small internal dimension.

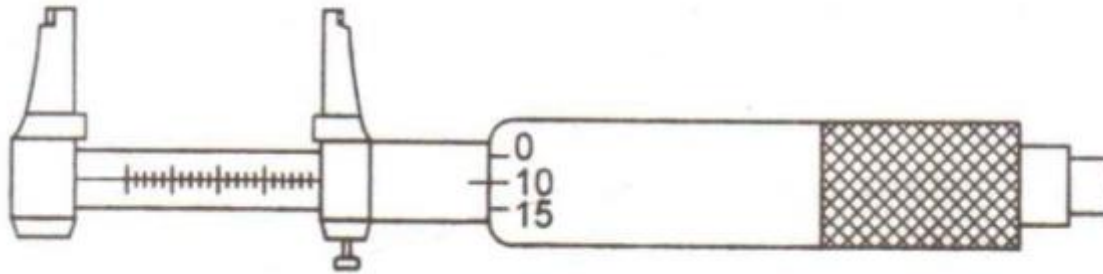


Fig 12. Inside Micrometer Caliper



Inside Micrometer

The inside micrometer is intended for internal measurement to an accuracy of 0.001 mm. In principle, it is similar to an external micrometer and is used for measuring holes with a diameter over 50 mm. It consists of :

- (a) measuring unit
- (b) extension rod with or without spacing collar, and
- (c) handle.

When the micrometer screw is turned in the barrel, the distance between the measuring faces of the micrometer can vary from 50 to 63 mm. To measure the holes with a diameter over 63 mm, the micrometer is fitted with extension rods. The extension rods of the sizes 13, 25, 50, 100, 150, 200 and 600 mm are in common use.

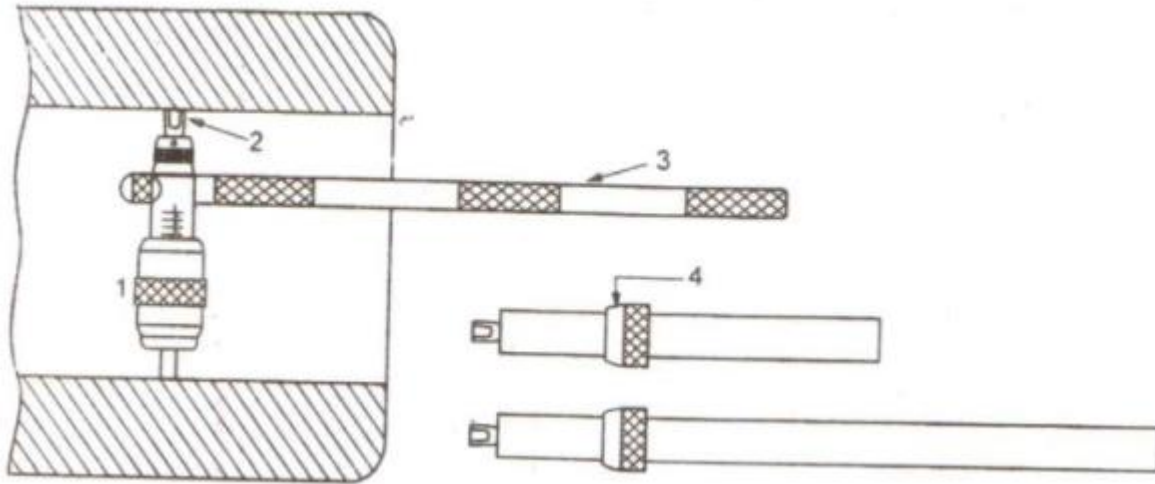


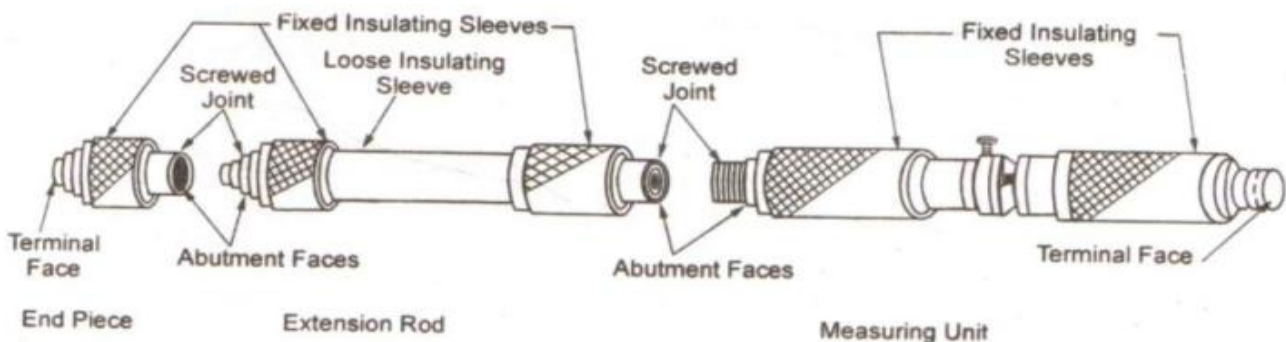
Fig 13. Measuring the Inside Diameter of a Hole by an Inside Micrometer (1) Micrometer,

(2) Anvil, (3) Handle and (4) Extension Rod

The measuring screw has a pitch of 0.5 mm. The barrel or sleeve is provided with a scale of 13 mm long and graduated into half-millimeter and millimeter divisions as in the external micrometer. A second scale is engraved on the beveled edge of the thimble. The beveled edge of the thimble is divided into 50 scale divisions round the circumference. Thus, on going through one complete turn, the thimble moves forward or backward by a thread pitch of 0.5 mm, and one division of its scale is, therefore, equivalent to a movement of $0.5 \times 1/50 = 0.01$ mm

✓ **Stick Micrometers**

Stick micrometers are used for measurement of longer internals length. A series of extension rods will permit continuous range of measurement up to the required length. It is connected with a 150 mm or 300 mm micrometer unit fitted with a micrometer of 25 mm range and having rounded terminal faces. Screw joints are used for joining the end-piece, extension rod and the measuring unit. The extension rod is generally hollow and has minimum external diameter of 14 mm. The accuracy of this instruments is in order of ± 0.005 mm. Figure 5.14 shows the parts of a stick micrometer



**Fig 14. Stick Micrometer
Screw Thread Micrometer Caliper**

✓

The shape of a Screw thread Micrometer is more or less like an ordinary micrometer with the difference that it is equipped with a pointed spindle and a double V-anvil, both correctly shaped to contact the screw thread of the work to be gauged. The angle of the V-anvil and the conical point at the end of the spindle correspond to the included angle of the profile of the thread. The extreme point of the cone is rounded so that it will not bear on the root diameter at the bottom of the thread, and similarly clearance is provided at the bottom of the groove in the V-anvil so that it will not bear on the thread crest. The spindle point of such a micrometer can be applied to the thread of any pitch provided the form or included angle is always same.

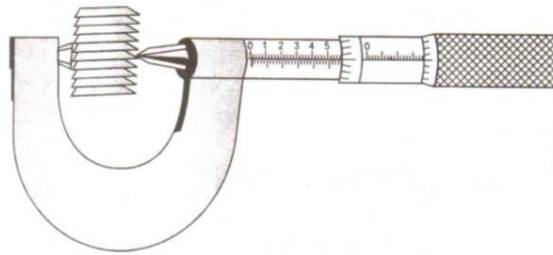


Fig 15.Screw Thread Micrometer Caliper

✓ **V-anvil Micrometer Caliper**

This is a special purpose micrometer used for checking out-of-roundness condition in centreless grinding and machining operations, odd-fluted taps, milling cutters, reamers etc. Use of special fixtures is eliminated in this type of micrometer.

The V equals 60 degrees and the tip of the Vee coincides with axis of spindle. The zero reading of micrometer starts from a point where the two sides of the V meet. Figure 5.16 shows a V-anvil micrometer caliper

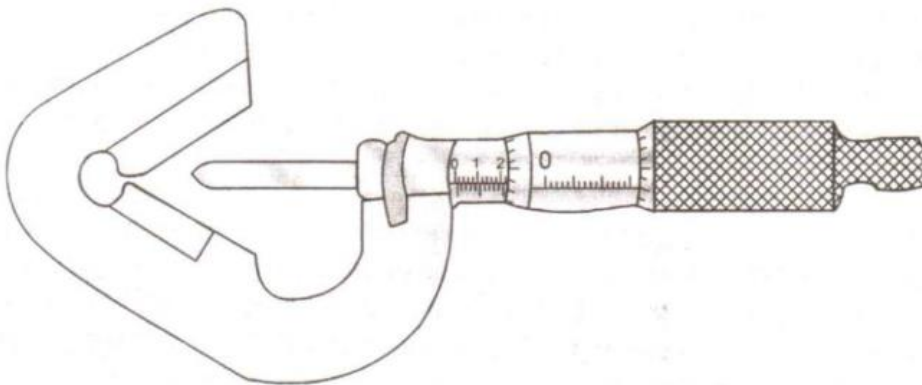


Fig 16.V-anvil Micrometer Caliper

Blade Type Micrometer

It is ideally suited for fast and accurate measurement of circular formed tools, diameters and depth of all types of narrow grooves, slots, keyways, recesses etc. It has non-rotating spindle which advances to contact the work without rotation.

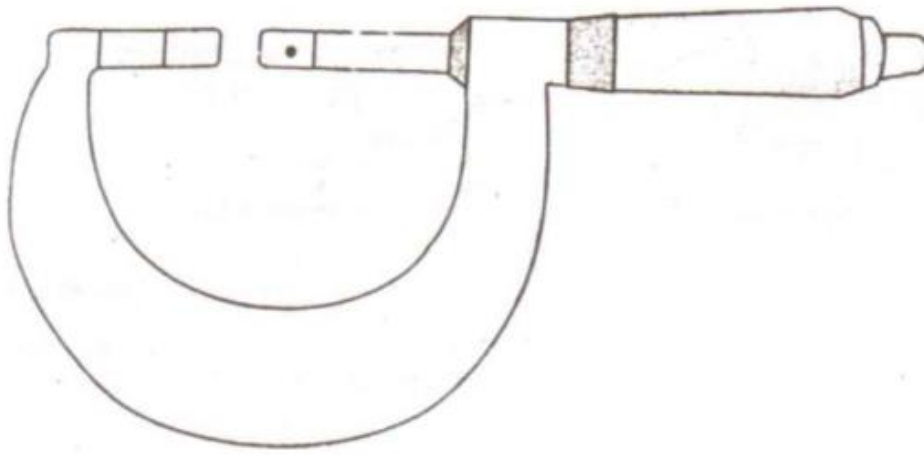


Fig 17.

✓ **Bench Micrometer**

A bench micrometer is a high precision micrometer with an anvil retractor device for repeated measurement. The worktable is adjustable and the indicator can measure up to 1 μm . The Anvil pressure is adjustable and linear friction transfer mechanism is used between anvil and indicator for high accuracy.

✓

Groove Micrometer

It is used for measuring grooves, recesses and shoulders located inside a bore. Standard discs with diameter 12.7 mm and 6.35 mm are used to measure the locations inside a small bore. It is also capable of measuring an edge of a land and groove

✓ **Blade Type Micrometer**

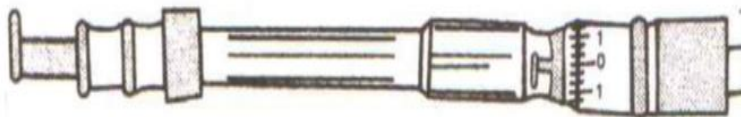


Fig 18. Groove Micrometer

✓ **Digital Micrometer**

Digital micrometer is capable of giving direct reading up to 0.001 mm. The spindle thread is hardened, ground and lapped in this type of micrometers. The positive locking clamp ensures locking of spindle at any desired setting. Operation is very simple with push button controls for “Zero” reset and indication “hold”

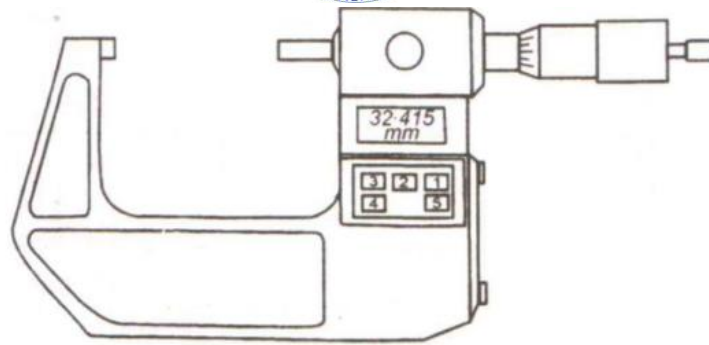


Fig 19.Digital Micrometer

- **Height Gauge**

This also uses the same principle of vernier caliper and is used especially for the measurement of height. It is equipped with a special base block, sliding jaw assembly and a removable clamp. The upper and lower surfaces of the measuring jaws are parallel to the base, which make possible to measure both over and under surfaces. A scribing attachment in place of measuring jaw can be used for scribing lines at certain distance above the surface. Specification of a vernier height gauge is made by specifying the range of measurement, type of scale required and any particular requirement in regard to the type of vernier desired.

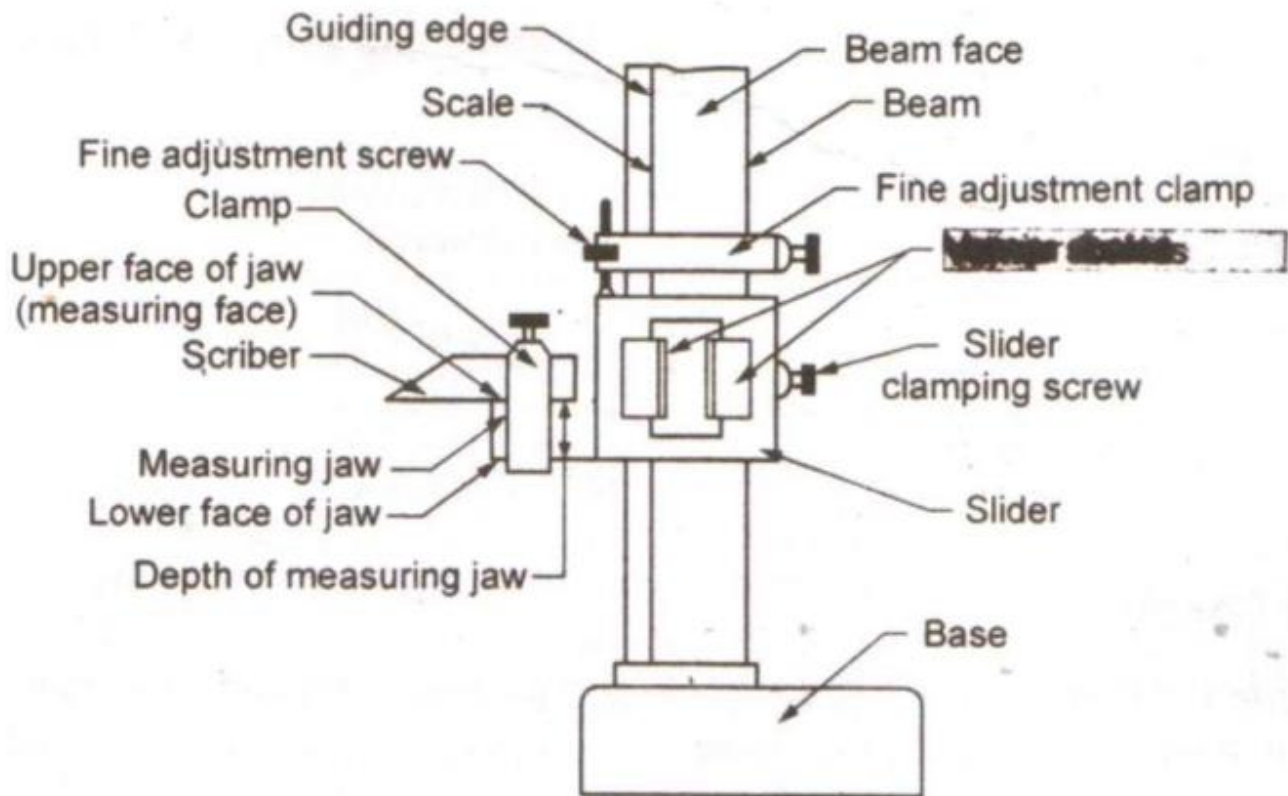


Fig 20.Vernier Height Gauge

**Self-Check-2****Written test**

choose the best answer for the following question (2 point each)

1. -----is the science of measurement

A, mensuration B, metrology C, geometric D, none

2. -----the mathematical name for calculating the volume , length area &etc.

A, geometric B, mensuration C, metrology D, c & a

3. vernier scale it slide on the -----..

A, jaw B, upper jaw C, main scale D, all

4. vernier depth gauge is used for measuring depth of hole &slots. .

A. true B. false

5. Vernier height gauge is measuring height of an object &marking line on object of given distance from datum base. .

A, true B, false C, no answer

6, on the Micrometer -----ensure a uniform pressure b/n the measuring surface. .

A, thimble B, anvil C, ratchet stop D, spindle lock nut

Note: Satisfactory rating - 6 points

Unsatisfactory - below 6 points

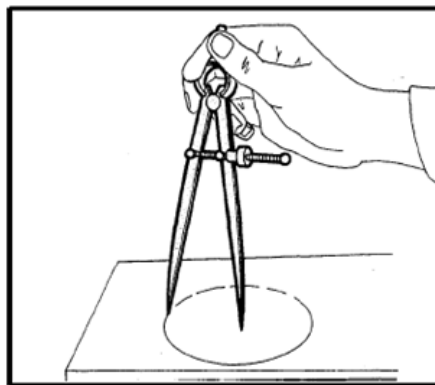
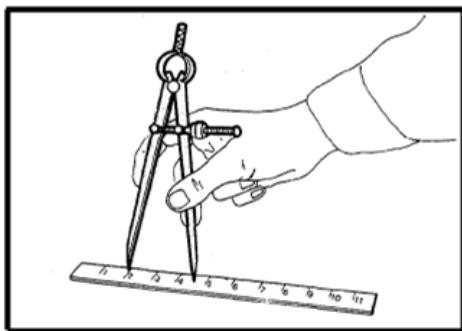
You can ask you teacher for the copy of the correct answers.

Operation Sheet No. 1**Title: - Select and identify measuring tools****Purpose: - Reading measurements by Using a Divider****Demands:** Measure Work piece and Obtain Accurate **measurements** to limit of the accuracy of the tool/ Instruments**Materials/Tools/ Equipment Needed:**

1. Students Guide
2. Steel ruler
3. Object to measure
4. divider
5. Pencil or pen
6. Paper

Activities:

1. Set the desired radius on the dividers using the appropriate graduations on a rule.
2. Place the point of one of the divider legs on the point to be used as the center.
3. Lean the dividers in the direction of movement and scribe the circle by revolving the dividers





3.1 MEASURING INSTRUMENTS

-Measuring instrument is a types of instrument that used to measure an object.
-To measure means to test. To test is to determine whether the work piece & materiel fulfill the specified requirements. Testing consists of compare the achieved size color, surface quality, strength, heat resistance mass etc with the desired specification or standard. Measuring & testing are continuous process throughout manufacturing weather working with hand tools.Measurement may be direct or indirect

3.1.1 Direct measurements are: vernier caliper, micrometer etc

3.1.2 Indirect measurements are: dial gauge indicator, calipers set to plug gauge

3.2 Destination between measuring & gauging

- The two basic activities involved in testing liner dimensions are measuring & gauging.
- Measuring consists of the numerical comparison of the length to be measured with a physical of measure.
- The observation contained the real value.
- Gauging is the method of ascertaining whether the test object confirms to specified limits regarding length, angle or shape etc

3.3 Measuring tools & instruments

3.3.1 Gauges: are used to test the dimensions as well as the shapes of work pieces. E.g. Profile gauges, measuring gauges, limiting gauges

3.3.2 Engineer's steel rule (metric):is also called steel rule because it is made of carbon steel or stainless steel. The rule is usually provided with a hole at its end for safe storage. The "zero" mark on a rule is made on the extreme end.



Fig 1. Engineer's steel rule.



- ✓ metric steel rule is graduated in millimeters & half millimeters. These Graduations are divisions of lines.
- ✓ Division is a space between two line
- ✓ The smallest division is half millimeter & the largest division is 10 millimeters (mm).
- ✓ The steel rule is used to measure distance that does not require any great accuracy. in addition they are used.
 - A. To measure size of work
 - B. Checking the marking on a wok piece
 - C. Setting other tools such as a pair of dividers

N.B. Errors in measurement with steel rule can occur from any or combination of the following.

- A. Wear on the end of the rule
- B. Graduations errors in the manufacturing of the rule
- C. Rule not holds parallel or at right angles to the work piece.

N.B. for general use steel rules are made in lengths up to 150mm & 300mm, & for larger lengths up to 2metter For greater lengths steel tapes (flexible steel rules) are used. They may have a length of up to 5metter.

- **Accuracy:** of an instrument is the lowest dimension that can be measured using the tool or it is the extent to which the reading it gives might be wrong.

Eg. Steel rule has an accuracy of $\pm 0.5\text{mm}$

-Vernier caliper has an accuracy of $\pm 0.1, 0.2, 0.05\text{mm}$

-Micro meter has an accuracy of $\pm 0.01, 0.02, 0.05\text{mm}$ etc

Eg. A piece of metal is measured its length using steel rule & reads $20 \pm 0.5\text{mm}$, then the measuring value may be $20 + 0.5 = 20.5$ or $20 - 0.5 = 19.5\text{mm}$

- **Precision:** is used to describe the closeness occurring between the results obtained for a quantity when it is measured several times under the same condition
-
- **The error of measurement:** is the difference between the result of the measurement & the true value of the errors may be random or systematic.
 - In measuring, the height of permissible value is the maximum limit & the lowest permissible value is the minimum limit.

N.B. the difference between these two limits is called **tolerance**.

Eg. Normal dimension of the work piece specified $32.5 \pm 0.2\text{mm}$.then the maximum & minimum limit is as follows

$$ML = 32.5 + 0.2 = 32.7\text{mm}$$

$$ml = 32.5 - 0.2 = 32.3\text{mm}$$

$$\text{Tolerance} = 32.7 - 32.3 = 0.4\text{mm}$$

N.B. The convenient measuring unit in general mechanics is millimeter (metric) & inch (with orth) That is 1 inch = 25.54mm

3.3.3 Measuring with vernier caliper

- Vernier calipers used to measure (take) internal, external, depth measurements. It is made from high quality alloy & instrument steels. - Vernier calipers have one fixed & one movable jaw.
- N.B. Using vernier calipers:
 - A. Taking external measurements
 - B. Taking internal measurements
 - C. Taking depth of a hole or grooves

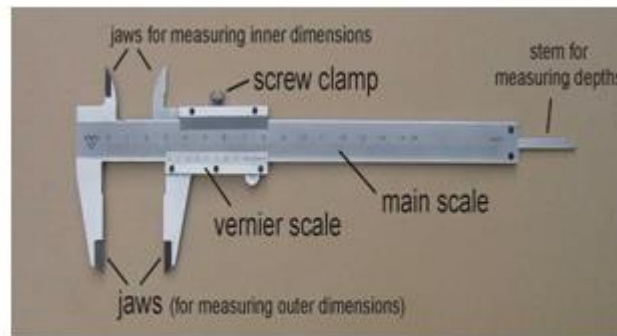


Fig 2. vernier caliper

- The common parts are beam which incorporates the fixed jaws & the main scale, the sliding jaw, which moves along the beam & to the object to be measured
- The slanted vernier scale values are, $1/10\text{mm}$, $1/20\text{mm}$ or $1/50\text{mm}$. the standard length of the $1/10\text{mm}$ is 19mm & the $1/20\text{mm}$ vernier scale length is 39mm & also for $1/50\text{mm}$ standard the length is 49mm

- **Care of the vernier calipers:**

- The following points should be remembered while using vernier calipers,
 - A. Dropping the vernier caliper is forbidden
 - B. Always clean & close the jaws in to their position & place the calipers in its case after use.
 - C. Calipers should be oiled to prevent from rust.
 - D. Ensure that all the screws are in position at all times.

3.3.4 MICRO METER

- Micrometer is commonly used when a part has to be measured to the second place of decimal in metric system. It gives more accurate measurements than steel rule. Micrometers are divided into outside, inside & depth micrometers & are used for taking:
 - A. External
 - B. Internal
 - C. Depth measurements

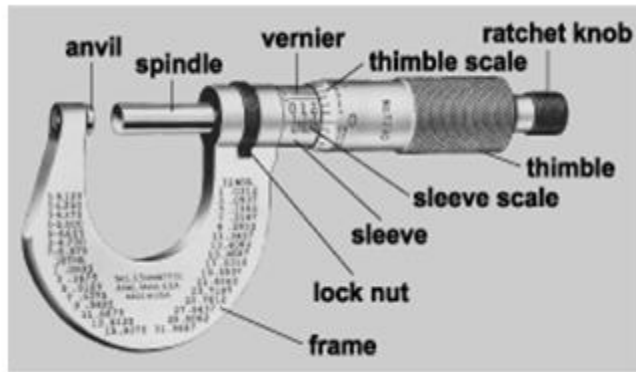


Fig 3. Micrometer

-Spindale & anvil face are the measuring faces made from tungsten carbide. Lock nut used to lock the spindle before reading is taken. Sleeve has measuring graduations for the main scale.

N.B. Micro meter used to measure 0.01mm or smaller.

-It is very accurate. We have three types of micrometer, these are:

- A. Outside micro meter: used to measure outside diameter of an object.
- B. Inside micrometer: used to measure parts of rings, slots & tubes.
- C. Depth micro meter: used to measure holes, slots & steps.

• **READING THE MICROMETER**

– When a complete turn of the micrometer spindle is made, it makes movements of 0.5mm. This is because of the screw of the micrometer has a pitch of 0.5mm. So that the jaws open 0.5mm for each turn of the thimble is divided (graduated) in to 50 parts÷ which gives a reading of $0.5 \div 50 = 0.01$.

Fig. Reading the micro meter (12.65)

-When reading the micrometer, we have to follow the following things

- A. The number of whole millimeter visible on the sleeve
- B. The half millimeters on the sleeve
- C. The thimble division coinciding with the datum line.

-The reading is taken as follows

- A. The number of whole millimeters ----- 12
- B. The half millimeters -----0.5
- C. The number of thimble divides (15x 0.01)-----0.15

The reading ----- 12.65mm

-N.B. Measure mentees are made between the anvil & the spindle.

• **CARE OF MICROMETER**

- A. Not to be handled liner than necessary.
- B. Not to be knocked to the floor & damage.
- C. Avoid the possibility of error by cleaned before measurement is taken etc ---

3.3.5 PROTRACTOR

-The measuring instruments used to measure the angle of the work pieces. There are two types of protractor. These are:

- A. Plain bevel protractor
- B. Vernier protractor

- **Plain bevel protractor:** is one of the common protractors used in general mechanic work shop. It made from tool steel, hardened & tempered. The tool has two parts, these are

- ✓ Protractor, which is graduated in degrees from 0 degree to 90 degree on either side of the 90 degree mark.
- ✓ A blade, which is longer & held on to the protractor by a knurled lock nut.

-The blade can be set at a various angles. The plain bevel protractor has an accuracy of degree, & hence it is not convenient for accurate (precision) work



Fig 4. plain bevel protractor.

- Vernier protractor: is another type of measuring instruments which is fitted to the vernier scale enabling angles to read to within 5 minutes of arc. This protractor is used to measure angle from 0 degree to 108 degree. It consists of:

- ✓ Protractor dial graduated in degrees
- ✓ A base with a vernier scale attached
- ✓ A sliding blade which can be extended & set in all direction

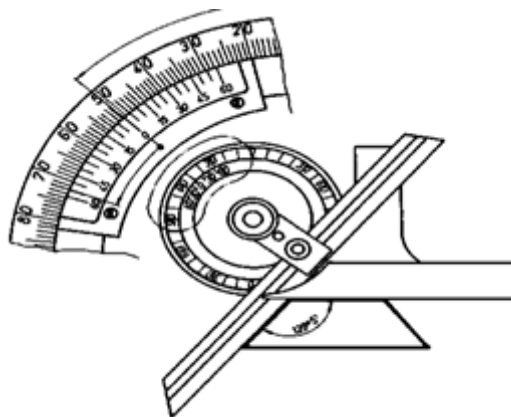


Fig 5. vernier protract

- **READING THE VERNIER PROTRACTOR**



- ✓ Read the number of whole degree between the zero on the main scale & zero on the vernier scale.
- ✓ Count the number of division of spaces from zero on the vernier scale to the point where a vernier line coincides with a line on the main scale
- ✓ Multiply this number by five (each division on the vernier represents 5minutes).then add to the whole number of degrees.

E.g From the figure, we get the following results,

- A. The number of whole degree is 60 degree
- B. The coinciding mark of the vernier scale & main scale is on the fourth line which is $4 \times 5 \text{ minute} = 20 \text{ minute}$.
- C. Therefore the reading is 60 degree, 20 minute

3.3.6 VERNIER HEIGHT GAUGE

-It used to measure the heights to within an accuracy of 0.02mm. It made from high quality alloy steel & has the following parts.

- A. A HEAVY BASE: which is flat at the bottom that slides on the surface plate
- B. VERTICAL BEAM: which is graduated in millimeters,& has a 300 mm height
- C. VERNIER SCALE: that slides up & down the beam. It has two locking screws & fine adjustment nut & screw.
- D. A SCRIBER: held on to the vernier scale. Used to make line on the work pieces.

-Height gauge is mostly used to for lay out work.

-It placed on the surface plate

-It also used for inspection.

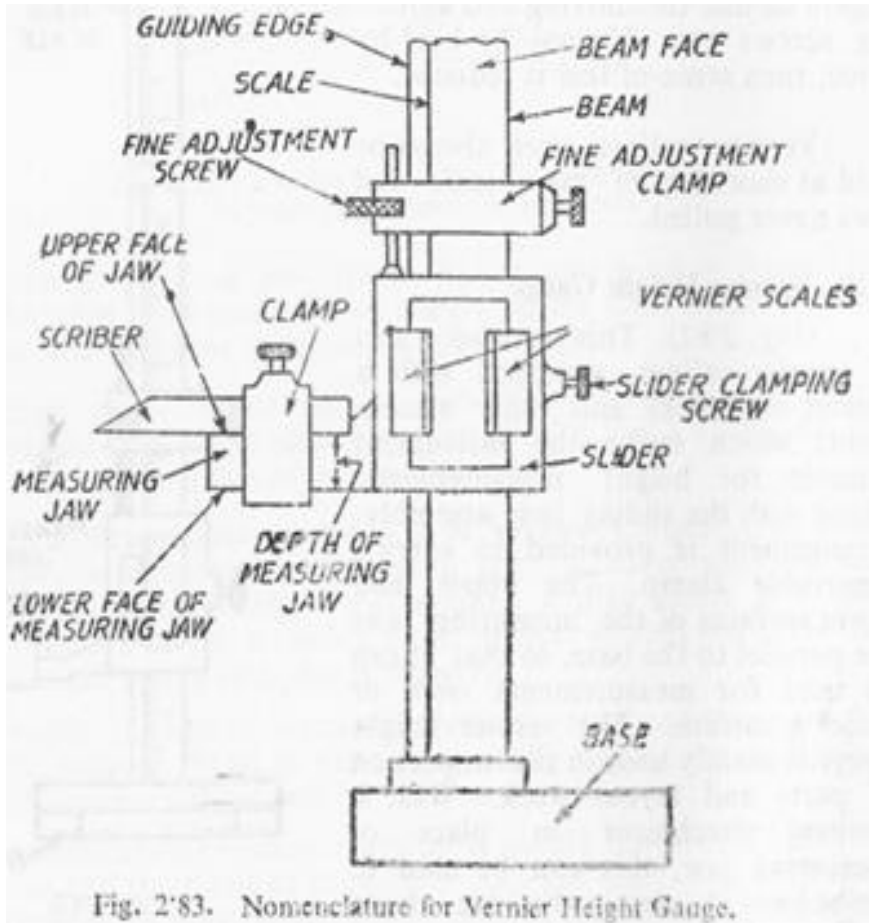


Fig 6. vernier height gauge.

3.3.7 FEELER GAUGE

A FEELER GAUGE: is an instrument which consists of a series of different sizes of blades used for checking gaps & clearance between surfaces ,mating parts ,bearing clearances, errors in square ness, & when setting up work or adjusting tools in machines.

-Blades ranging in size are from 0.04 mm to 5.0 mm.

There are two ranges of feeler gauges.

- One type has thirteen (13) blades whose thickness in mm. these are 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, and 1.0.
-The length of each blade is 100mm & it is tapered in width.
- The other type has ten (10) blades whose thick ness in mm is 0.05, 0.1, 0.15, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, & 0.8. The length of each blade is 75mm & is tapered in width. Sometimes blades range from 0.04 to 5.0mm.



Fig 7. feeler gauge



- **Depth gauge:** used to measure grooves, holes, & depth
- **Radius gauge:** used to measure the rounding of the corners.
 - ✓ Internal radius gauge: used to measure internal surface.
 - ✓ External radius gauge: used to measure external surface.
- **Pitch gauge:** used to measure threads.
 - ✓ Major diameter (D)
 - ✓ Minor diameter (d)
- **Screw gauge:**
 - ✓ Ring gauge: used to test external threads.
 - ✓ Plug gauge: used to test internal threads

3.3.8 THE ENGINEER'S TRY SQUARE

- It also called solid Steel Square or right edge.
- Used to check the square ness of two surfaces
- The solid steel square has two main parts these are,
 - A. Blade: made of hardened steel. Has a straight & parallel edge.
 - B. Stock: made of hardened steel. Has straight & parallel surface.
- The blade & stock are fixed such that two accurate right angles.
- Three uses of a solid square:
 - A. To check a surface for flatness
 - B. To determine ,if two surfaces are at right angles or square to each other
 - C. To check the accuracy of other squares

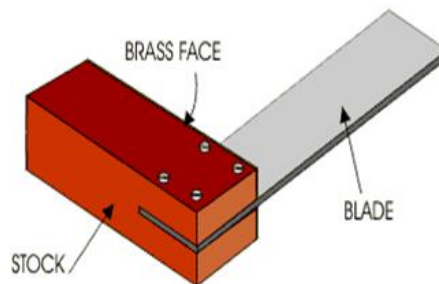


Fig 8.Engineer's try square

3.3.9 CALIPERS

- Used to measure the distance in directly & these measuring values are transferred to the steel rule or other convenient measuring instrument.
- Used to measure the diameter of the holes, the diameter of round bares etc.
- The common types of calipers are the following
 - A. Outside calipers
 - B. Inside calipers
 - C. Odd leg or hermaphrodite calipers
 - Outside calipers: are two legged steel instruments with these legs bent inside.
- Used to measure diameter of round object, to test the thickness of plates & for testing parallel surfaces
- The distance between the legs is measured by the rule

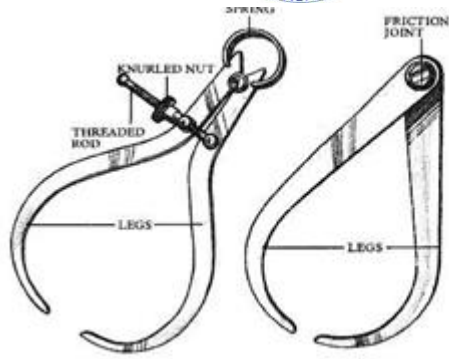


Fig 9.outside caliper

- **The inside calipers:** are two legged steel instruments bent out wards. They are used for testing the diameter of holes, the distance between shoulders & the sides of the holes for parallelism

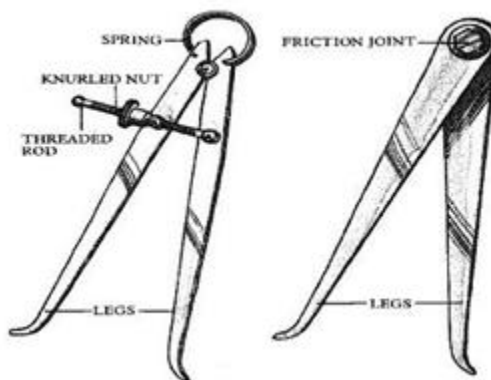


Fig 10. inside calipers

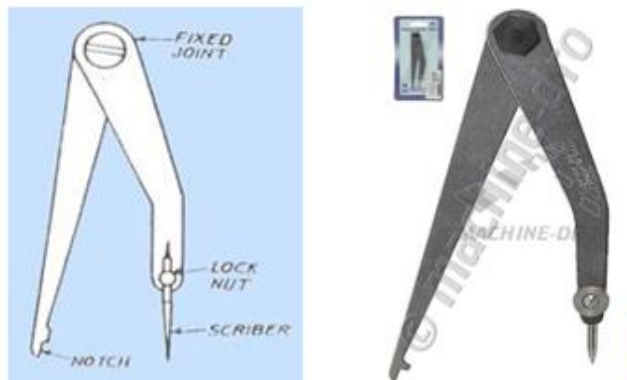


Fig 11. An odd leg calipers & its parts

**Self-Check-3****Written test**

choose the best answer for the following question (2 point each)

1. The inside calipers with two legged steel instruments bent out wards are used for testing.
A. diameter of holes, B. the distance between shoulders C. the sides of the holes for parallelism. .
D. All of the above
2. One of the following is not the uses of a solid square. .
A. To check a surface for flatness
B. To determine if two surfaces are at right angles or square to each other
C. To check the accuracy of other squares
D. None
3. Calipers should be oiled to prevent from rust. .
A. True B. False
4. Which one of the following instruments is used to measure angle from 0 degree to 108 degree. .
A. Caliper B. Micrometer C. protractor D. feeler gauge

Note: Satisfactory rating - 4 points

Unsatisfactory - below 4 points

You can ask you teacher for the copy of the correct answ



Operation Sheet -2

alternative measuring tools

Operation Sheet No. 2

Title: - alternative measuring tools

Purpose: - Take measurements with vernier caliper, an outside micrometer, a depth micrometer.

Demands: Measure Work piece and Obtain Accurate **measurements** to limit of the accuracy of the tool/ Instruments

Materials/Tools/ Equipment Needed:

1. Students Guide
2. Vernier caliper
3. Outside micrometer
4. Inside micrometer
5. Pencil or pen
6. Paper

Activities:

1. Taking external measurements
2. Taking internal measurements
3. Taking depth of a hole or grooves
4. Clean the measuring instrument.



LAP Test	Select measuring instruments
-----------------	-------------------------------------

Name: _____ Date: _____

Time started: _____ Time finished: _____

Instructions: Given necessary templates, tools and materials you are required to perform the following tasks within --- hour.

Task 1- Select and identify measuring tools

Task 2 - use alternative measuring tools



This learning guide is developed to provide you the necessary information regarding the following **content coverage** and topics:

- Obtain accurate measurements
- Perform trigonometric functions, algebraic computations
- Self-check numerical computation
- Construct where appropriate, formulae to enable problems to be solved
- Reading instruments

This guide will also assist you to attain the learning outcome stated in the cover page. Specifically, **upon completion of this Learning Guide, you will be able to:**

- . Obtain accurate measurements according to work requirements / ISO standard
- Perform calculation needed, including : trigonometric functions, algebraic computations to complete work tasks using the four basic process
- Self-check and correct numerical computation for accuracy
- . Construct where appropriate, formulae to enable problems to be solved based on applied calculations
- . Read **instruments** to the limit of accuracy of the tool

Learning Instructions:

1. Read the specific objectives of this Learning Guide.
2. Follow the instructions described below.
3. Read the information written in the “Information Sheets”. Try to understand what are being discussed. Ask your trainer for assistance if you have hard time understanding them.
4. Accomplish the “Self-checks” which are placed following all information sheets.
5. Ask from your trainer the key to correction (key answers) or you can request your trainer to correct your work. (You are to get the key answer only after you finished answering the Self-checks).
6. If you earned a satisfactory evaluation proceed to “Operation sheets
7. Perform “the Learning activity performance test” which is placed following “Operation sheets” ,
8. If your performance is satisfactory proceed to the next learning guide,
9. If your performance is unsatisfactory, see your trainer for further instructions or go back to “Operation sheets”.



1.1 . Definition: Accuracy is the ability of the instrument to measure the accurate value. In other words, it is the closeness of the measured value to a standard or true value. The accuracy can be obtained by taking the small readings

The accurate measurements are near the center. To determine if a value is accurate compare it to the accepted value. As these values can be anything a concept called percent error has been developed. Find the difference (subtract) between the accepted value and the experimental value, then divide by the accepted value

1.2. Accuracy & Precision

• Accuracy

Definition: Accuracy is the ability of the instrument to measure the accurate value. In other words, it is the closeness of the measured value to a standard or true value. The accuracy can be obtained by taking the small readings. The small reading reduces the error of the calculation. The accuracy of the system is classified in the following ways.

- 1. Point Accuracy** – Point accuracy means the accuracy of the instrument is only at the particular point on its scale. This accuracy does not give any information about the general accuracy of the instrument.
- 2. Accuracy as Percentage of Scale Range** – The uniform scale range determines the accuracy of the instrument. This can be easily be understood by the help of the example shown below.
3. Consider the thermometer having the range up to 500°C. The accuracy of the thermometer is considered up to ± 0.5 , i.e. ± 0.5 percent increases or decrease in the value of the instrument is negligible. But if the reading is more or less than 0.5°C, it is considered the high-value error.
- 4. Accuracy as Percentage of True Value** – Such type of accuracy of the instruments is determined by identifying the measured value regarding their true value. The accuracy of the instruments is neglected up to ± 0.5 percent from the true value.

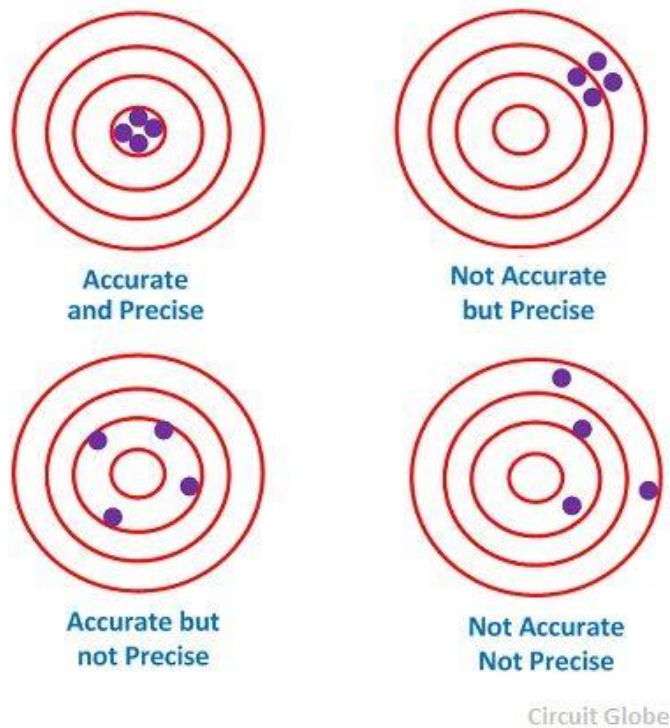


Fig 1.

- **Precision**

Definition: The term precision means two or more values of the measurements are closed to each other. The value of precision differs because of the observational error. The precision is used for finding the consistency or reproducibility of the measurement. The conformity and the number of significant figures are the characteristics of the precision. The high precision means the result of the measurements are consistent or the repeated values of the reading are obtained. The low precision means the value of the measurement varies. But it is not necessary that the highly precise reading gives the accurate result.

Example – Consider the 100V, 101V, 102V, 103V and 105V are the different readings of the voltages taken by the voltmeter. The readings are nearly close to each other. They are not exactly same because of the error. But as the reading are close to each other then we say that the readings are precise.

- **Ohm’s Law**

Ohm's law states that, in an electrical circuit, the current passing through most materials is directly proportional to the potential difference applied across them.

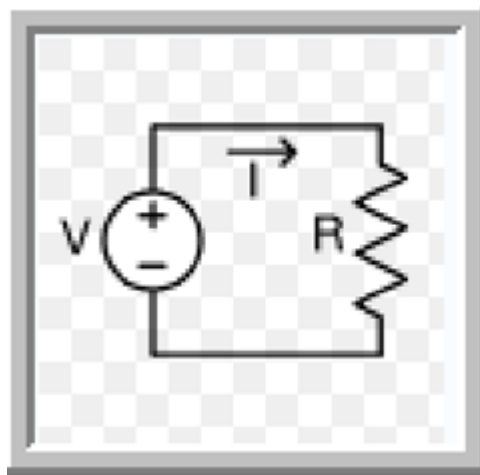


Fig.2

- Ohm's Law Formulas

There are three forms of Ohm's Law:

- ✓ $I = V/R$
- ✓ $V = IR$
- ✓ $R = V/I$

where:

I = Current , V = Voltage , R = Resistance

Fig. 3-4: A circle diagram to help in memorizing the Ohm's Law formulas $V = IR$, $I = V/R$, and $R = V/I$. The V is always at the top

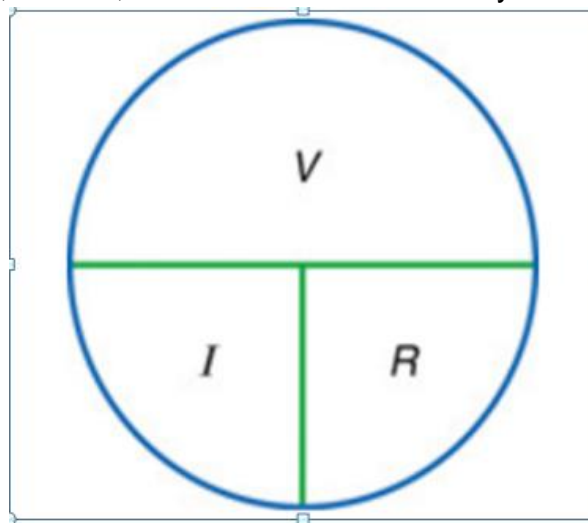


Fig .3

3-1: The Current $I = V/R$

$$I = V/R$$

In practical units, this law may be stated as: amperes = volts / ohms

Fig. 3-1: Increasing the applied voltage V produces more current I to light the bulb with more intensity.

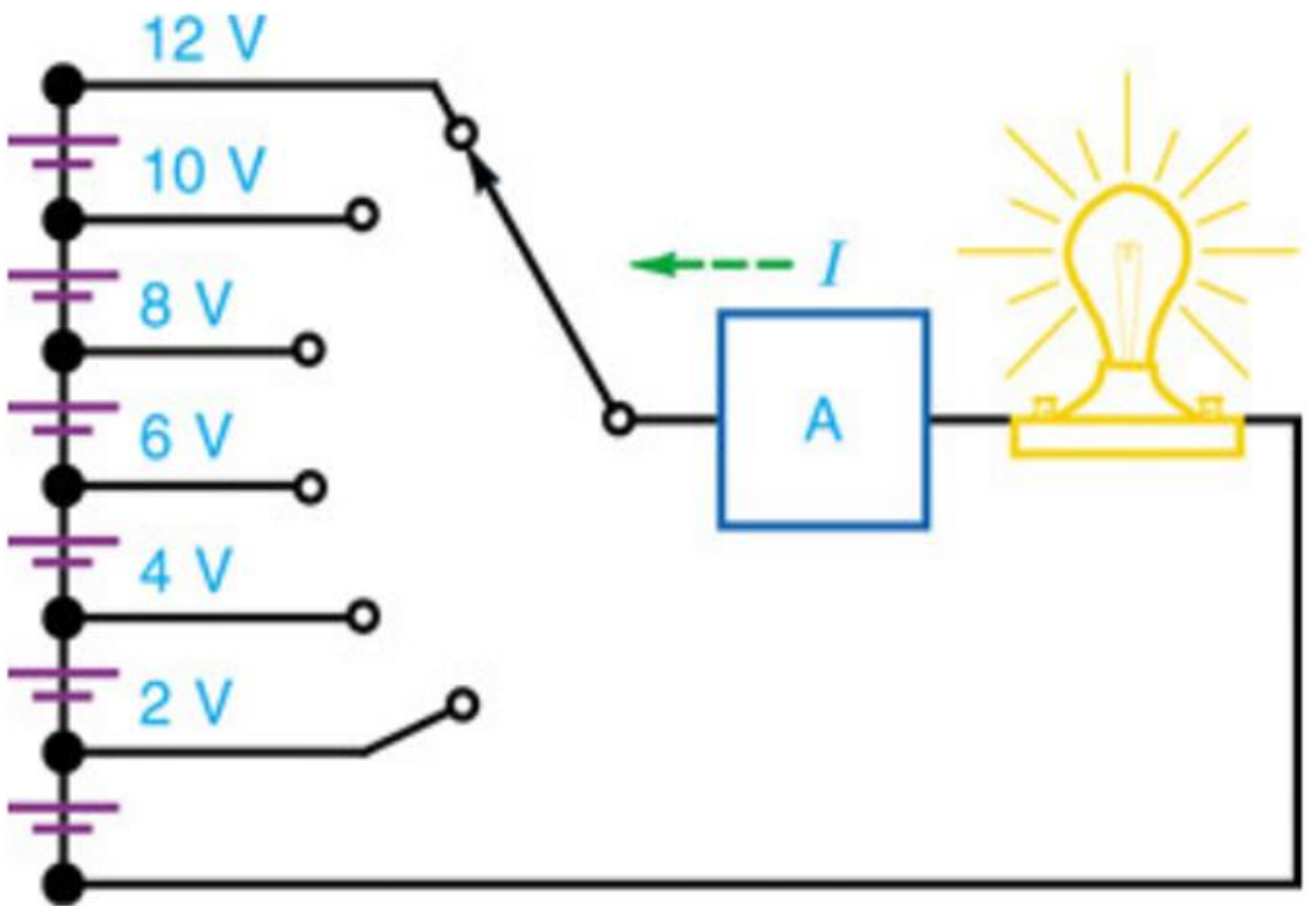


Fig . 4

3-4: Practical Units

The three forms of Ohm's law can be used to define the practical units of current voltage, and resistance:

$$1 \text{ ampere} = 1 \text{ volt} / 1 \text{ ohm}$$

$$1 \text{ volt} = 1 \text{ ampere} \times 1 \text{ ohm}$$

$$1 \text{ ohm} = 1 \text{ volt} / 1 \text{ ampere}$$

Applying Ohm's Law

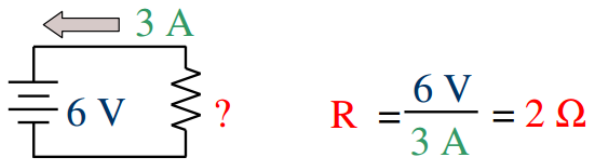
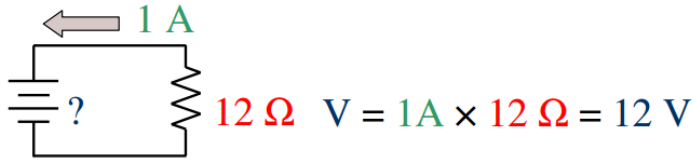
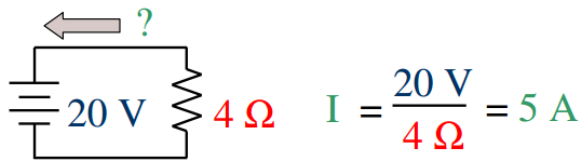
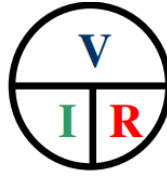


Fig . 5

Problem

Solve for the resistance, R, when V and I are known

- $V = 14 \text{ V}$, $I = 2 \text{ A}$, $R = ?$
- $V = 25 \text{ V}$, $I = 5 \text{ A}$, $R = ?$
- $V = 6 \text{ V}$, $I = 1.5 \text{ A}$, $R = ?$
- $V = 24 \text{ V}$, $I = 4 \text{ A}$, $R = ?$

3-5: Multiple and Submultiple Units

Units of Voltage The basic unit of voltage is the volt (V). Multiple units of voltage are: kilovolt (kV) 1 thousand volts or 10^3 V megavolt (MV) 1 million volts or 10^6 V Submultiple units of voltage are: millivolt (mV) 1-thousandth of a volt or 10^{-3} V microvolt (μV) 1-millionth of a volt or 10^{-6} V

3-5: Multiple and Submultiple Units

Units of Current The basic unit of current is the ampere (A). Sub multiple units of current are: milliampere (mA) 1-thousandth of an ampere or 10^{-3} A microampere (μA) 1-millionth of an ampere or 10^{-6} A

3-5: Multiple and Submultiple Units

Units of Resistance The basic unit of resistance is the Ohm (Ω). Multiple units of resistance are: kilohm (k Ω) 1 thousand ohms or $10^3 \Omega$ Megohm (M Ω) 1 million ohms or $10^6 \Omega$

Problem

How much is the current, I, in a 470-k Ω resistor if its voltage is 23.5 V? How much voltage will be dropped across a 40 k Ω resistance whose current is 250 μA ?

- **Wattage**



Electric power is the rate, per unit time, at which electrical energy is transferred by an electric circuit. The SI unit of power is the watt, one joule per second.

Electric power is usually produced by electric generators, but can also be supplied by sources such as electric batteries. It is usually supplied to businesses and homes (as domestic mains electricity) by the electric power industry through an electric power grid. Electric energy is usually sold by the kilowatt hour ($1 \text{ kW}\cdot\text{h} = 3.6 \text{ MJ}$) which is the product of the power in kilowatts multiplied by running time in hours. Electric utilities measure power using an electricity meter, which keeps a running total of the electric energy delivered to a customer.

Electrical power provides a low entropy form of energy and can be carried long distances and converted into other forms of energy such as motion, light or heat with high energy efficiency.^[1] Electric power, like mechanical power, is the rate of doing work, measured in watts, and represented by the letter P . The term wattage is used colloquially to mean "electric power in watts." The electric power in watts produced by an electric current I consisting of a charge of Q coulombs every t seconds passing through an electric potential (voltage) difference of V is

where

Q is electric charge in coulombs

t is time in seconds

I is electric current in amperes

V is electric potential or voltage in volts

What is voltage and wattage?

Volts are the base unit used to measure Voltage. One volt is defined as the "difference in electric potential between two points of a conducting wire when an electric current of one ampere dissipates one watt of power between those points." As the number of volts increases, the current increases too.

To determine the wattage, use a simple multiplication formula. The ampere (or amps) is the amount of electricity used. Voltage measures the force or pressure of the electricity. The number of watts is equal to amps multiplied by volts.

- **Frequency**

At its most basic, frequency is how often something repeats. In the case of electrical current, frequency is the number of times a sine wave repeats, or completes, a positive-to-negative cycle. The more cycles that occur per second, the higher the frequency. ... Power line frequency (normally 50 Hz or 60 Hz)

Role of frequency

In every case it is measured in Hertz or number of times per second. Mains **frequency** is the measure of the number of voltage cycles (polarity change) per second in the mains AC supply. Signal processing is all about electrical signal frequencies and how various circuits respond to them.

Relation between current, voltage and frequency



n AC electrical circuits, there are many components where many factors like current, voltage, impedance and frequency are correlated. Talking about inductive load, it's inductive reactance is directly proportional to frequency of operation and thus since current is inversely proportional to the inductive reactance

The formula for frequency is: f (frequency) = $1 / T$ (period). $f = c / \lambda =$ wave speed c (m/s) / wavelength λ (m). The formula for time is: T (period) = $1 / f$ (frequency). $\lambda = c / f =$ wave speed c (m/s) / frequency f (Hz)

- **End play**

The end play allows room for the formation of an oil film, misalignment, and thermal expansion of the bearing components. End play is the total distance the shaft can move between the two thrust bearings and is sometimes called float, thrust bearing clearance or axial clearance

This is the amount of clearance between the crankshaft's thrust plate and the vertical surface of the main thrust bearing. Mount a magnetic base to the engine and set the dial indicator to read off the crank snout. Gently pry the crank all the way forward and zero the gauge

Bearing internal clearance (fig. 1) is defined as the total distance through which one bearing ring can be moved relative to the other in the radial direction (radial internal clearance) or in the axial direction (axial internal clearance).

<https://www.engine labs.com/videos/>

- **conductance**

Conductance is an expression of the ease with which electric current flows through a substance. In equations, conductance is symbolized by the uppercase letter G . The standard unit of conductance is the siemens (abbreviated S), formerly known as the mho. When a current of one ampere (1 A) passes through a component across which a voltage of one volt (1 V) exists, then the conductance of that component is 1 S . The siemens is, in fact, equivalent to one ampere per volt. If G is the conductance of a component (in siemens), I is the current through the component (in amperes), and E is the voltage across the component (in volts), then:

$$G = I/E$$

In general, when the applied voltage is held constant, the current in a direct-current (DC) circuit is directly proportional to the conductance. If the conductance is doubled, the current is also doubled; if the conductance is cut to $1/10$ its initial value, the current also becomes $1/10$ as great. This rule also holds for most low-frequency alternating-current (AC) systems, such as household utility circuits. In some AC circuits, especially at high frequencies, the situation is more complex, because some components in these systems store and release energy, as well as dissipating or converting it.

Conductance is inversely related to resistance. If R is the resistance of a component or device (in ohms), then the conductance G (in siemens) is given by:

$$G = 1/R$$

- **Impedance:**

Since AC circuits containing reactance also contain resistance, the two combine to oppose the flow of current. This combined opposition by the resistance and the reactance is called the Impedance, and is represented by the symbol Z.

Assume you want to find the impedance of a series combination of 8 ohms resistance and 5 ohms inductive reactance. Start by drawing a horizontal line, R, representing 8 ohms resistance, as the base of the triangle. Then, since the effect of the reactance is always at right angles, or 90 degrees, to that of the resistance, draw the line X_L , representing 5 ohms inductive reactance, as the altitude of the triangle. This is shown in figure below. Now, complete the hypotenuse (longest side) of the triangle. Then, the hypotenuse represents the impedance of the circuit.

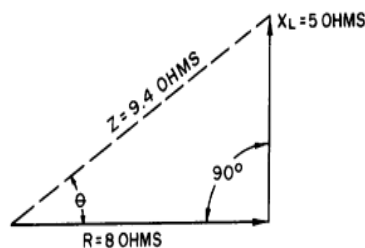


Fig . 6

Fig. the vector diagram relationship of resistance, inductive reactance, and impedance in a series circuit.

One of the properties of a right triangle is:

$$(\text{hypotenuse})^2 = (\text{base})^2 + (\text{altitude})^2$$

or,

$$\text{hypotenuse} = \sqrt{(\text{base})^2 + (\text{altitude})^2}$$

Applied to impedance, this becomes,

$$(\text{impedance})^2 = (\text{resistance})^2 + (\text{reactance})^2$$

or,

$$\text{impedance} = \sqrt{(\text{resistance})^2 + (\text{reactance})^2}$$

or,

$$Z = \sqrt{R^2 + X^2}$$

Now suppose you apply this equation to check your results in the example given above



Given: $R = 8 \Omega$
 $X_L = 5 \Omega$

Solution: $Z = \sqrt{R^2 + X_L^2}$
 $Z = \sqrt{(8 \Omega)^2 + (5 \Omega)^2}$
 $Z = \sqrt{64 + 25 \Omega}$
 $Z = \sqrt{89 \Omega}$
 $Z = 9.4 \Omega$

- **Capacitance**

A **capacitor** is a passive electronic component that stores energy in the form of an electrostatic field. In its simplest form, a **capacitor** consists of two conducting plates separated by an insulating material called the dielectric. ... Because of their tiny physical size, these components have low **capacitance**

What is the formula for capacitance?

The definition of **capacitance** is given by this **equation**: **capacitance** C, measured in farads, equals charge Q, measured in coulombs, divided by voltage V, measured in volts. The **capacitance** is based on the physical characteristics of the capacitor

What do you mean by capacitance?

Capacitance is the ability of a system of electrical conductors and insulators to store electric charge when a potential difference exists between the conductors. The symbol for **capacitance** is C. **Capacitance** is expressed as a ratio of the electrical charge stored to the voltage across the conductors.

Capacitance Formula. ... The **capacitance** is the collected charge divided by the voltage difference across the **capacitor**. **Capacitance** is measured in Farads (F), charge is measured in Coulombs (C), and voltage is measured in Volts (V). Be careful not to confuse **capacitance**: C, and the unit Coulombs: C

Electrical capacitance is a property of objects that can hold electric charge. A capacitor is an electric component that results from creating a small gap between charge-carrying layers, for example, a parallel-plate capacitor. The capacitance is the collected charge divided by the voltage difference across the capacitor. Capacitance is measured in Farads (F), charge is measured in Coulombs (C), and voltage is measured in Volts (V). Be careful not to confuse capacitance: C, and the unit Coulombs: C.

$$\text{capacitance} = \frac{\text{electric charge}}{\text{voltage drop across a capacitor}}$$

$$C = \frac{Q}{V}$$

C = capacitance (Farads, F)

Q = the charge built up on the capacitor (Coulombs, C)



V = voltage difference between two sides of a capacitor (Volts, V)

Capacitance Formula Questions:

- 1) In an electric circuit, a capacitor is holding a charge of 0.500 C . The voltage difference across the capacitor is 5.00 V . What is the capacitance?

Answer: The capacitance can be found using the formula:

$$C = \frac{Q}{V}$$
$$C = \frac{0.500\text{ C}}{5.00\text{ V}}$$
$$C = 0.100\text{ F}$$

The capacitance is 0.100 F , which can also be written in milli-Farads: 100 mF .

- 2) The charge held on a small parallel-plate capacitor is $100\text{ }\mu\text{C}$ (micro-Coulombs). The voltage difference across the capacitor is 20.0 mV (milliVolts). What is the capacitance?

Answer: The charge is given in units of μC . One micro-Coulomb is equal to one one-millionth of a Coulomb: $1\text{ }\mu\text{C} = 1/1000000\text{ C}$. The voltage is given in units of mV . One milliVolt is equal to one one-thousandth of a Volt: $1\text{ mV} = 1/1000\text{ V}$. Using these values, the capacitance can be found using the formula:

$$C = \frac{Q}{V}$$
$$C = \frac{100\text{ }\mu\text{C}}{20.0\text{ mV}}$$
$$C = \frac{100\text{ }\mu\text{C}}{20.0\text{ mV}} \times \frac{1/1000000\text{ C}}{1\text{ }\mu\text{C}} \times \frac{1\text{ mV}}{1/1000\text{ V}}$$
$$C = \frac{0.000100\text{ C}}{0.0200\text{ V}}$$
$$C = 0.00500\text{ F}$$

The capacitance is 0.00500 F , which can also be written in milli-Farads: 5.00 mF .

• Position, Displacement, And Distance

In describing an object's motion, we should first talk about position – where is the object? A position is a vector because it has both a magnitude and a direction: it is some distance from a zero point (the point we call the origin) in a particular direction. With one-dimensional motion, we can define a straight line along which the object moves. Let's call this the x -axis, and represent different locations on the x -axis using variables such as x_0 and x_1 , as in Figure below.



Positions $\vec{x}_0 = +3\text{ m}$ and $\vec{x}_1 = -2\text{ m}$, Where the $+$ and $-$ signs indicate the direction.

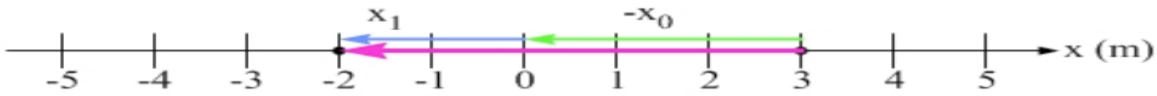
- **Displacement:** a vector representing a change in position. A displacement is measured in length units, so the MKS unit for displacement is the meter (m). We generally use the Greek letter capital delta (Δ) to represent a change. If the initial



position is and the final position is we can express the displacement as:
Displacement is given by

$$\Delta \vec{x} = \vec{x}_f - \vec{x}_i .$$

$\Delta \vec{x} = \vec{x}_1 - \vec{x}_0 = -2 \text{ m} - (+3 \text{ m}) = -5 \text{ m} .$, From the above position equation



To determine the displacement of an object, you only have to consider the change in position between the starting point and the ending point. The path followed from one point to the other does not matter. For instance, let's say you start at and you then have a displacement of 8 meters to the left followed by a second displacement of 3 meters right. The total distance traveled is the sum of the magnitudes of the individual displacements, 8 m + 3 m = 11 m. The net displacement (the vector sum of the individual displacements), however, is still 5 meters to the left:

- **Out of roundness**

- ✓ **Roundness Parameters**

- **E** = Eccentricity (ECC)*

This is the term used to describe the position of the center of a profile relative to some datum point. It is a vector quantity in that it has magnitude and direction. The magnitude of the eccentricity is expressed simply as the distance between the profile center (defined as the center of the fitted reference circle) and the datum point. The direction is expressed as an angle from the datum point.

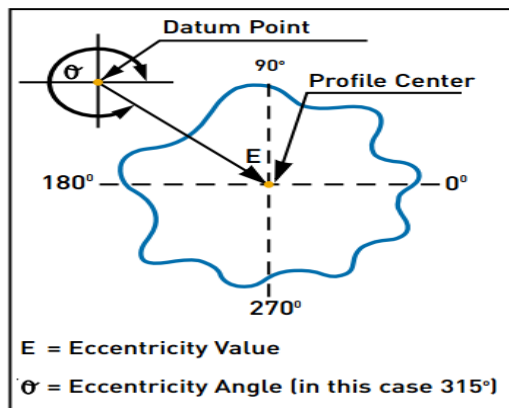


Fig. 7

- **⊙** = Concentricity (CONC)

This is similar to eccentricity but has only a magnitude and no direction. The concentricity is defined as the diameter of the circle described by the profile center when rotated about

the datum point. It can be seen that the concentricity value is twice the magnitude of the eccentricity

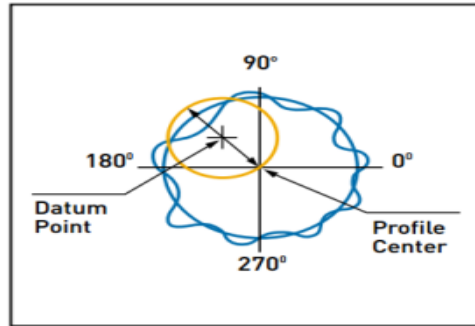


Fig. 8

 = **Runout** (Runout)

Sometimes referred to as TIR (Total Indicated Reading), Run out is defined as the radial difference between two concentric circles centered on the datum point and drawn such that one coincides with the nearest and the other coincides with the farthest point on the profile. Run out is a useful parameter in that it combines the effect of form error and concentricity to give a predicted performance when rotated about a datum.

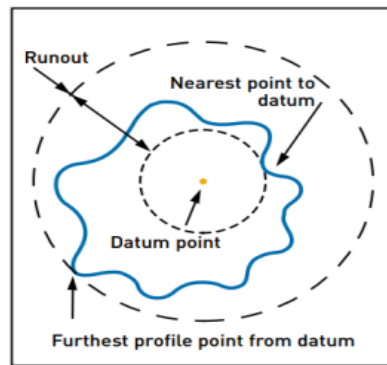



Fig. 9

 = **Flatness** (FLTt)

A reference plane is fitted and flatness calculated as the peak to valley departure from that plane. Either LS (least squares) or MZ (minimum zone) can be used.

• **Taper calculations**

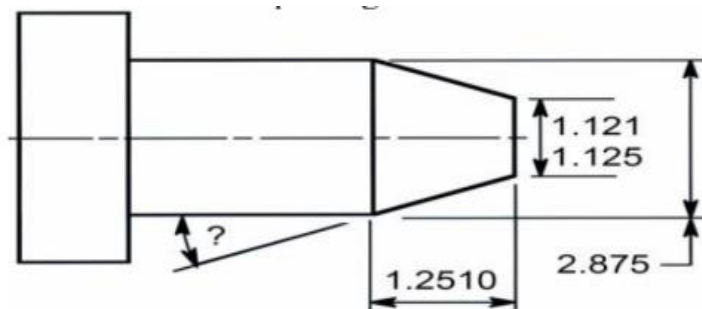
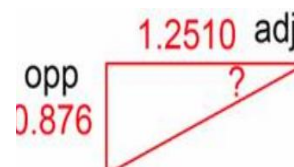


Fig. 10

Solution:

- Step 1. Find triangle
- Step 2. label known & needed
- Step 3. select trig rule = use TAN





- Step 4. $\tan \text{ angle} = \text{opp} / \text{adj}$
 $\tan \text{ angle} = 0.876 / 1.2510$
 $\text{angle} = \mathbf{35 \text{ degree}}$





Self-Check-1	Written test
---------------------	---------------------

Directions: choose the best answer for the following question (2 point each)

- 1. ability of the instrument to measure the accurate value.
A. precision B. Accuracy
- 2. The term ----- means two or more values of the measurements are closed to each other.
A. precision B. Accuracy
- 3. The accurate measurements are near the center.
A. True B. False

Note: Satisfactory rating - 3 points Unsatisfactory - below 3 points

You can ask you teacher for the copy of the correct answers.



2.1 Algebraic Expressions

A basic characteristic of algebra is the use of letters (or combinations of letters) to represent numbers. The letters used to represent the numbers are **variables**, and combinations of letters and numbers are **algebraic expressions**. Here are a few examples

$$3x, \quad x + 2, \quad \frac{x}{x^2 + 1}, \quad 2x - 3y$$

- **Definition of Algebraic Expression**

A collection of letters (called **variables**) and real numbers (called **constants**) combined using the operations of addition, subtraction, multiplication, division, and exponentiation is called an **algebraic expression**.

The **terms** of an algebraic expression are those parts that are separated by addition. For example, the algebraic expression $x^2 - 3x + 6$ has three terms: x^2 , $-3x$, and 6 . Note that x^2 is a term, rather than $x^2 - 3x$ because $x^2 - 3x + 6 = x^2 + (-3x) + 6$.

Think of subtraction as a form of addition

The terms x^2 and $-3x$ are called the **variable terms** of the expression, and 6 is called the **constant term** of the expression. The numerical factor of a variable term is called the **coefficient** of the variable term. For instance, the coefficient of $-3x$ is -3 , the variable term x^2 is a x^2 and the coefficient of the variable term is 1 . (The constant term of an expression is also considered to be a coefficient.)

Example 1 Identifying Terms and Coefficients

Identify the terms and coefficients in each algebraic expression.



(a) $5x - \frac{1}{3}$ (b) $4y + 6x - 9$ (c) $x^2y - \frac{1}{x} + 3y$

Solution

<i>Terms</i>	<i>Coefficients</i>
(a) $5x, -\frac{1}{3}$	$5, -\frac{1}{3}$
(b) $4y, 6x, -9$	$4, 6, -9$
(c) $x^2y, -\frac{1}{x}, 3y$	$1, -1, 3$

Properties of Algebra

The properties of real numbers (see Section P.2) can be used to rewrite algebraic expressions. The following list is similar to those given in Section P.2, except that the examples involve algebraic expressions. In other words, the properties are true for variables and algebraic expressions as well as for real numbers.

Properties of Algebra

Let a , b , and c be real numbers, variables, or algebraic expressions.

Property

Example

Commutative Property of Addition

$$a + b = b + a$$

$$5x + x^2 = x^2 + 5x$$

Commutative Property of Multiplication

$$ab = ba$$

$$(3 + x)x^3 = x^3(3 + x)$$

Associative Property of Addition

$$(a + b) + c = a + (b + c)$$

$$(-x + 6) + 3x^2 = -x + (6 + 3x^2)$$

Associative Property of Multiplication

$$(ab)c = a(bc)$$

$$(5x \cdot 4y)(6) = (5x)(4y \cdot 6)$$



Distributive Properties

$$a(b + c) = ab + ac$$

$$(a + b)c = ac + bc$$

$$2x(4 + 3x) = 2x \cdot 4 + 2x \cdot 3x$$

$$(y + 6)y = y \cdot y + 6 \cdot y$$

Additive Identity Property

$$a + 0 = 0 + a = a$$

$$4y^2 + 0 = 0 + 4y^2 = 4y^2$$

Multiplicative Identity Property

$$a \cdot 1 = 1 \cdot a = a$$

$$(-5x^3)(1) = (1)(-5x^3) = -5x^3$$

Additive Inverse Property

$$a + (-a) = 0$$

$$4x^2 + (-4x^2) = 0$$

Multiplicative Inverse Property

$$a \cdot \frac{1}{a} = 1, a \neq 0$$

$$(x^2 + 1)\left(\frac{1}{x^2 + 1}\right) = 1$$

Because subtraction is defined as “adding the opposite,” the Distributive Property is also true for subtraction. For instance, the “subtraction form” of

$$a(b + c) = ab + ac \text{ is}$$

$$\begin{aligned} a(b - c) &= a[b + (-c)] \\ &= ab + a(-c) \\ &= ab - ac. \end{aligned}$$

In addition to these properties, the properties of equality, zero, and negation given in Section P.2 are also valid for algebraic expressions. The next example illustrates the use of a variety of these properties

Example 2 Identifying the Properties of Algebra

Identify the property of algebra illustrated in each statement

(a) $(5x^2)3 = 3(5x^2)$

(b) $(3x^2 + x) - (3x^2 + x) = 0$

(c) $3x + 3y^2 = 3(x + y^2)$

(d) $(5 + x^2) + 4x^2 = 5 + (x^2 + 4x^2)$

(e) $5x \cdot \frac{1}{5x} = 1, x \neq 0$

(f) $(y - 6)3 + (y - 6)y = (y - 6)(3 + y)$

Solution

(a) This statement illustrates the Commutative Property of Multiplication. In other words, you obtain the same result whether you multiply $5x^2$ by 3, or 3 by $5x^2$.

(b) This statement illustrates the Additive Inverse Property. In terms of subtraction, this property simply states that when any expression is subtracted from itself the result is zero.



- (c) This statement illustrates the Distributive Property. In other words, multiplication is distributed over addition.
- (d) This statement illustrates the Associative Property of Addition. In other words, to form the sum

$$5 + x^2 + 4x^2$$

5 and x^2

x^2 and $4x^2$;

it does not matter whether are added first or are added first.

(e) This statement illustrates the Multiplicative Inverse Property. Note that it is important that x be a nonzero number. If x were zero, the reciprocal of x would be undefined.

(f) This statement illustrates the Distributive Property in reverse order.

$$ab + ac = a(b + c)$$

Distributive Property

$$(y - 6)3 + (y - 6)y = (y - 6)(3 + y)$$

Note in this case that $a = y - 6$, $b = 3$, and $c = y$.

2.2 PLANE TRIGONOMETRY

There are six trigonometric functions: sine, cosine, tangent, cotangent, secant, and cosecant. The relationships of the trigonometric functions are shown in Fig. 1.20. Trigonometric functions shown for angle A (right-angled triangle) include

sin	A	=	a/c	(sine)
cos	A	=	b/c	(cosine)
tan	A	=	a/b	(tangent)
cot	A	=	b/a	(cotangent)
sec	A	=	c/b	(secant)

$\csc A = c/a$ (cosecant)

For angle B, the functions would become

(see Fig. 1.20)

$\sin B = b/c$ (sine)

$\cos B = a/c$ (cosine)

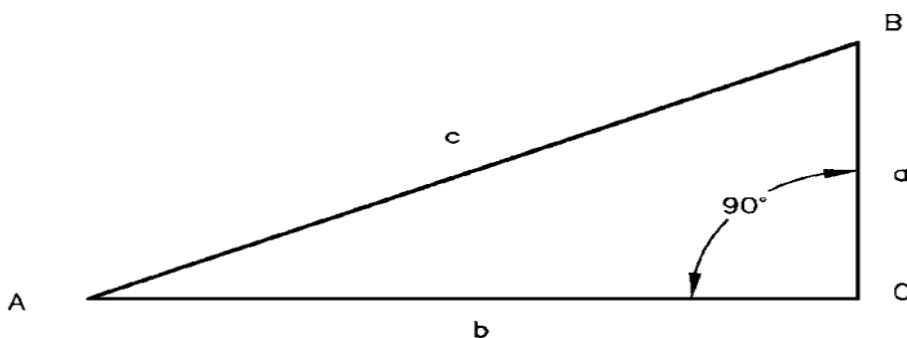


Fig 1. Right-angled triangle.

$\tan B = b/a$ (tangent)

$\cot B = a/b$ (cotangent)



$$\sec B = c/a \text{ (secant)}$$

$$\csc B = c/b \text{ (cosecant)}$$

As can be seen from the preceding, the sine of a given angle is always the side opposite the given angle divided by the hypotenuse of the triangle. The cosine is always the side adjacent to the given angle divided by the hypotenuse, and the tangent is always the side opposite the given angle divided by the side adjacent to the angle. These relationships must be remembered at all times when performing trigonometric operations.

Also:

$$\sin A = \frac{1}{\csc A}$$

$$\cos A = \frac{1}{\sec A}$$

$$\tan A = \frac{1}{\cot A}$$

This reflects the important fact that the cosecant, secant, and cotangent are the reciprocals of the sine, cosine, and tangent, respectively. This fact also must be remembered when performing trigonometric operations.

2.2.1 Signs and Limits of the Trigonometric Functions. The following coordinate chart shows the sign of the function in each quadrant and its numerical limits. As an example, the sine of any angle between 0 and 90° will always be positive, and its numerical value will range between 0 and 1, while the cosine of any angle between 90 and 180° will always be negative, and its numerical value will range between 0 and 1. Each quadrant contains 90°; thus the fourth quadrant ranges between 270 and 360°.

Quadrant II	y	Quadrant I
(1 - 0) + sin		sin + (0 - 1)
(0 - 1) - cos		cos + (1 - 0)
(∞ - 0) - tan		tan + (0 - ∞)
(0 - ∞) - cot		cot + (∞ - 0)
(∞ - 1) - sec		sec + (1 - ∞)
(1 - ∞) + csc		csc + (∞ - 1)
x'		x
Quadrant III	0	Quadrant IV
(0 - 1) - sin		sin - (1 - 0)
(1 - 0) - cos		cos + (0 - 1)
(0 - ∞) + tan		tan - (∞ - 0)
(∞ - 0) + cot		cot - (0 - ∞)
(1 - ∞) - sec		sec + (∞ - 1)
(∞ - 1) - csc		csc - (1 - ∞)
	y'	

2.2.2 Trigonometric Laws



The trigonometric laws show the relationships between the sides and angles of nonright-angle triangles or oblique triangles and allow us to calculate the unknown parts of the triangle when certain values are known. Refer to Fig. 1.21 for illustrations of the trigonometric laws that follow.

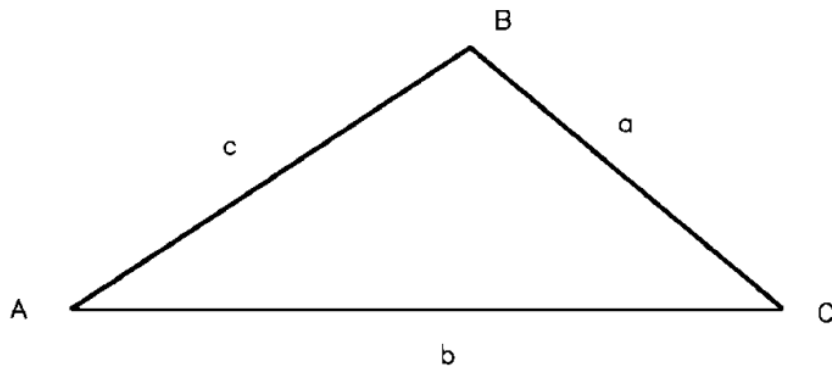


Fig 2. Oblique triangle.

• **The Law of Sines.**

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

And, $\frac{a}{b} = \frac{\sin A}{\sin B}$ $\frac{b}{c} = \frac{\sin B}{\sin C}$ $\frac{a}{c} = \frac{\sin A}{\sin C}$

Also, $a \times \sin B = b \times \sin A$; $b \times \sin C = c \times \sin B$, etc.

The Law of Cosines

$$\left. \begin{aligned} a^2 &= b^2 + c^2 - 2bc \cos A \\ b^2 &= a^2 + c^2 - 2ac \cos B \\ c^2 &= a^2 + b^2 - 2ab \cos C \end{aligned} \right\} \text{May be transposed as required}$$

• **The Law of Tangents**

1.21. $\frac{a+b}{a-b} = \frac{\tan \frac{A+B}{2}}{\tan \frac{A-B}{2}}$

With the preceding laws, the trigonometric functions for right-angled triangles, the Pythagorean theorem, and the following triangle solution chart, it will be possible to find the solution to any plane triangle problem, provided the correct parts are specified

**Self-Check-2****Written test**

Directions: choose the best answer for the following question (2 point each)

1. An algebraic expression containing three terms is called a .
(a) monomial (b) binomial (c) trinomial (d) All of these
2. Which one of the following is numeric expressions. .
A, $5 + 13$ B, $5k + 4$ C, $5h$ D, ALL
3. Identify from the following variable expressions. .
A, $5 + 13$ B, $5k + 4$ C, $2 \times 5 - 6$ D, $8 + 7 \square \square 6$
4. When you solve math problems, you can use a letter or a symbol to stand in for the number. The letter or symbol is called a .
A. Coefficient B. Variables C. Constant D. all

Note: Satisfactory rating - 4 points

Unsatisfactory - below 4 points

You can ask you teacher for the copy of the correct answers



Operation Sheet -1

Perform trigonometric functions, algebraic computations

Operation Sheet No. 1

- **Title:** - trigonometric functions, algebraic computations
- **Purpose:** - perform basic mathematical operations with emphasis in **Trigonometric Functions** and algebraic computations

Materials/Tools/ Equipment Needed:

7. Students Guide
8. Paper
9. Pen
10. Mathematical tables

Activities: The trainees shall be able to:-

1. Illustrating the basic steps in solving and in presenting solutions of mathematical problems
2. Multiplying, dividing, adding, and subtracting **Trigonometric Functions**

Performance Standard:

The student shall be able to perform basic mathematical operations with emphasis in **Trigonometric Functions**.

Information:

Illustrating the Basic Steps in Solving and in Presenting Solutions of Mathematical Problems

Basic Steps

1. Statement of the Problem
2. Comprehension
Read the text of the problem slowly and carefully and visualize the situation clearly. If possible, make a sketch.
3. Framework
Write down neatly the values which have been given and which are to be found, using symbols and dimensions.
4. Basic Equation
Relate the situation recognized to the relevant Basic Equation, Only then solve for the required value.
5. Illustration

Notes:

Make sure that the calculation proceeds step by step. Formulate the answer — at least in your head — as a complete sentence.

In addition it is a good idea to do a rough calculation before the final one. Besides this, always check the dimensions by carrying and shortening the units of measurement.



Remarks:

The teacher shall always set a deadline for finishing a task. But fast students should be given a chance to solve more calculation problems and in so doing acquire more experience.

The teacher should act as a student's consultant, which is an active role. Thus, he shall go around in the class, look at the students' solutions while they do them and give advice.

**Information Sheet-3****Self-check numerical computation**

3.1

identify the terms of the algebraic expression.

1. $10x + 5$

2. $-16t^2 + 48$

3. $-3y^2 + 2y - 8$

4. $25z^3 - 4.8z^2$

5. $4x^2 - 3y^2 - 5x + 2y$

6. $14u^2 + 25uv - 3v^2$

7. $x^2 - 2.5x - \frac{1}{x}$

8. $\frac{3}{t^2} - \frac{4}{t} + 6$

3.2

identify the coefficient of the term.

9. $5y^3$

10. $4x^6$

11. $-\frac{3}{4}t^2$

12. $-8.4x$

3.3

identify the property of algebra that is illustrated by the statement.

13. $4 - 3x = -3x + 4$

14. $(10 + x) - y = 10 + (x - y)$

15. $-5(2x) = (-5 \cdot 2)x$

16. $(x - 2)(3) = 3(x - 2)$

17. $(x + 5) \cdot \frac{1}{x + 5} = 1, \quad x \neq -5$

18. $(x^2 + 1) - (x^2 + 1) = 0$

19. $5(y^3 + 3) = 5y^3 + 5 \cdot 3$

20. $10x^3y + 0 = 10x^3y$

21. $(16t^4) \cdot 1 = 16t^4$

22. $-32(u^2 - 3u) = -32u^2 + 96u$

3.4

use the property to rewrite the expression



23. (a) Distributive Property

$$5(x + 6) = \square$$

(b) Commutative Property of Multiplication

$$5(x + 6) = \square$$

24. (a) Distributive Property

$$6x + 6 = \square$$

(b) Commutative Property of Addition

$$6x + 6 = \square$$

25. (a) Commutative Property of Multiplication

$$6(xy) = \square$$

(b) Associative Property of Multiplication

$$6(xy) = \square$$

26. (a) Additive Identity Property

$$3ab + 0 = \square$$

(b) Commutative Property of Addition

$$3ab + 0 = \square$$

27. (a) Additive Inverse Property

$$4t^2 + (-4t^2) = \square$$

(b) Commutative Property of Addition

$$4t^2 + (-4t^2) = \square$$

28. (a) Associative Property of Addition

$$(3 + 6) + (-9) = \square$$

(b) Additive Inverse Property

$$9 + (-9) = \square$$

4

Sample Problems Using Trigonometry

4.1

Samples of Solutions to Triangles

Solving Right-Angled Triangles by Trigonometry. Required: Any one side and angle A or angle B (see Fig. 1.). Solve for side a:

$$\sin A = \frac{a}{c}$$

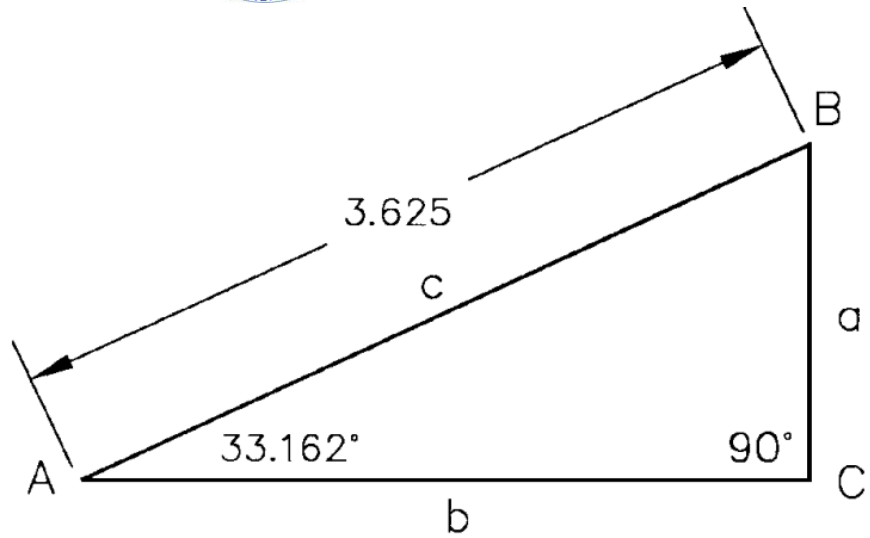


Fig 1.

Solve the triangle.

$$\sin 33.162^\circ = \frac{a}{3.625}$$

$$a = 3.625 \times \sin 33.162^\circ$$

$$= 3.625 \times 0.5470$$

$$= 1.9829$$

Solve for side b:

$$\cos A = \frac{b}{c}$$

$$\cos 33.162^\circ = \frac{b}{3.625}$$

$$b = 3.625 \times \cos 33.162^\circ$$

$$b = 3.625 \times 0.8371$$

$$b = 3.0345$$

Then

$$\text{angle } B = 180^\circ - (\text{angle } A + 90^\circ)$$

$$= 180^\circ - 123.162^\circ$$

$$= 56.838^\circ$$



We now know sides a , b , and c and angles A , B , and C . Solving Non-Right-Angled Triangles Using the Trigonometric Laws. Solve the triangle in Fig. 2. Given: Two angles and one side:

$$A = 45^\circ$$

$$B = 109^\circ$$

$$a = 3.250$$

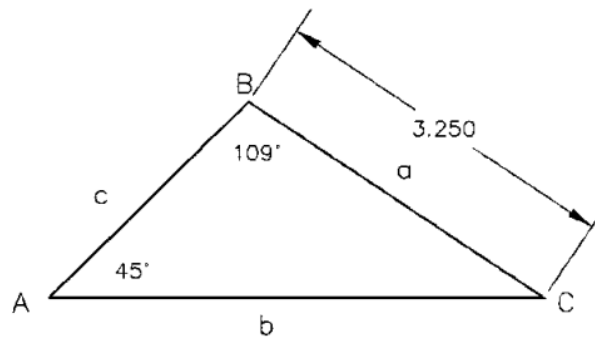


Fig 2.

• Solve the triangle.

First, find angle C :

$$\begin{aligned} \text{Angle } C &= 180^\circ - (\text{angle } A + \text{angle } B) \\ &= 180^\circ - (45^\circ + 109^\circ) \\ &= 180^\circ - 154^\circ \\ &= 26^\circ \end{aligned}$$

Second, find side b by the law of sines:

$$\begin{aligned} \frac{a}{\sin A} &= \frac{b}{\sin B} \\ \frac{3.250}{0.7071} &= \frac{b}{0.9455} \end{aligned}$$

Therefore,

$$\begin{aligned} b &= \frac{3.250 \times 0.9455}{0.7071} \\ &= 4.3457 \end{aligned}$$

Third, find side c by the law of sines:



$$\frac{a}{\sin A} = \frac{c}{\sin C}$$
$$\frac{3.250}{0.7071} = \frac{c}{0.4384}$$

Therefore,

$$c = \frac{3.250 \times 0.4384}{0.7071}$$
$$= 2.0150$$

The solution to this triangle has been calculated as $a \approx 3.250$, $b \approx 4.3457$, $c \approx 2.0150$, angle $A \approx 45^\circ$, angle $B \approx 109^\circ$, and angle $C \approx 26^\circ$. We now use the Mollweide equation to check the calculated answer by substituting the parts into the equation and checking for a balance, which signifies equality and the correct solution.

$$\frac{a-b}{c} = \frac{\sin\left(\frac{A-B}{2}\right)}{\cos\left(\frac{C}{2}\right)}$$

$$\frac{3.250 - 4.3457}{2.0150} = \frac{\sin\left(\frac{45 - 109}{2}\right)}{\cos\left(\frac{26}{2}\right)}$$

$$\frac{-1.0957}{2.0150} = \frac{\sin(-32^\circ)}{\cos 13^\circ} \quad (\text{Find } \sin -32^\circ \text{ and } \cos 13^\circ \text{ on a calculator.})$$

$$\frac{-1.0957}{2.0150} = \frac{-0.5299}{0.9744} \quad (\text{Divide both sides.})$$

$$-0.5438 = -0.5438 \quad (\text{Cross-multiplying will also show an equality.})$$

This equality shows that the calculated solution to the triangle shown in Fig. 2. is correct.

Solve the triangle in Fig. 3. Given: Two sides and one angle:

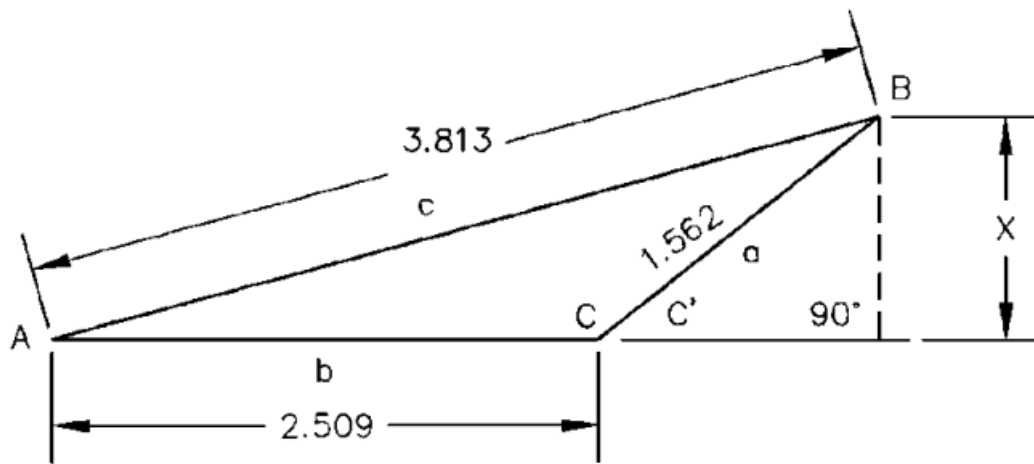


Fig 3.

Solve the triangle.

$$\text{Angle } A = 16^\circ$$

$$a = 1.562$$

$$b = 2.509$$

First, find angle B from the law of sines

$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

$$\frac{1.562}{\sin 16} = \frac{2.509}{\sin B}$$

$$\frac{1.562}{0.2756} = \frac{2.509}{\sin B}$$

$$1.562 \cdot \sin B = 0.6915 \quad (\text{by cross-multiplication})$$

$$\sin B = \frac{0.6915}{1.562}$$

$$\sin B = 0.4427$$

$$\arccos 0.4427 = 26.276^\circ = \text{angle } B$$

Second, find angle C:



$$\begin{aligned}\text{Angle } C &= 180^\circ - (\text{angle } A + \text{angle } B) \\ &= 180^\circ - 42.276^\circ \\ &= 137.724^\circ\end{aligned}$$

$$\begin{aligned}\text{Angle } C &= 180^\circ - (\text{angle } A + \text{angle } B) \\ &= 180^\circ - 42.276^\circ \\ &= 137.724^\circ\end{aligned}$$

Third, find side c from the law of sines:

$$\begin{aligned}\frac{a}{\sin A} &= \frac{c}{\sin C} \\ \frac{1.562}{0.2756} &= \frac{c}{0.6727} \\ 0.2756c &= 1.0508 \\ c &= 3.813\end{aligned}$$

We may now find the altitude or height x of this triangle (see Fig. 3). Refer to Fig. 2. and text for the following equation for x .

$$\begin{aligned}x &= b \frac{\sin A \sin C}{\sin (C' - A)} \quad (\text{where angle } C' = 180^\circ - 137.724^\circ = 42.276^\circ \text{ in Fig. 1.29}) \\ &= 2.509 \times \frac{0.2756 \times 0.6727}{\sin (42.276 - 16)} \\ &= 2.509 \times \frac{0.1854}{0.4427} \\ &= 2.509 \times 0.4188 \\ &= 1.051\end{aligned}$$

This height x also can be found from the sine function of angle C' , when side a is



$$\sin C' = \frac{x}{1.562}$$

$$x = 1.562 \sin C' = 1.562 \times 0.6727 = 1.051$$

known, as shown here

3.4 Systems of measurement and conversion

3.4.1 Units of measurements

- This class addresses common units of measurement used in manufacturing and explains how to convert from one unit of measurement to another
- Below are all the competencies and job programs that contain the class units of measurement. Competencies are our latest job specific curricula that help to practical, hands on task....

3.4.2 Definition of English System

- A standard system of measurements based on the inch, pound, and Fahrenheit degrees.
- English measurements are primarily used in the United States and England.

3.4.3 Definition of Metric System

- A standard system of measurement based on the meter, kilogram. And celsius degrees. The metric system is internationally recognized.

Identify the English and Metric

	Metric System	English System
Length	meter	inch, foot, mile
Mass	gram	ounce, pound, ton
Volume	liter	pint, quart, gallon
Power	watt	horsepower
Torque	newton-meter	pound-foot
Temperature	degrees Celsius	degree-fahrenheit



3.3.4 Convert Metric to English

Conversion Factors

Metric to English

To Obtain	Multiply	By
Inches	Centimeters	0.3937007874
Feet	Meters	3.280839895
Yards	Meters	1.093613298
Miles	Kilometers	0.621 3711922
Square Inches	Square Centimeters	0.1550003100
Square Feet	Square Meters	10.76391042
Square Yards	Square Meters	1.195990046
Cubic Inches	Milliliters	0.061 02374409
Cubic Feet	Cubic Meters	35.31 466672
Cubic Yards	Cubic Meters	1.307 950619
Fluid Ounces	Milliliters	0.03381402270
Teaspoons	Milliliters	0.202884136
Tablespoons	Milliliters	0.067 6280454
Cups	Liters	4.22675284
Quarts	Liters	1.05668821
Gallons	Liters	0.264 1720524
Ounces	Grams	0.035 27396195
Pounds	Kilograms	2.204 622622
Miles per Hour	Kilometers per Hour	1.609 344001

English to Metric

To Obtain	Multiply	By
Centimeters	Inches	2.54
Meters	Feet	0.3048
Meters	Yards	0.9144
Kilometers	Miles	1.609344
Square Centimeters	Square Inches	6.4516
Square Meters	Square Feet	0.09290304
Square Meters	Square Yards	0.83612736
Milliliters	Cubic Inches	16.387064
Cubic Meters	Cubic Feet	0.02831684659
Cubic Meters	Cubic Yards	0.764554858
Milliliters	Fluid Ounces	29.57352956
Milliliters	Teaspoons	4.92892159
Milliliters	Tablespoons	14.7867648
Liters	Cups	0.236588236
Liters	Quarts	0.946352946
Liters	Gallons	3.785411784
Grams	Ounces	28.34952313
Kilograms	Pounds	0.45359237
Kilometers per Hour	Miles per Hour	0.621 371192

Note: Boldface numbers are exact, others are given to ten significant figures.



A $? \text{ m} = 100 \text{ yd}$

Known

$3 \text{ ft} = 1 \text{ yd}$

B $12 \text{ in} = 1 \text{ ft}$

$2.54 \text{ cm} = 1 \text{ in}$

$100 \text{ cm} = 1 \text{ m}$

C $? \text{ m} = 100 \text{ yd} \times \frac{3 \text{ ft}}{1 \text{ yd}} \times \frac{12 \text{ in}}{1 \text{ ft}} \times \frac{2.54 \text{ cm}}{1 \text{ in}} \times \frac{1 \text{ m}}{100 \text{ cm}}$

D $? \text{ m} = 100 \cancel{\text{yd}} \times \frac{3 \cancel{\text{ft}}}{1 \cancel{\text{yd}}} \times \frac{12 \cancel{\text{in}}}{1 \cancel{\text{ft}}} \times \frac{2.54 \cancel{\text{cm}}}{1 \cancel{\text{in}}} \times \frac{1 \text{ m}}{100 \cancel{\text{cm}}}$

E $? \text{ m} = \frac{100 \times 3 \times 12 \times 2.54}{100} \text{ m}$

F $? \text{ m} = 91.44 \text{ m}$

Illustrating the Basic Steps in Solving and in Converting Length Measurements

Measurement of length

Length

Length is the measurement of something from one end to the other end.

- The SI unit of length is meter (m) (base unit).
- other units include centimeters (cm), millimeters (mm) and kilometers (km)
- One meter is the distance travelled by light in a vacuum in $1/299792458$ of a second.

Metric System

- used for scientific work in the United States
- Measurements are based on the meter
 - 1 Meter = 100 centimeters (cm)
 - 1 Meter = 1,000 millimeters (mm)
 - 1000 Meters = a Kilometer (km)
- Units are in multiples of 10
- The unit is the meter. Subdivisions follow the decimal system.

$$1 \text{ m} = \underline{10} \text{ dm} = 100 \text{ cm} = 1000 \text{ mm}$$

$$1 \text{ dm} = \underline{10} \text{ cm} = 100 \text{ mm}$$

$$1 \text{ cm} = \underline{10} \text{ mm}$$

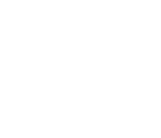
Note: The conversion factor from one unit to another is ten — there is a “jump of ten” from one place unit to the next Sizes comparison **Inch System**

- English – standard measurement in the United States, now called U.S. Customary System
 - Uses, inch, foot, yard, rod and mile as units
 - 12 inches in a foot
 - 3 feet in a yard
 - $16 \frac{1}{2}$ feet in a rod
 - 5,280 foot in a mile
- Traditional unit for woodworking and metalworking



- Some fine rules or scales have 32 marks per inch.
- Most rules have 16 marks per inch with each mark equaling 1/16 of an inch.

The length unit “inch”, with its standard symbol “in”, is divided into 16 parts



**Self-Check-3****Written test**

Directions: choose the best answer for the following question (2 point each)

1. $5x + x^2 = x^2 + 5x$

- A. commutative property of addition
- B. commutative property of multiplication
- C. .associative property of addition
- D. associative property of multiplication

2. $(a+b)+c = a+(b+c)$

- A. commutative property of addition
- B. commutative property of multiplication
- C. associative property of addition
- D. associative property of multiplication

3. Which one show distributive properties.

- A. $(ab)c = a(bc)$
- B. $(a+b)+c = a+(b+c)$
- C. $a(b+c) = ab+ac$
- D. $a+b = b+a$

Note: Satisfactory rating - 3 points

Unsatisfactory - below 3 points

You can ask you teacher for the copy of the correct answers



Operation Sheet -2

numerical computation

Operation Sheet No. 2

Title: - Applications of Basic numerical computation

Purpose: - perform basic mathematical operations with emphasis in fractions.

Materials/Tools/ Equipment Needed:

4. Students Guide
5. Paper
6. Pen
7. Mathematical tables

Activities:

1. Illustrating the basic steps in solving and in presenting solutions of mathematical problems
2. Multiplying, dividing, adding, and subtracting fractions

Performance Standard:

The student shall be able to perform basic mathematical operations with emphasis in fractions.

Information:

Illustrating the Basic Steps in Solving and in Presenting Solutions of Mathematical Problems

Basic Steps

4.1.1 Statement of the Problem

4.1.2 Comprehension

Read the text of the problem slowly and carefully and visualize the situation clearly. If possible, make a sketch.

4.1.3 Framework

Write down neatly the values which have been given and which are to be found, using symbols and dimensions.

4.1.4 Basic Equation

Relate the situation recognized to the relevant Basic Equation, Only then solve for the required value.

4.1.5 Illustration

4.1.6 Solution of Problems

Notes:

Make sure that the calculation proceeds step by step. Formulate the answer — at least in your head — as a complete sentence.

In addition it is a good idea to do a rough calculation before the final one. Besides this, always check the dimensions by carrying and shortening the units of measurement.

Remarks:

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The teacher shall always set a deadline for finishing a task. But fast students should be given a chance to solve more calculation problems and in so doing acquire more experience.

The teacher should act as a student's consultant, which is an active role. Thus, he shall go around in the class, look at the students' solutions while they do them and give advice.



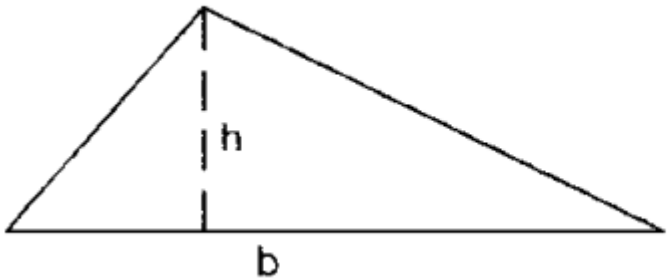
Information Sheet-4	Construct where appropriate, formulae to enable problems to be solved
----------------------------	------------------------------------------------------------------------------

MENSURATION

Mensuration is the mathematical name for calculating the areas, volumes, length of sides, and other geometric parts of standard geometric shapes such as circles, spheres, polygons, prisms, cylinders, cones, etc., through the use of mathematical equations or formulas. Included here are the most frequently used and important mensuration formulas for the common geometric figures, both plane and solid. (See Figs. 4.1 through 4.35.)

Symbols	area
A	
a, b, etc.	sides
A, B, C	angles
h	height perpendicular to base b
L	length of side or edge
r	radius
n	number of sides
C	circumference
V	volume
S	surface area

Table -1



$$A = \frac{1}{2}bh$$

Fig 4.1. Oblique triangle.

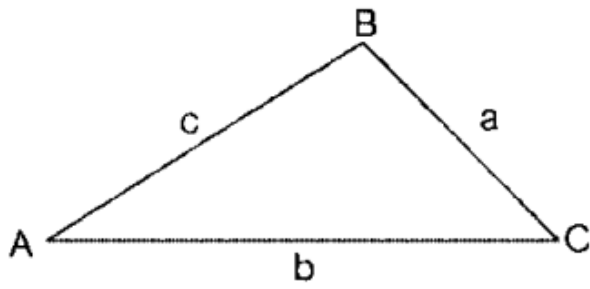


Fig 4.2. Oblique triangle.

$$A = \frac{1}{2}ab \sin C$$

$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

where $s = \frac{1}{2}(a + b + c)$

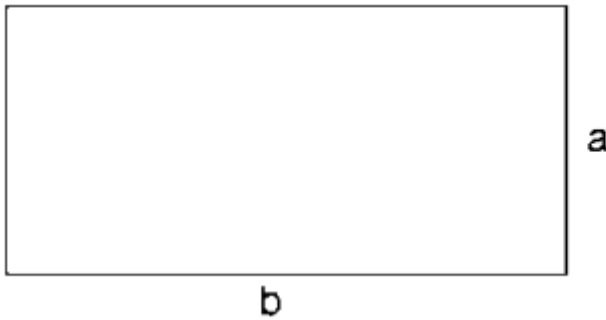


Fig 4.3. Rectangle

$$A = ab$$

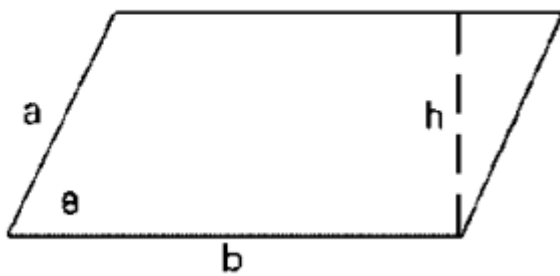


Fig 4.4. Parallelogram.

$$A = bh$$

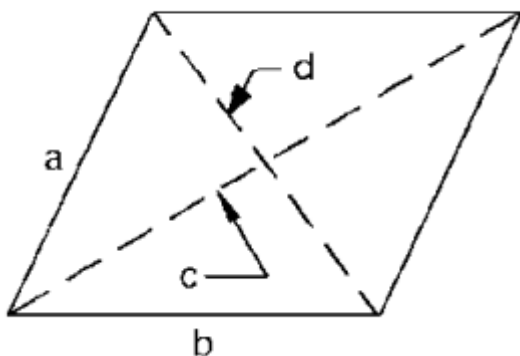
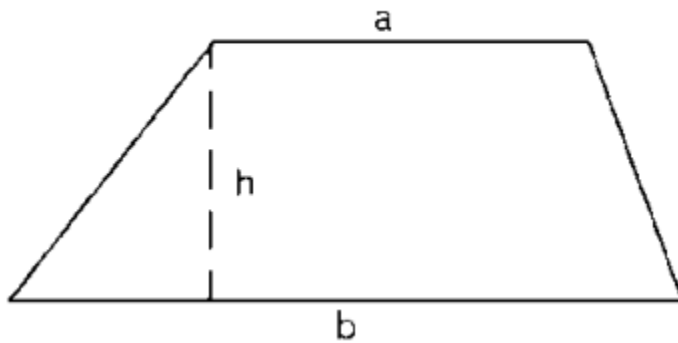


Fig 4.5. Rhombus

$$A = \frac{1}{2} cd$$



$$A = \frac{1}{2} (a + b)h$$

Fig 4.6. Trapezoid

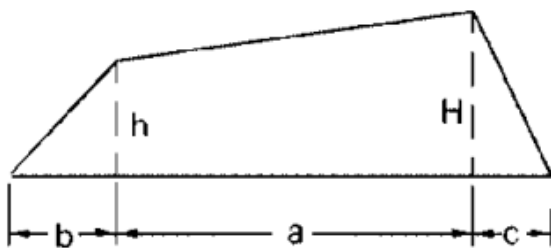
MENSURATION OF PLANE AND SOLID FIGURES

Surfaces and Volumes of Polyhedra:

(Where L = leg or edge)

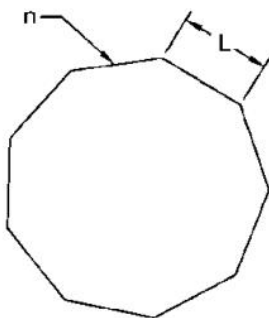
Polyhedron	Surface	Volume
Tetrahedron	$1.73205L^2$	$0.11785L^3$
Hexahedron	$6L^2$	$1L^3$
Octahedron	$3.46410L^2$	$0.47140L^3$

Table -2 Polyhedral.



$$A = \frac{(H + h)a + bh + cH}{2}$$

Fig 4.7. Trapezium



In a polygon of n sides of L , the radius of the inscribed circle is:

$$r = \frac{L}{2} \cot \frac{180}{n};$$

The radius of the circumscribed circle is:

$$r_1 = \frac{L}{2} \csc \frac{180}{n}$$

Fig 4.8. Regular polygon.

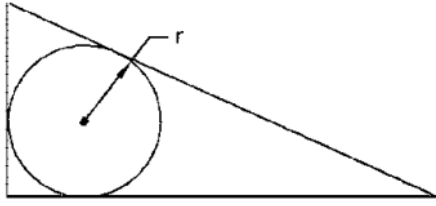


Fig 4.9. Inscribed circle.

The radius of a circle inscribed in any triangle whose sides are a, b, c is:

$$r = \frac{\sqrt{s(s-a)(s-b)(s-c)}}{s}$$

where $s = \frac{1}{2}(a + b + c)$

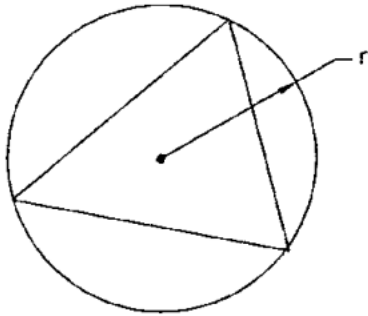


Fig 4.10. Circumscribed circle.

In any triangle, the radius of the circumscribed circle is:

$$r = \frac{abc}{4\sqrt{s(s-a)(s-b)(s-c)}}$$

where $s = \frac{1}{2}(a + b + c)$

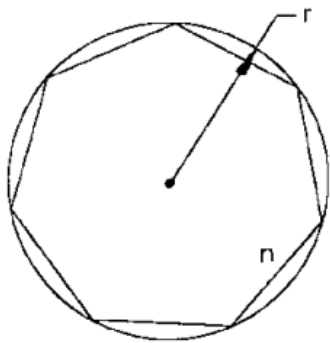


Fig. 4.11. Inscribed polygon.

Area of an inscribed polygon is:

$$A = \frac{1}{2} nr^2 \sin \frac{2\pi}{n}$$

where r = radius of circumscribed circle
 n = number of sides

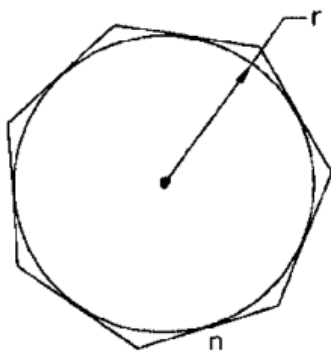
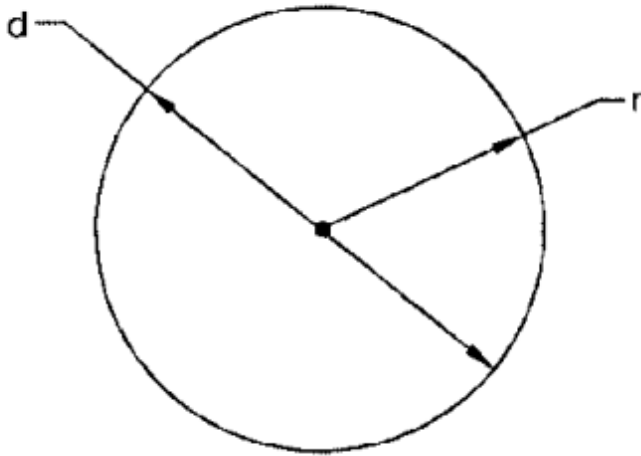


Fig 4.12. Polygon Circumscribed

Area of a circumscribed polygon is:

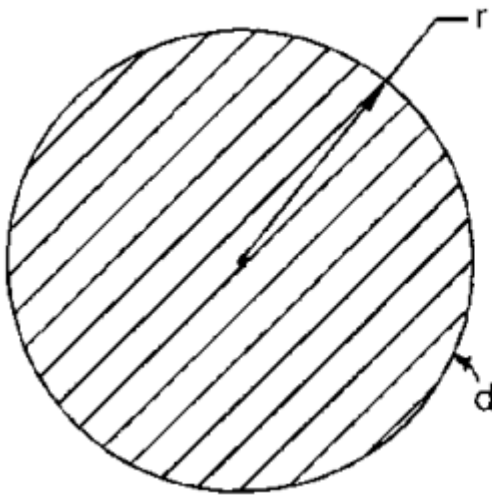
$$A = nr^2 \tan \frac{\pi}{n}$$

where r = radius of inscribed circle
 n = number of sides



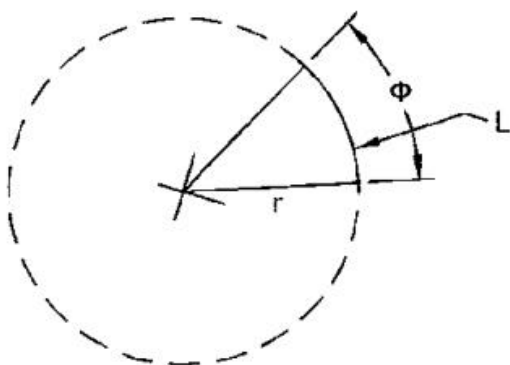
$$C = 2\pi r = \pi d$$

Fig 4.13.Circle—circumference.



$$A = \pi r^2 = \frac{1}{4}\pi d^2$$

Fig 4.14. Circle—area.



Length of arc L :

$$L = \frac{\pi r \phi}{180} \quad (\text{when } \phi \text{ is in degrees})$$

$$L = \pi r \phi \quad (\text{when } \phi \text{ is in radians})$$

Fig 4.15.Length of arc.

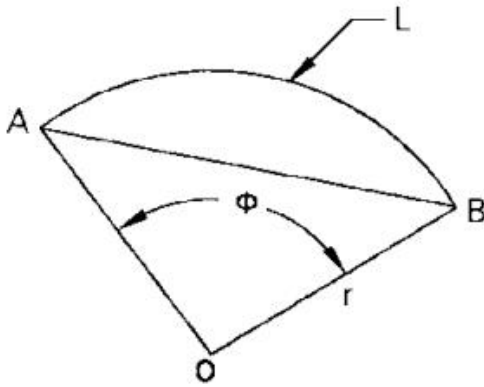


Fig 4.16. Chord and sector.

Length of chord:

$$AB = 2r \sin \frac{1}{2}\phi$$

Area of the sector:

$$A = \frac{\pi r^2 \phi}{360} = \frac{rL}{2}$$

where L = length of the arc

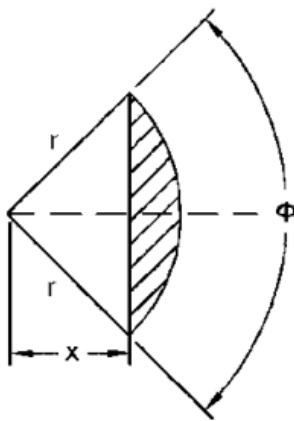


Fig 4.17. Segment of a circle.

Area of segment of a circle:

$$A = \frac{\pi r^2 \phi}{360} - \frac{r^2 \sin \phi}{2}$$

where: $\phi = 180^\circ - 2 \arcsin \left(\frac{x}{r} \right)$

If ϕ is in radians:

$$A = \frac{1}{2} r^2 (\phi - \sin \phi)$$

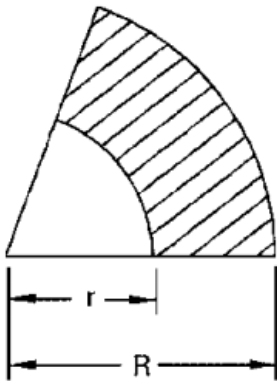


Fig 4.18. Ring.

Area of the ring between circles.

Circles need not be concentric:

$$A = \pi(R + r)(R - r)$$

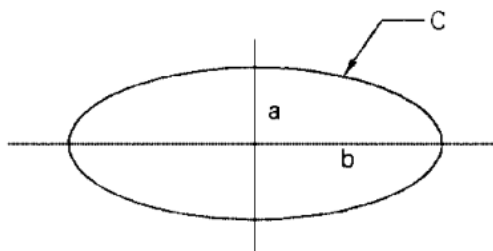


Fig 4.19. Ellipse

Circumference and area of an ellipse (approximate):

$$C = 2\pi \sqrt{\frac{a^2 + b^2}{2}}$$

Area:

$$A = \pi ab$$

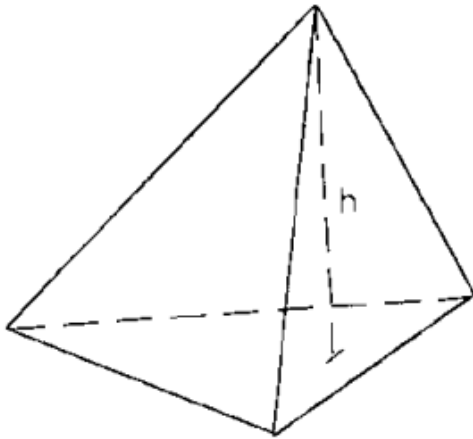


Fig 4.20.Pyramid.

Volume of a pyramid:

$$V = \frac{1}{3} \times \text{area of base} \times h$$

where h = altitude

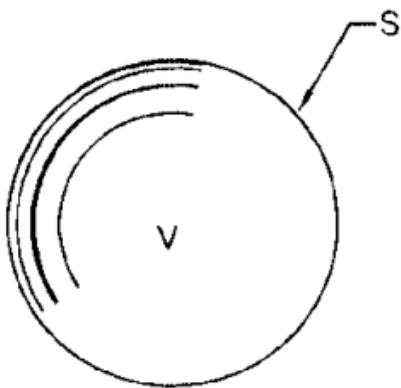


Fig 4.21.Sphere.

Surface and volume of a sphere:

$$S = 4\pi r^2 = \pi d^2$$

$$V = \frac{4}{3} \pi r^3 = \frac{1}{6} \pi d^3$$

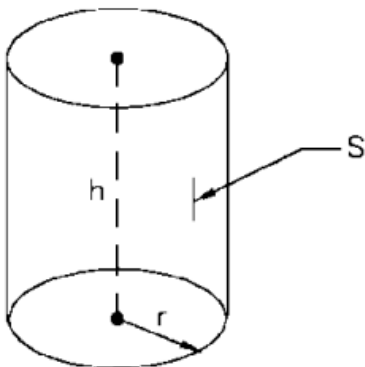


Fig 4.22.Cylinder

Surface and volume of a cylinder:

$$S = 2\pi rh$$

$$V = \pi r^2 h$$

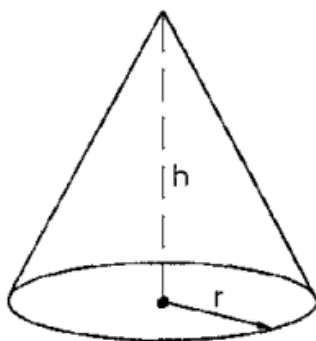


Fig 4.23.Cone.

Surface and volume of a cone:

$$S = \pi r \sqrt{r^2 + h^2}$$

$$V = \frac{\pi}{3} r^2 h$$

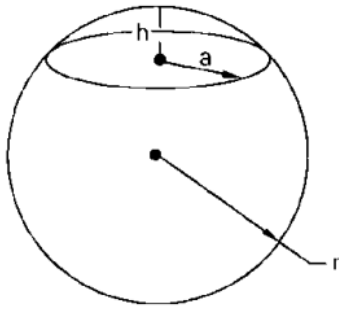


Fig 4.24.Spherical segment.

Area and volume of a curved surface of a spherical segment:

$$A = 2\pi rh \quad V = \left(\frac{\pi h^2}{3}\right)(3r - h)$$

When a is radius of base of segment:

$$V = \frac{\pi h}{4} (h^2 + 3a^2)$$

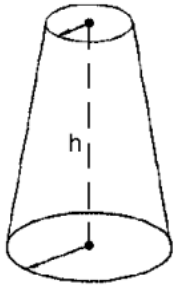


Fig 4.25.Frustum of a cone.

Surface area and volume of a frustum of a cone:

$$S = \pi (r_1 + r_2) \sqrt{h^2 + (r_1 - r_2)^2}$$

$$V = \frac{h}{3} (r_1^2 + r_1 r_2 + r_2^2) \pi$$

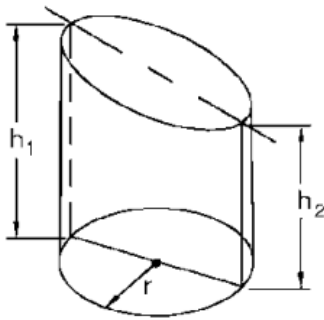


Fig 4.26.Truncated cylinder.

Area and volume of a truncated cylinder:

$$A = \pi r (h_1 + h_2)$$

$$V = \frac{\pi}{2} r^2 (h_1 + h_2)$$

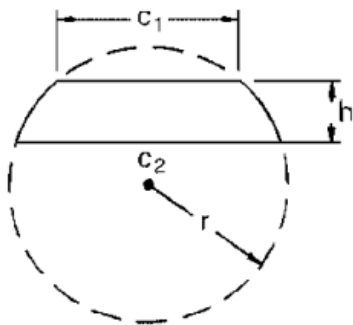
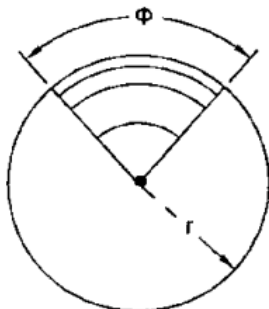


Fig 4.27.Spherical zone.

Area and volume of a spherical zone:

$$A = 2\pi rh$$

$$V = \frac{\pi}{6} h \left(\frac{3c_1^2}{4} + \frac{3c_2^2}{4} + h^2 \right)$$

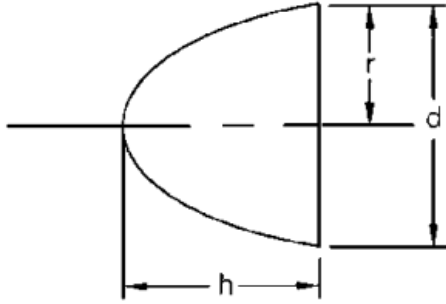


Area and volume of a spherical wedge:

$$A = \frac{\phi}{360} 4\pi r^2$$

$$V = \frac{\phi}{360} \cdot \frac{4\pi r^3}{3}$$

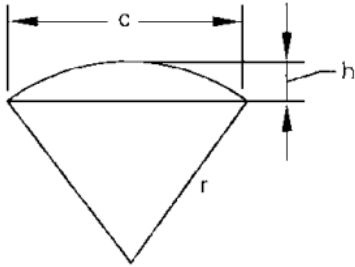
Fig 4.28.Spherical wedge.



Volume of a paraboloid:

$$V = \frac{\pi r^2 h}{2}$$

Fig 4.29.Parabolic.



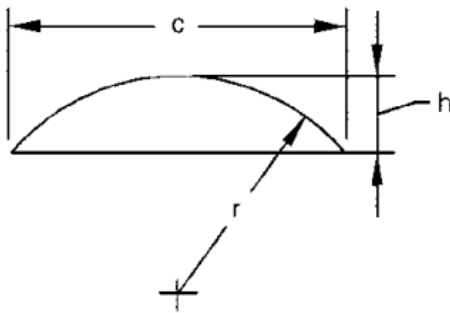
Area and volume of a spherical sector (yields total area):

$$A = \pi r \left(2h + \frac{c}{2} \right)$$

$$V = \frac{2\pi r^2 h}{3} \quad c = 2 \sqrt{h(2r - h)}$$

4.19.

Fig 4.30. Spherical sector.



Area and volume of a spherical segment:

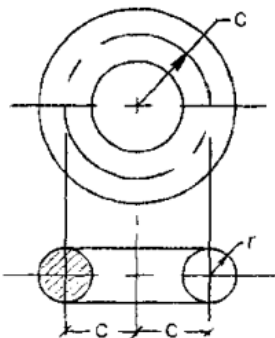
$$A = 2\pi r h$$

$$\text{Spherical surface} = \pi \left(\frac{c^2}{4} + h^2 \right)$$

$$c = 2 \sqrt{h(2r - h)} \quad r = \frac{c^2 + 4h^2}{8h}$$

$$V = \pi h^2 \left(r - \frac{h}{3} \right)$$

Fig 4.31.Spherical segment.



Area and volume of a torus:

$$A = 4\pi^2 c r \quad (\text{total surface})$$

$$V = 2\pi^2 c r^2 \quad (\text{total volume})$$

Fig 4.32.Torus.

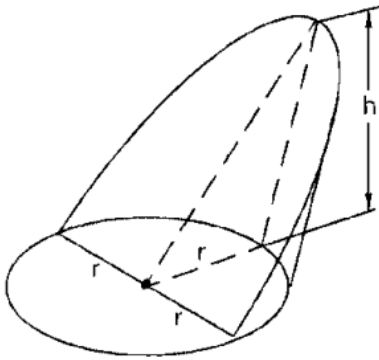


Fig 4.33. Portion of a cylinder.

Area and volume of a portion of a cylinder (base edge = diameter):

$$A = 2rh \quad V = \frac{2}{3} r^2 h$$

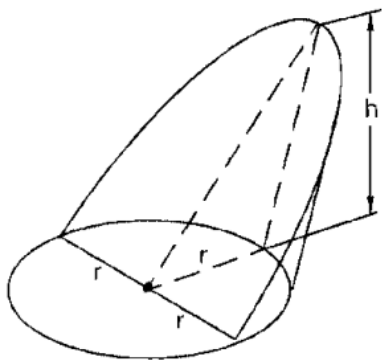


Fig 4.34. Special case of a cylinder.

Area and volume of a portion of a cylinder (special cases):

$$A = \frac{h(ad \pm c \times \text{perimeter of base})}{r \pm c}$$

$$V = \frac{h\left(\frac{2}{3} a^3 \pm cA\right)}{r \pm c}$$

where d = diameter of base circle

Note. Use $\square c$ when base area is larger than half the base circle; use $\square c$ when base area is smaller than half the base circle.

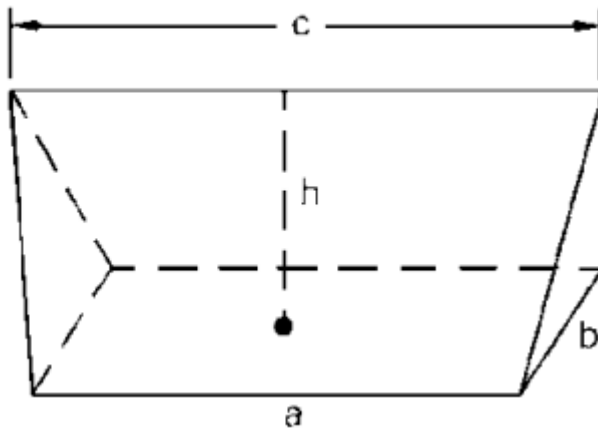


Fig 4.35. Wedge.

Volume of a wedge

$$V = \frac{(2b + c)ah}{6}$$



Operation Sheet 3

appropriate, formulae

Operation Sheet No. 3

Title: - Applications of Basic appropriate, formulae

Purpose: - perform basic mathematical operations with emphasis in conversions.

Materials/Tools/ Equipment Needed:

11. Students Guide
12. Paper
13. Pen
14. Mathematical tables

Activities:

- 5 Solve problems on the applications the pythagoras' theorem;
- 6 Solve problems on the applications of shapes and circumference;
- 7 Solve problems on the applications of time and angular units;
- 8 Solve problems on the applications of trigonometric functions;
- 9 Solve problems on the applications of areas; and
- 10 Solve problems on the application of volumes.

Performance Standard:

The trainees should be able to solve problems concerning the applications of trigonometry, areas, and volumes.

Information:

Illustrating the Basic Steps in Solving and in Presenting Solutions of Mathematical Problems

Basic Steps

11. Statement of the Problem
12. Comprehension

Read the text of the problem slowly and carefully and visualize the situation clearly. If possible, make a sketch.

10.1.1 Framework

Write down neatly the values which have been given and which are to be found, using symbols and dimensions.

10.1.2 Basic Equation

Relate the situation recognized to the relevant Basic Equation, Only then solve for the required value.

10.1.3 Illustration

10.1.4 Solve correctly the questions given the evaluation section of the lesson.

10.1.5 Solution of Problems.

Notes:

Make sure that the calculation proceeds step by step. Formulate the answer — at least in your head — as a complete sentence.

In addition it is a good idea to do a rough calculation before the final one. Besides this, always check the dimensions by carrying and shortening the units of measurement.



Remarks:

The emphasis in the lesson is the capability of the students to solve application problems. It is therefore recommended that due attention should be given to the exercises with the close supervision of the instructor. In mathematics, there is no substitute for practice.

The teacher shall always set a deadline for finishing a task. But fast students should be given a chance to solve more calculation problems and in so doing acquire more experience.

The teacher should act as a student's consultant, which is an active role. Thus, he shall go around in the class, look at the students' solutions while they do them and give advice.

Summary:

Read – comprehend - sketch

Relate the situation to the basic equation

Information Sheet-5	Reading instruments
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5.1 READING A VERNIER CALIPER To read a vernier caliper, you must understand both the steel rule and vernier scales. The vernier scale is located on the sliding jaw of the caliper. The steel rule scale is located on the caliper's long arm.

Understanding the Scales Figure 1, below, shows a portion of a typical steel rule scale. The steel rule scale may be graduated by English or metric measure. English measure uses inches. Metric measure uses centimeters and millimeters

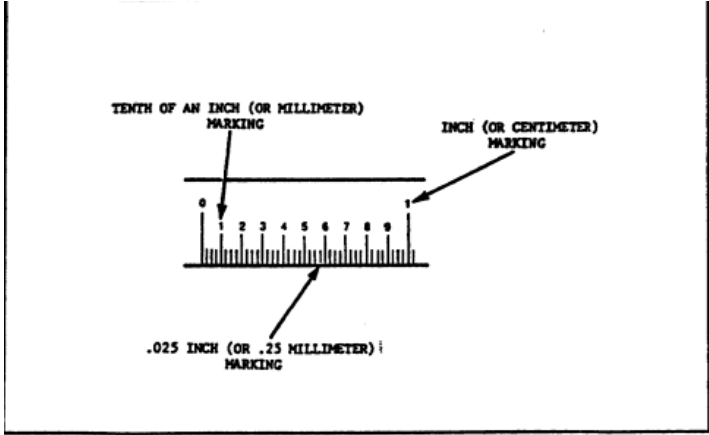


Fig. 1.

THE STEEL RULE SCALE

- Steel Rule Scale.** Usually, the steel rule scale on a vernier caliper is in English measure. The longest lines show the whole inch markings. Each inch is divided into tenth inch parts which are numbered. Each tenth inch portion is divided into four parts. Each of these parts equals 0.025 of an inch. Thus, the full inch is divided into 40 equal parts. The smallest graduation is 0.025 (1/40) of an inch. Sometimes the back side of a vernier caliper has a metric scale. When this is the case, the steel rule is divided into centimeters (cm). Each full centimeter is divided into ten parts. Each of these parts is equal to one millimeter (mm). There are ten millimeters in one centimeter. The space between each millimeter mark is divided into quarters, each of which is equal to 0.25mm.

The difference between the width of one of the 25 spaces on the vernier scale and one of the 24 spaces on the rule equals 1/1000 (0.001) of an inch. Relationship of the Scales. Imagine that the tool is set so that the 0 line on the vernier scale lines up exactly with the 0 line on the rule. The 0 lines are said to coincide. The line to the right of the 0 on the vernier scale will differ from the line to the right of 0 on the rule by 1/1000 (0.001) of an inch. The second line will differ by 2/1000 (0.002) of an inch. The difference will keep increasing by 1/1000 of an inch for each division until



vernier line 25 coincides with rule line 24. Using this relation, the vernier scale can be used to measure fractional parts of the $1/40$ (0.025) inch spaces on the rule.

- **Reading a Standard Vernier Caliper:** Example 1 Let's look at two examples of how the relationship of the scales works in an actual measurement. Figure 2, on the next page, shows one example of a scale setting on a vernier caliper. To read this measurement, use the following steps:

Step 1.

Read the number of whole inches on the top (rule) scale to the left of the vernier zero. Record this number. In this example, you would record 2.000 inches.

Step 2.

Next, read the number of tenths to the left of the vernier zero. In this case, that number is three tenths of an inch. Record it as 0.300 inch. You now know how many whole and how many tenths inches the measurement is. In this example, you have 2.000 inches plus 0.300 inch, equaling 2.300 inches.

Step 3.

Remember, each tenth inch is divided into four parts. Each of these parts equals 0.025 inch. Read how many of these 0.025 inch parts are between the tenths mark you recorded and the zero on the vernier scale. In the example shown in figure 2, there are two of these 0.025 inch parts. Therefore, multiply 2 times 0.025 inch. This equals 0.05 inch. Add this amount to the 2.300 inches you already have. The total now equals 2.350 inches

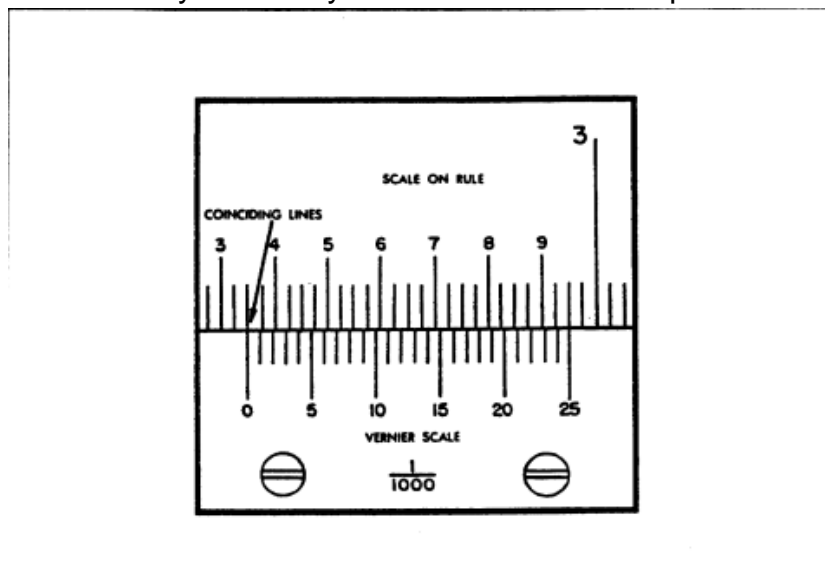


Figure 2
READING A VERNIER CALIPER - EXAMPLE 1

Step 4.

For the last part of the reading, find the line on the vernier scale which exactly coincides with a line on the rule. In the example shown in figure 6, the coinciding vernier line is zero. Therefore, there is no fractional part of a 0.025 inch space to calculate. The exact reading for this sample is 2.350 inches. Reading a Standard Vernier Caliper: Example 2 Now let's look at another sample reading. Figure 7, on the next page, shows a scale



setting that is almost the same as the one we saw in figure 2. In fact, the first readings will be identical, as shown below:

Step 1. The number of whole inches to the left of the vernier scale zero is 2.000 inches.
Step 2. The number of tenths inches to the left of the vernier zero is 3, equaling 0.300 inch.

Step 3. Two whole 0.025 spaces lie between the 3 tenths mark and the vernier zero. Thus, 2 times 0.25 inch equals 0.050 inch. The total reading so far is 2.000 inches plus 0.300 inch, plus 0.050 inch. This equals 2.350 inches. In this sample, however, the vernier zero does not exactly coincide with a line on the rule scale. The total reading will be 2.350 inches plus a fraction of a space on the rule.

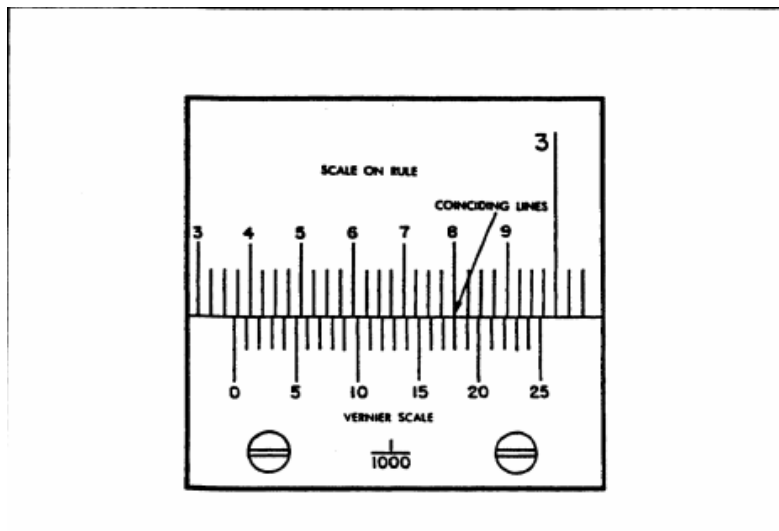


Fig .3

READING A VERNIER CALIPER - EXAMPLE 2

Step 4. To interpret the rest of the reading, find the line on the vernier scale that exactly coincides with a line on the rule scale. In the sample shown in figure 3, the vernier line 18 exactly coincides with a line on the rule scale. This tells you that 18/25 of a whole space must be added to the measurement. Remember that 1/25 of a space equals 0.001 inch. Therefore, 18/25 of a space equals 0.018 inch. Calculate the total reading by adding 2.350 inches and 0.018 inch. The sum is 2.368 inches this is the exact measurement reading shown in figure 3. Reading a Metric Vernier Caliper The standard vernier caliper you just learned to read uses the English measurement scales (inches). Some calipers have a metric scale on the back side. Therefore, you must also know how to interpret readings from a metric vernier caliper. The methods used to interpret a reading from a metric scale on a vernier caliper are nearly the same as those you just learned. The only difference is that you are working in centimeters and millimeters instead of inches. Assume that the scales shown in figure 7 (on the previous page) are metric. You would interpret the reading as follows:

Step 1. The number of whole centimeters (cm) to the left of the vernier zero equals 2.000cm. Each centimeter equals 10 millimeters. Therefore, the reading in millimeters (mm) is 20.000mm.



Step 2. The number of millimeters (mm) to the left of the vernier zero equals 3mm. The total reading so far is 20.000mm plus 3mm, or 23.000mm. Step 3. Read the number of 0.25mm spaces between the 3 millimeter mark and the vernier zero. There are two of these spaces, equaling 2 times 0.25mm, or 0.50mm. Added to the previous amount, the total reading so far is 23.50mm.

Step 4. Read the highest line on the vernier scale which lines up exactly with the line on the rule scale. This is line 18. Multiply 18 times 0.01mm. This equals 0.18mm. Add 0.18mm to 23.500mm to get the exact total reading of 23.68mm.

Reading Inside Measurements with a Vernier Caliper The jaws of a vernier caliper are shaped so that you can use the tool to make inside measurements. On most vernier calipers, the back side reads "INSIDE." When this is the case, the scale positions on that side of the caliper are set to adjust for the thickness of the jaw tips. Read the scales on the side of the caliper marked "INSIDE" just as you would for an outside measurement. Sometimes the scale isn't marked. If the scale isn't marked, measure an inside length using the caliper side normally used for outside. Read the scales as you would for an outside reading. Then add the measuring point allowance (the thickness of the tips) to your reading. This point allowance can be found in the manufacturer's instructions. Or you can use table 1, below:

5.2 READING A MICROMETER Interpreting a reading of a micrometer measurement is much like reading a vernier caliper. To read a micrometer, you compare the positions of two scales. The scales on an outside micrometer and a depth micrometer work the same. If you learn to read one, you will know how to read the other. The only calculation difference will be the way you count the size (range) of the outside micrometer used or the length of extension rod used on a depth micrometer. First, let's learn how the scales work. Understanding Standard Micrometer Scales Again, you must understand how the scales work before you can interpret a reading. The scales on standard and metric micrometers both work on the same idea. However, the meaning of the graduation lines changes. To understand how the scales work, we will use the standard micrometer as an example. On a standard micrometer, one scale is on the barrel. The other scale is on the thimble. The scale on the barrel is fixed. It does not move. The scale on the thimble moves along the barrel scale (figure 4, below).

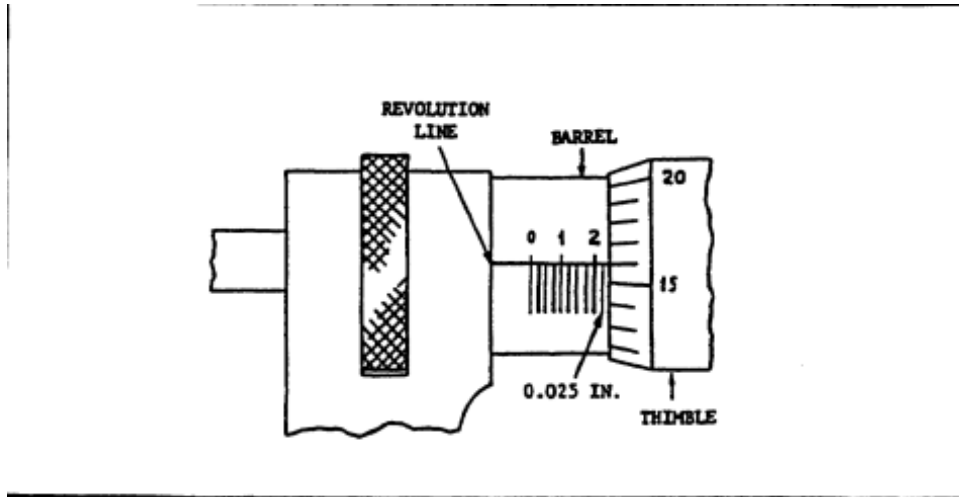


figure 4
MICROMETER SCALES

The lines on the barrel scale stand for full turns of the thimble, and therefore of the micrometer screw. The thimble edge moves one line along the barrel scale for every full turn (revolution) of the thimble.

On a standard micrometer, the measurement is in inches. Each line on the barrel scale equals $1/40$ (0.025) of an inch. For each revolution, the micrometer screw moves forward or back $1/40$ (0.025 of an inch). On an outside micrometer, this means that the screw moves the spindle away from or toward the anvil exactly $1/40$ (0.025) of an inch for every full turn. The full length of the barrel scale represents one inch of micrometer screw movement forward or back. The long horizontal line on the barrel is called the revolution line. It is divided into the 40 parts which make up the barrel scale. Each line on the barrel scale equals $1/40$ (0.025) of an inch of screw movement. Every fourth line is numbered 1, 2, 3, and so forth. Each numbered line equals $1/10$ (0.10) of an inch of screw movement. Thimble Scale. The thimble scale moves along the barrel scale. The beveled edge of the thimble is divided into 25 equal parts. As the thimble is turned, each line of the thimble scale will, in turn, line up with the revolution line on the barrel. Each line on the thimble scale stands for $1/1000$ (0.001) of an inch of screw movement. Every fifth line on the thimble is numbered (5, 10, 15, etc.). One complete and exact revolution of the thimble equals $25/1000$, or $1/40$ (0.025) of an inch.

Reading a Standard Micrometer Once you understand how the scales work, it is not hard to read the micrometer.

Just follow these steps:

Step 1.

First, check where the thimble edge is on the barrel scale. Read the highest figure visible on the barrel. In figure 4, on the previous page, this number is 2. Therefore, you know that the micrometer screw has moved more than $2/10$ (0.20) of an inch.

Step 2.

Count the number of lines you can see between the number you just read (in this case, 2) and the thimble edge. In the sample in figure 4, you can see only one line. Each line stands for 0.025 inch. Add what you have so far. In this case, you should get (0.20 inch + 0.025 inches) a total of 0.225 inch. You now know that the screw has moved more than 0.225 inch.

Step 3.

Now, look at the thimble scale. Find the line on the thimble scale that lines up with or has passed the revolution line in the barrel. In figure 8, this line is number 16 on the thimble scale. Each thimble scale line stands for 0.001 inch, so 16 of these equal 0.016 inch. Add this (0.016 inch) to what you have so far (0.225 inch) and the total measurement is 0.241 inch.

Reading a Vernier Micrometer A vernier micrometer is just like a standard micrometer except that it has a second scale on the barrel (figure 5, below). This second scale is a vernier scale. With the vernier scale added, the micrometer can be accurate to ten-thousandths (0.0001) of an inch. Use of the vernier scale gives the fine readings between the lines on the thimble. Without the vernier scale, you would have to estimate a ten-thousandth reading.

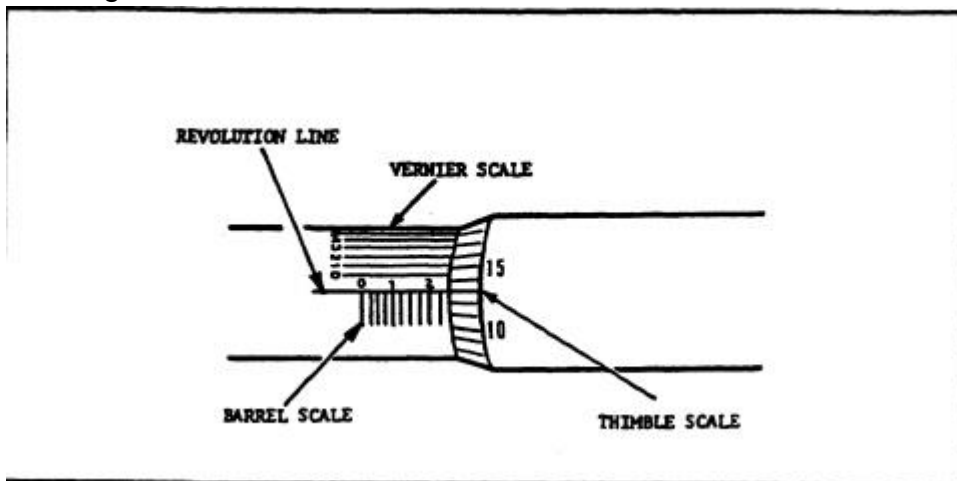


Fig. 5

VERNIER MICROMETER SCALES.

This vernier scale is divided into ten spaces. The ten spaces on the vernier scale take up the same length as nine spaces on the thimble scale. Each unit on the vernier scale equals 0.0009 inch. The size difference between the units on each scale is 0.0001 inch. You read the vernier micrometer the same as you read a standard one. However, you must take one more step. This step adds the vernier reading to the total size. Figure 6, below, shows the relationship of the barrel, thimble, and vernier scales. We will use this figure as a sample. To read the measurement shown in figure 10, Use these steps:
Step 1.

Read the highest figure showing on the barrel. In this case, that figure is 2. A 2 showing on the barrel means 0.200 inch.

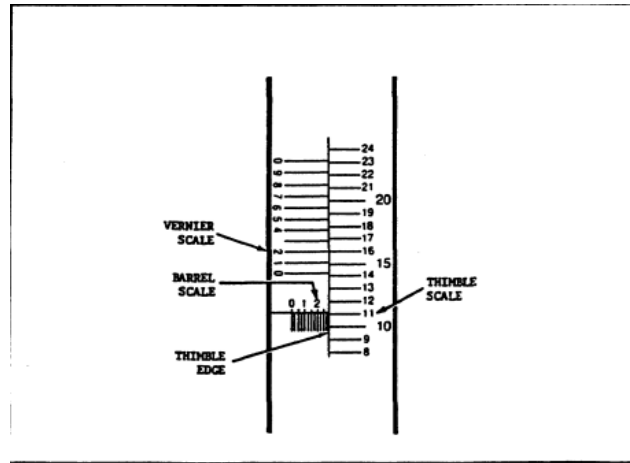


Fig 6

5.2.1 READING A VERNIER MICROMETER

Step 2.

Count the number of lines showing between the number you read (in this case 2) and the thimble edge . The sample in figure 6 has 3 lines showing. Each line stands for 0.025 inch. Therefore, 3 times 0.025 inch equals 0.075 inch. Add 0.075 inch to 0.200 inch. The subtotal is 0.275inch.

Step 3. Find the thimble scale line that lines up with or has passed the revolution line. For the setting in figure 10, the thimble scale line is 11. Each thimble line equals 0.001 inch, so 11 of them equal 0.011 inch. Add this (0.011 inch) to 0.275 inch to get 0.286 inch

Step 4.

So far, the reading is the same as it would have been on a standard micrometer. Now, however, you can use the vernier scale to get even greater accuracy. Find the line on the vernier scale that coincides (exactly lines up with) a line on the thimble. In figure 10, vernier scale line 2 coincides with a thimble scale line. Each line on the vernier scale stands for 0.0001 inch. Therefore, 2 vernier lines equal 0.0002 inch. Add this amount to the subtotal 0.286 inch. The result is 0.2862 inch. This is the exact size measured to the nearest 0.0001 of an inch. Understanding the Scales on a Metric Micrometer The metric micrometer uses the same scale/screw movement principle as the standard micrometer. However, the meaning of the lines on the barrel and thimble scales changes. On a metric micrometer, each full thimble turn moves the screw 0.5 millimeter (mm). The lines on the barrel scale (figure 7, below) read in millimeters, from 0 to 25. It takes two full thimble revolutions to move the screw 1.0mm

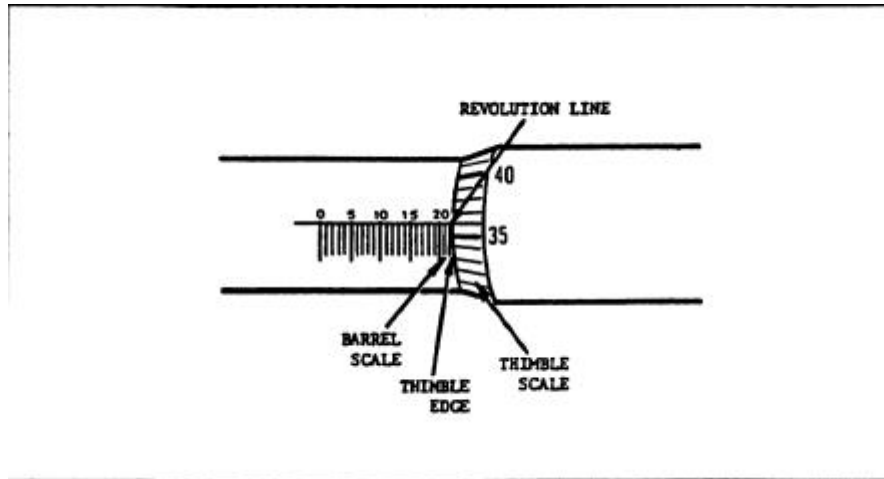


Fig.7

- READING A METRIC MICROMETER

The thimble scale has 50 lines. Every fifth line is numbered. As you turn the thimble, each thimble line passes the revolution line on the barrel. A turn equal to one thimble line moves the micrometer screw $\frac{1}{50}$ of 0.5mm, or $\frac{1}{100}$ mm. Two thimble lines equal $\frac{2}{100}$ mm, and so forth. Reading a Metric Micrometer Read a metric micrometer much like you read a standard one. Remember, it takes two full turns for the thimble edge to move one full space (one millimeter) on the barrel scale. To read the metric micrometer shown in figure 7 (on the previous page), use these steps:

Step 1. Read the highest number you can see on the barrel. In figure 7, the number is 20. This equals 20.0mm. Record this number.

Step 2. Count the number of lines you can see between the number 20 (the highest number you could see on the barrel) and the thimble edge. Each of these lines equals 1.0mm. In this case there are two lines. Two times 1.0mm equals 2.0mm. Add 2.0mm to 20.0mm, and the reading so far is 22.0mm.

Step 3. Find the thimble line that lines up exactly (coincides) with or has passed the revolution line (long line) on the barrel. In figure 7, this line is 36. Because each line on the thimble equals 0.01mm, 36 lines equals 0.36mm. Add this value to 22.0mm to arrive at the total measurement reading of 22.36mm.

NOTE

When finding the value for step 3 above, remember that each full turn of the thimble is equal to only 0.5mm. It takes two full turns of the thimble to move the spindle one whole millimeter. You found the number 36 in step 3 by assuming that the thimble was on its first turn. This was true because the thimble edge nearly touched the barrel mark. If the thimble was on its second turn, the edge would be away from the barrel line. In that case, the reading would have been 86 (50 + 36). The Effects of Outside Micrometer Size (Range) on a Reading Remember that the total movement between the anvil and spindle on an outside micrometer is only one inch. To make readings on items of various sizes, you must choose the right size outside micrometer. When you interpret the reading you



take with an outside micrometer, you must consider the size of micrometer you are using. The size of outside micrometer you are using tells you the biggest distance that you can measure with that micrometer. A two inch micrometer has a range between one and two inches. That means that it will only measure items that are between one and two inches in size. The biggest measurement reading you can get with this micrometer is two inches. A three inch micrometer has a range from 2 to 3 inches. It will measure items that are between 2 and 3 inches in size. The biggest measurement you can make with a three inch micrometer is 3 inches. Let's use a three inch outside micrometer as an example. To interpret the reading of a measurement you might take with a three inch micrometer, use these steps:

Step 1. Because it is a three inch micrometer, it will measure items between 2 and 3 inches in size. This tells you that the size of the item you are measuring is at least 2 inches; however, it can't be more than 3 inches. Therefore, the first number you record is 2.0 inches. You will find out how much bigger than 2.0 inches the size is by reading the micrometer scales.

Step 2. You read the scales exactly as you did before. First read the highest figure you can see on the barrel. Remember, each number on the barrel equals 0.1 inch. For example, if the number you see is 2, you would multiply 2 times 0.1 inch. The result is 0.2 inch. record 0.2 inch. Add 0.2 inch to 2.0 inches. The reading so far is 2.2 inches.

Step 3. Count the number of lines you can see between the highest figure seen on the barrel and the edge of the thimble. Remember, each of these lines equals 0.025 inch. For the current example, assume that you can see three lines. You would multiply 3 times 0.025 inch. The value is 0.075 inch. Add 0.075 inch to the 2.2 inches recorded from step 2. The subtotal for this example (2.2 inches + 0.075 inch) equals 2.275.

Step 4. Find the line on the thimble that coincides with or has passed the revolution line (long line) on the barrel. Assume that this line on the thimble is 24. Each thimble line is equal to 0.001 inch. Multiply 0.001 inch by 24. You should get 0.024 inch. Add this to the subtotal from step 3 (2.275 inches). Your grand total for the measurement should be 2.299 inches (2.275 inches + 0.024 inch). As you can see, the size of outside micrometer you are using will add whole inch values to your final reading. The outside micrometer size tells you the biggest reading you can get by using that micrometer. The Effects of a Depth Micrometer Extension Rod on a Reading Just as the size of outside micrometer effected your measurement reading, the size of the extension rod you select for your depth micrometer will have an effect. However, the kind of effect it has is slightly different. The outside micrometer size told you the biggest reading you could get with that micrometer. The size of the extension rod you choose for your depth micrometer tells you the smallest distance it will span. Using this knowledge as a guide, the first number you should record for a measurement reading taken with a depth micrometer is the size of the extension rod. For example, suppose your are taking a measurement using a depth micrometer with a 5 inch extension rod. The first number you should record is 5.0 inches.



Then read the micrometer scales just as you would for any micrometer measurement. Suppose the scales read 0.294 inch. Add this number to the 5.0 inches you have already recorded. The total depth measurement would be 5.294 inches.

5.2.2 CONCLUSION

This task has shown you how the scales on a vernier caliper and on a micrometer work. You have learned how to interpret the readings of these scales to come up with accurate measurements. Now you must learn how to actually use the tools to make precision measurements. Task 3 will show you the techniques for using these tools.

5.2.3 CHOOSING THE RIGHT MEASURING TOOL Which tool you select to take a measurement depends on the type of measurement you are taking and the accuracy you need. When taking inside and outside measurements, you can use either a vernier caliper or a micrometer (inside or outside). For depth measurements, you will be able to select from several depth instruments. There are advantages and disadvantages to each type of tool. Inside and Outside Measurements You can make inside or outside precision measurements with either a vernier caliper or with a micrometer (inside or outside). Vernier calipers tend to be more adaptable than micrometers. Micrometers, however, are more accurate. You can use the vernier caliper for many different kinds of measurements. You can use this one tool for both inside and outside measurements. Because of the shape of the jaws and their position with respect to the scale, the vernier caliper is more adaptable than a micrometer. However, the vernier caliper is not as accurate as a micrometer. If you need a very precise measurement, use a micrometer. A micrometer is more reliable and more accurate than a caliper.

Vernier Caliper. You may decide a vernier caliper is best for the measurement you are making. If this is so, you must choose a vernier caliper in a size that is larger than the measurement you want to make. Vernier calipers come in 6, 12, 24, and 36 inch sizes. Standard metric sizes are 150mm, 300mm, and 600mm. Remember that vernier calipers are not as accurate as micrometers. However, you can rely on given standards of accuracy from a well maintained caliper. If you check any one inch of its length, the caliper should be accurate within 0.001 inch. In any 12 inches, you should obtain accuracy within 0.002 inches. At most, this amount of inaccuracy should only increase by about 0.001 inch for each additional 12 inches

5.2.4 Inside Micrometers. You may choose to use an inside micrometer to make an inside measurement. This sub course will not show you the specific techniques for using an inside micrometer. We will, however, take a brief look at how to select the right inside micrometer extension rod You must choose an inside micrometer (figure 8, below) with a range that includes the approximate size you want to measure. This means you must consider the size of the micrometer unit, the range of its screw, and the length of the extension rods available. The smallest size you can check is equal to the size of the micrometer unit with its screw set to zero and its shortest anvil in place. The average inside micrometer set has a range from 2 to 10 inches. You use extension rods to cover the steps (by 1 inch increments) of this range. The micrometer set may also have a collar.



This collar is 0.5 inch long. It is used for splitting the inch step between two rods. The collar extends a rod another 0.5 inch. This allows the range of each step to overlap the next

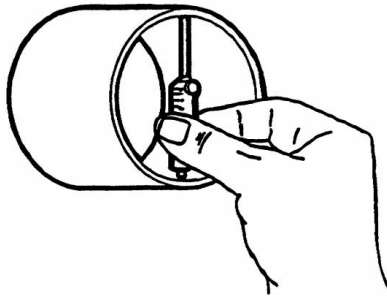


Fig 8

- CHOOSING AN INSIDE MICROMETER.

The range of the micrometer screw itself is very short. The smallest models have a 0.25 inch screw. Average models have a 0.5 inch screw. The largest inside micrometers have only a 1 inch screw. There are several things to consider if you want to properly choose an inside micrometer to make a measurement. First you must estimate the inside measurement you want to make. This estimate should be within the range of the micrometer screw. The size of the extension rod you need depends on the size and range of the inside micrometer. With the inside micrometer screw set to zero, you will fit an extension rod to the micrometer. If you choose the right extension rod, the total length of the micrometer and rod will be less than (but within the micrometer screw range of) the estimated distance to be measured.

- **Depth Measurements** You can use a depth micrometer to get very accurate depth measurements. Two other types of measuring tools are available for depth measurements. One of these is the rule depth gage; the other is the vernier depth gage. Although you will only learn how to use a depth micrometer in this sub course, we will describe the other two depth gages briefly . This is so that you can be familiar with the tools that might be available to you in the shop. If you want to learn more about using the rule depth gage or a vernier depth gage, look in TM 9-243. Rule Depth Gage. The rule depth gage (figure 13, on the next page) is a graduated rule. You may use it to measure the depth of holes, slots, counter bores, and recesses. This gage has a sliding head designed to bridge a hole or slot. The head holds the rule perpendicular to the surface from which you are measuring. The rule depth gage has a range of zero to five inches. The sliding head has a clamping screw so that it can be clamped in any position. The sliding head is flat. It is perpendicular to the axis of the rule. The head ranges in size from 2 to 2 5/8 inches wide and from 1/8 to 1/4 inch thick.

5.2.5 Depth Micrometer. The depth micrometer has a flat base attached to the barrel of a micrometer head. It usually has a range from zero to nine inches. Its range depends on the length of extension rod used. The hollow micrometer screw itself has a range of either 1/2 inch or 1 inch. The size of the flat base from 2 to 6 inches. The depth micrometer can enter a hole only 3/32 of an inch in diameter.

Vernier Depth Gage. The vernier depth gage (figure 9, on the next page) consists of a scale and a sliding head. The scale is either 6 or 12 inches long. The sliding head is a lot like the one on a vernier caliper. This head is specially designed to bridge holes and slots.

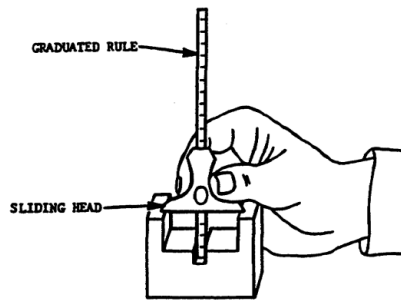


Fig .9

CHOOSING A RULE DEPTH GAGE

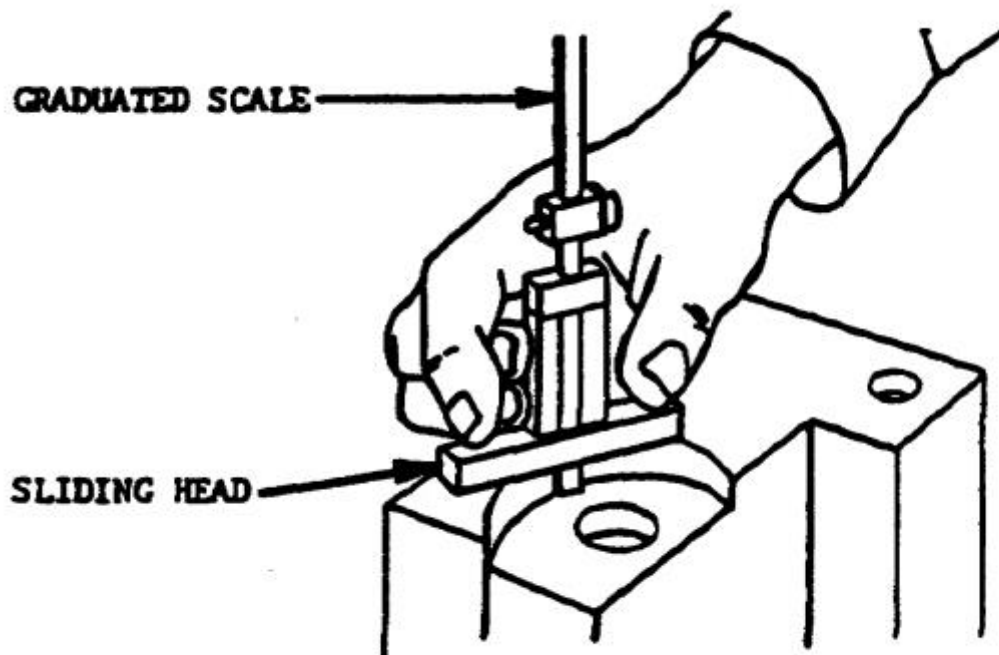


Fig 10

- CHOOSING A VERNIER DEPTH GAGE

You can use a vernier The vernier depth gage has the range of the rule depth gage. It is not quite as accurate as a depth micrometer. It cannot enter holes that are less than 1/4 inch in diameter. The depth micrometer is able to enter holes that have a 3/32 inch diameter. However, the vernier depth gage will enter a 1/32 inch slot, while the depth micrometer cannot. Selecting the proper tool for a measurement is important. It will help

you get the best measurement with the least amount of trouble. After you select a tool, you must know how to use it properly. First we will look at how to use a vernier caliper USING A VERNIER CALIPER Vernier calipers work a lot like slide calipers. caliper to make a very accurate outside measurement (figure 11, below). You can also use it to make an inside measurement (figure 12, on the next page). To make an accurate measurement, you must not only know how to operate the caliper, but how to use the right amount of pressure.

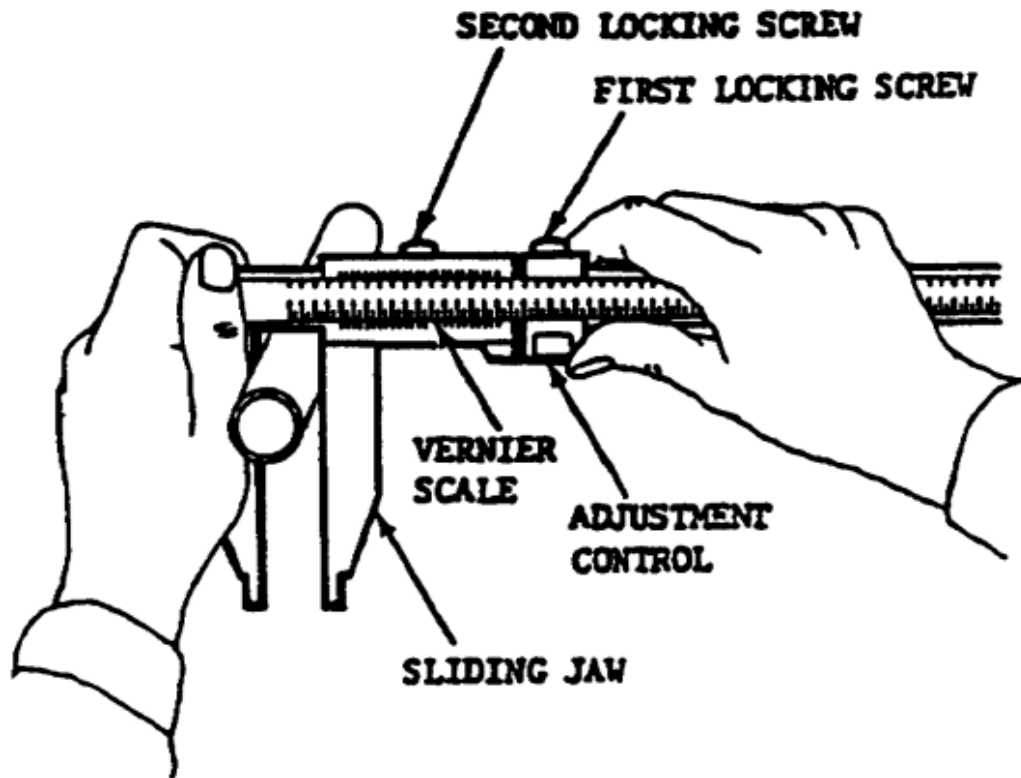


Fig 11
USING A VERNIER CALIPER TO MAKE

AN OUTSIDE MEASUREMENT

Operating the Vernier Caliper To use a vernier caliper, first loosen both locking screws. This will allow you to move the sliding jaw along the rule. Hold the fixed jaw in one hand, and move the sliding jaw with your other hand. When the jaws are in the position you want, secure the sliding jaw. Do this by tightening the locking screw above the adjustment control. Use the adjustment control to make any needed fine adjustments to the vernier scale. Tighten the second locking screw. If you are using the right amount of measuring pressure, you can now read an accurate measurement on the vernier caliper.

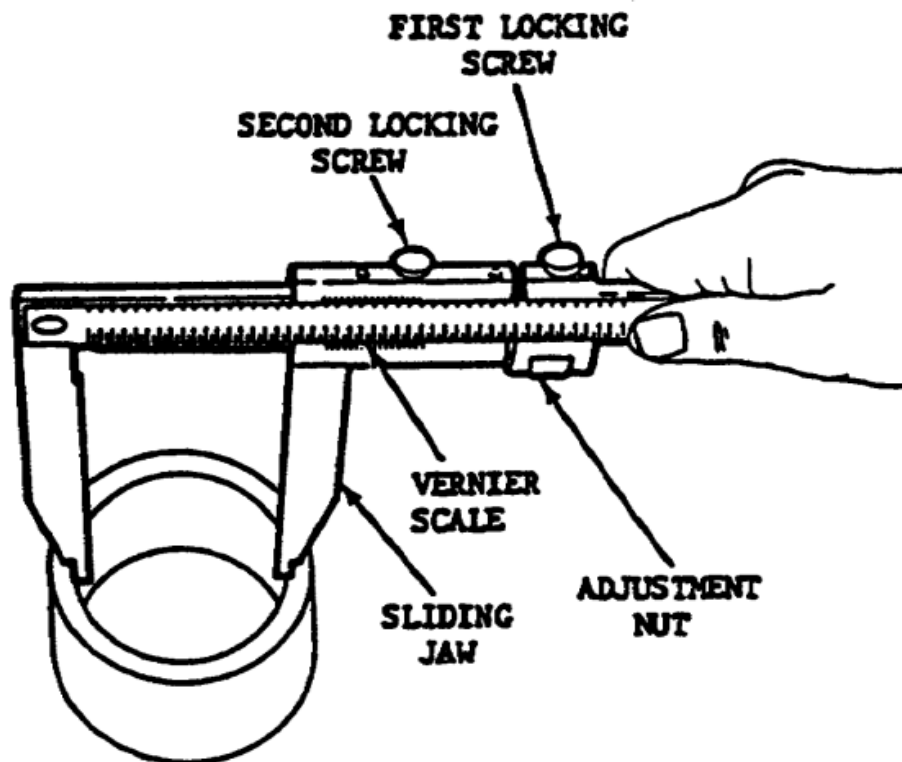


Fig 12

- USING A VERNIER CALIPER TO MAKE
 - AN INSIDE MEASUREMENT

Using the Right Pressure You will not get an accurate measurement with a vernier caliper unless you use the right amount of measuring pressure. If you use too much pressure, you might get a wrong reading because of play in the sliding jaw. Too little pressure can also result in the wrong reading. To get the right amount of pressure, you must be able to "feel" the measurement. The jaws of the caliper are long, and there can be some play in the sliding jaw, especially if you use too much pressure. This can cause inaccurate measurements. Therefore, you must develop the ability to handle the caliper. One way to do this is to practice by using the caliper to measure known standards. You might try measuring gage blocks or gage plugs until you consistently get accurate readings.

5.2.6 USING AN OUTSIDE MICROMETER

If you choose an outside micrometer instead of a vernier caliper, you will also get accurate readings of outside dimensions. Just as with the vernier caliper, the technique you use will effect the accuracy of your measurement.

Measuring Small Parts Figure 13, below, shows how you should hold your hands when you use an outside micrometer to measure a small part. You should hold the part in one hand; hold the micrometer in the other hand. Hold the micrometer so that the thimble rests between your thumb and your forefinger. From this position, you can use your third finger to hold the frame against the palm of your hand. If you support the frame this way, it will be easy to guide the part you are measuring over the anvil. Your thumb and forefinger are in a position to turn the thimble so that the spindle will move over against the part.

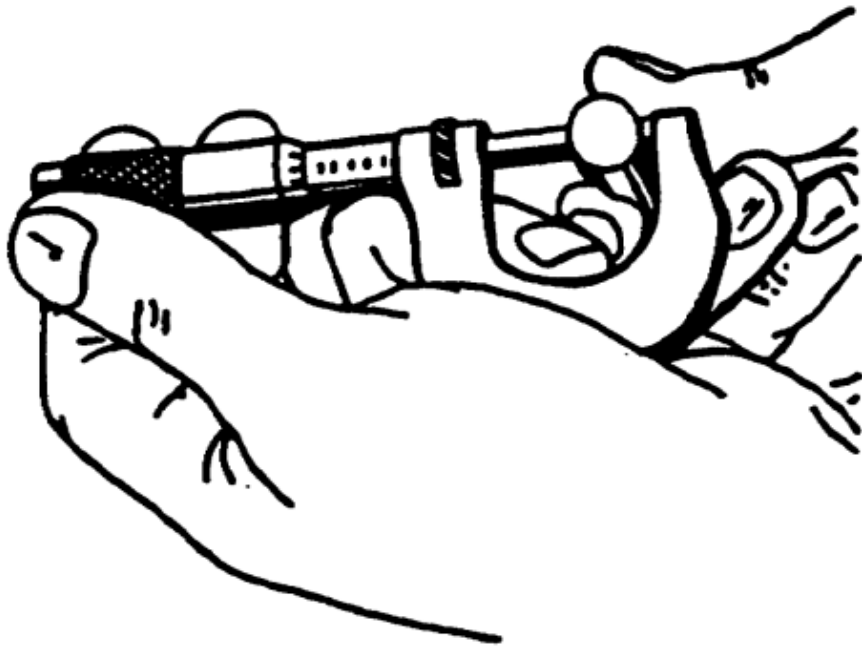


Fig 13
MEASURING A SMALL PART USING
AN OUTSIDE MICROMETER

Measuring Larger Work

When you measure larger work, you must hold the workpiece still, in a position where you can get at it with the micrometer. When you check a part too large to be held in one hand, you should use the method shown in figure 14, on the next page. Hold the frame in one hand to position it and to locate it square to the measured surface. Use your other hand to turn the thimble. A large, flat part should be checked in several places. This will tell you how much variation there is in the thickness of the part

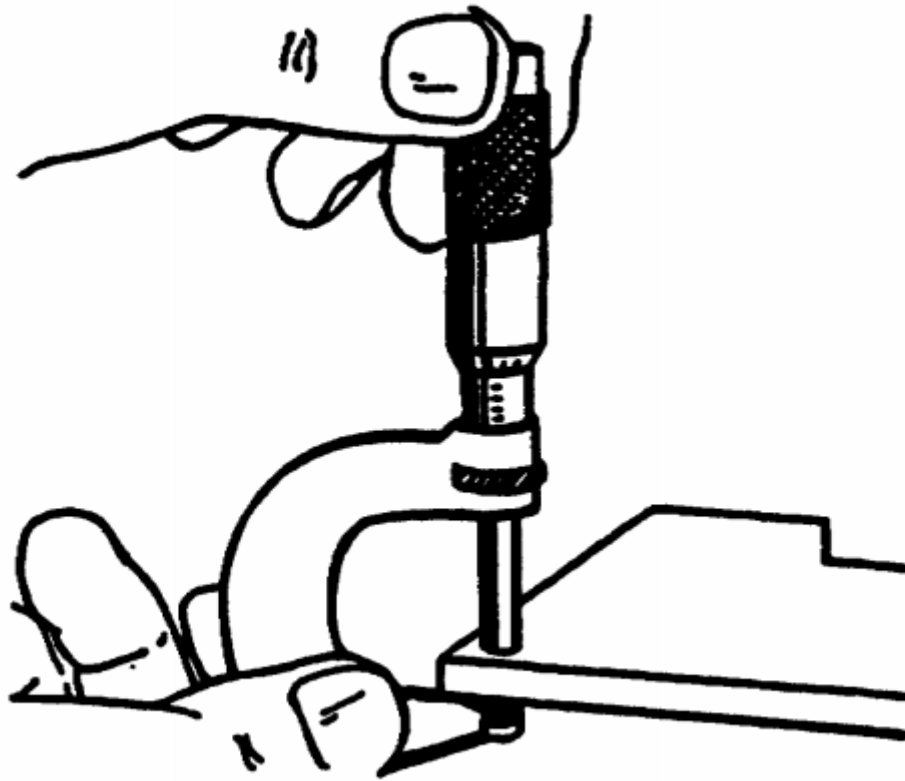


Fig 14

- USING AN OUTSIDE MICROMETER TO
MEASURE LARGER WORK

Techniques for Gaging a Shaft The hand positions you should use when gaging a shaft are shown in figure 15, on the next page. You hold the frame in one hand while turning the thimble with the other hand. When you gage a cylindrical part with a micrometer, you must be able to “feel” the setting. This is the only way you can be sure that the spindle is on the diameter. You must also check the diameter in several places to determine the out-of-roundness of the shaft.

Measuring Very Large Diameters

When you need to measure very large diameters, you may need to screw a special anvil to the frame of a micrometer. Outside micrometers are made in various sizes up to 168 inches. You can reduce the range of one of these micrometers by using a special anvil. A set of different length anvils lets you use a large micrometer over a wide range of sizes even though the spindle only moves one inch.

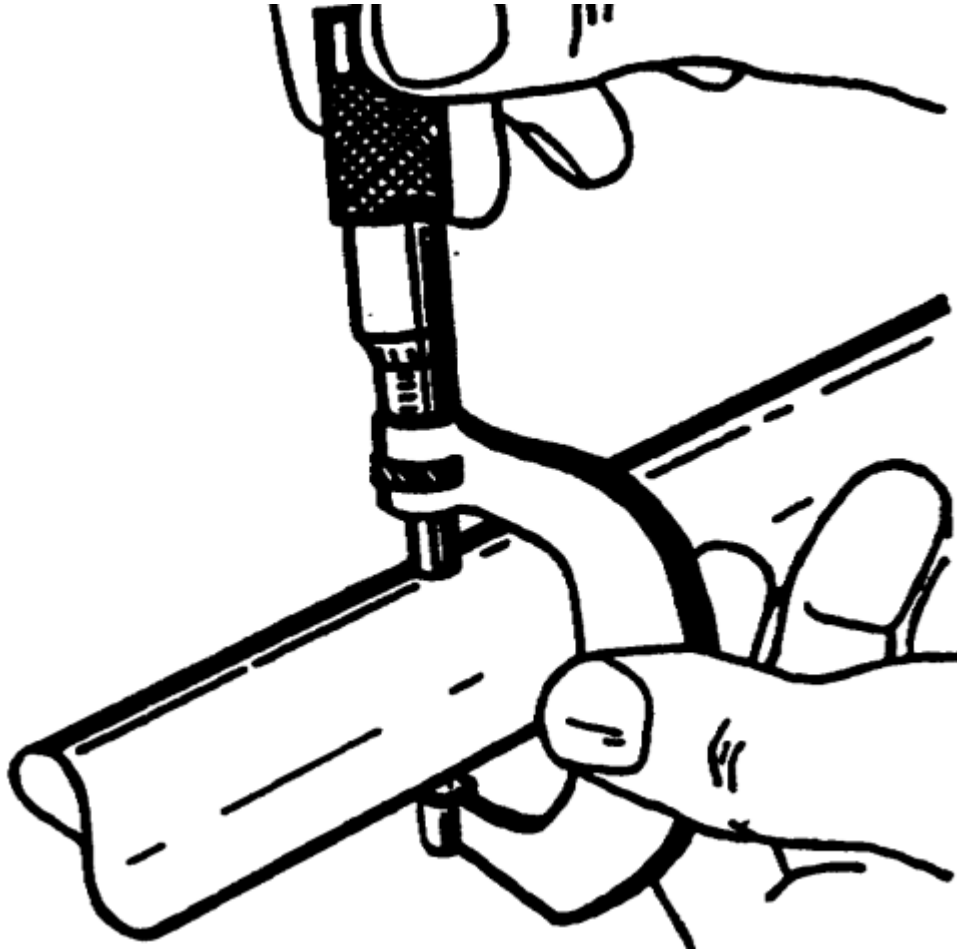


Fig 15

- USING AN OUTSIDE MICROMETER TO GAGE A SHAFT

- USING A DEPTH MICROMETER

When using a vernier caliper and an outside micrometer, you used special hand positions and techniques to get accurate measurements. The depth micrometer also requires special hand positions. Figure 16, on the next page, shows a depth micrometer being used to measure a projection. Look at the hand positions. You will use one hand to hold the flat base firmly against the measuring surface. In the other hand, you will hold the depth micrometer so that you can turn the thimble with the thumb and forefinger. When you use a depth micrometer, you must remember to select the proper extension rod. The rod you choose should be less than one inch shorter than your estimate of the measurement. For example, if you estimate that the measurement will be 4 1/4 inches, you should set the screw to zero and then fit a 4 inch extension rod to the micrometer. The one inch movement of the micrometer screw allows accurate measurement of the remaining distance

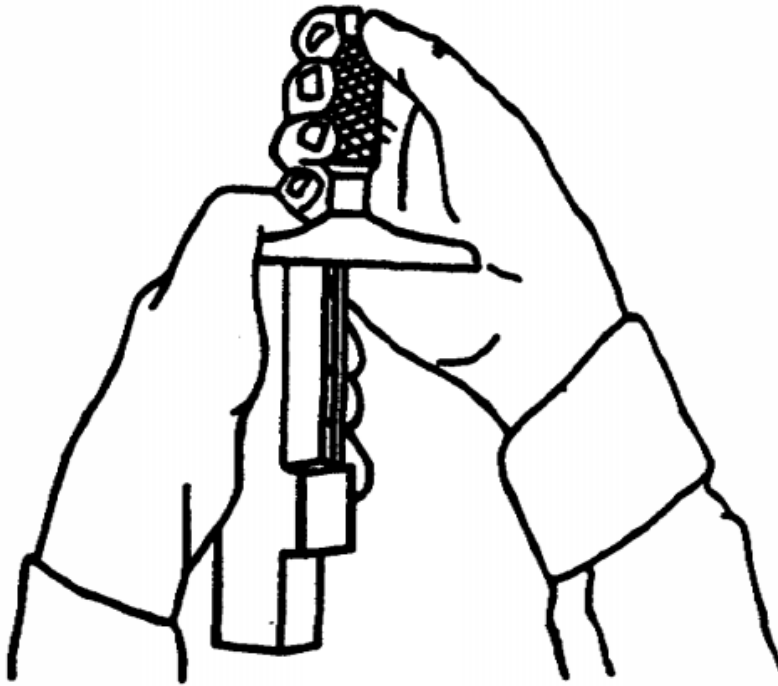


Fig 16
USING A DEPTH MICROMETER

5.3 CONCLUSION

You should now be able to select the right tool for the measurement you want to make. After selecting either a vernier caliper, an outside micrometer, or a depth micrometer, you should be able to use the techniques needed to get an accurate measurement. With the chosen tool in place, you will be able to read its scales accurately. You also now know how to properly care for one of these tools after you use it. Before you take the examination, try the practice exercise on the next page. It will help you check what you have learned about these three tools

1.4 .1 Try-square and Protractor, Telescopic gauge, Dial gauge.

Try Square: Care should be taken to ensure that its blade is perpendicular to the surface being tested

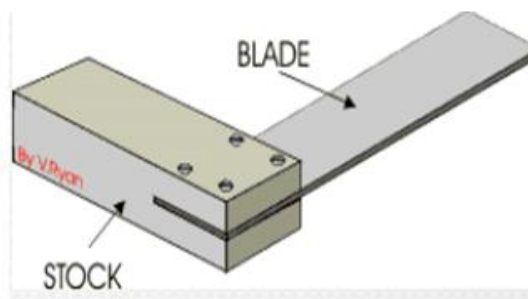


Fig. 17

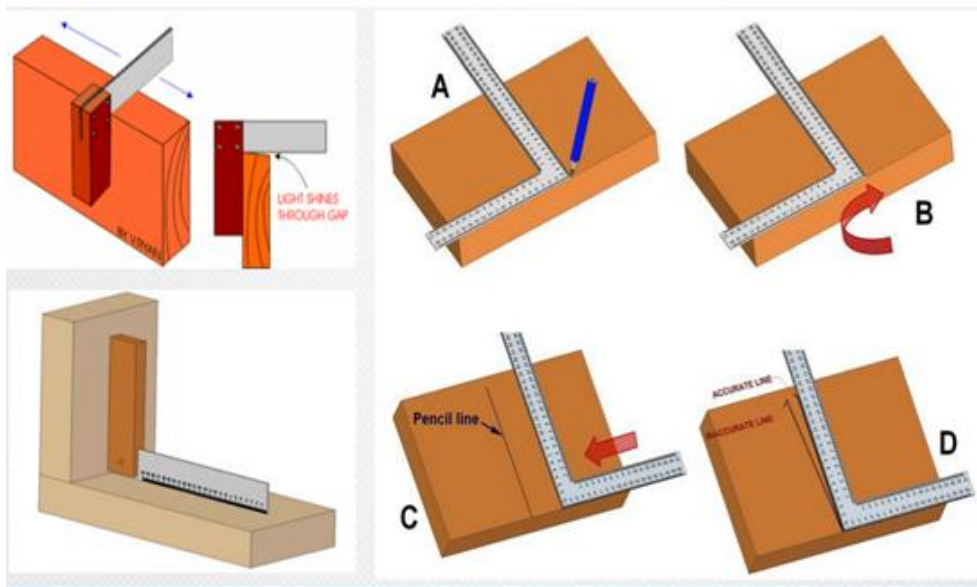


Fig.18

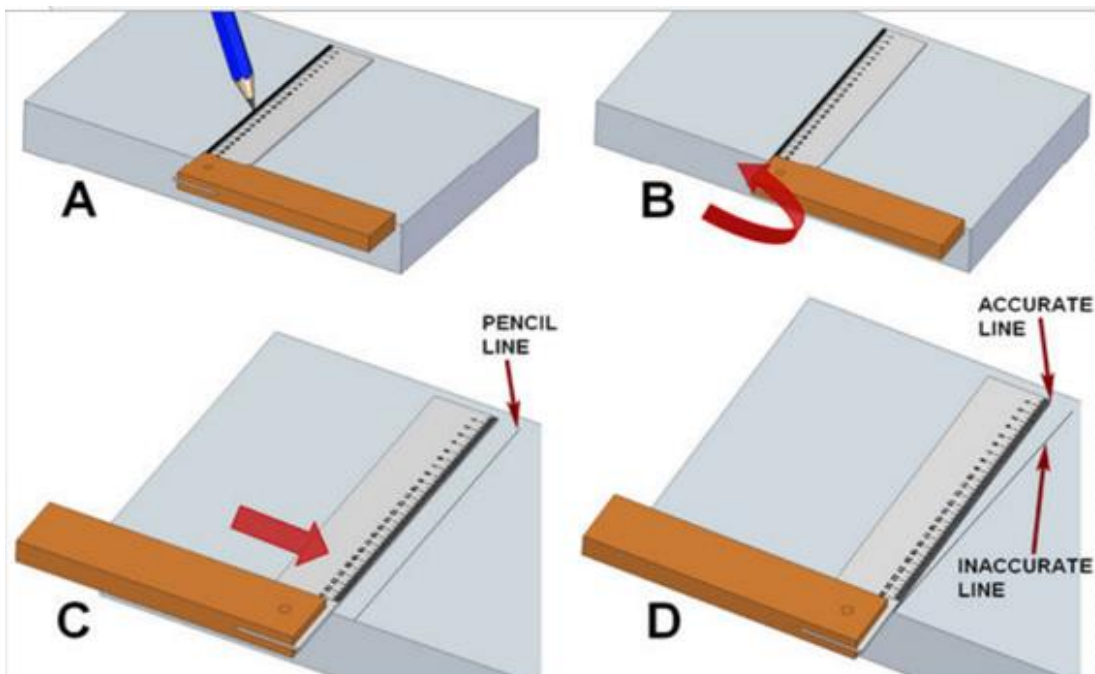


Fig .19

5.4.2 Telescopic gauge

- Used to measure inside cylinders.
- Allow “T” gauge to extend to inside opening
- Lock shaft
- Measure with micrometer

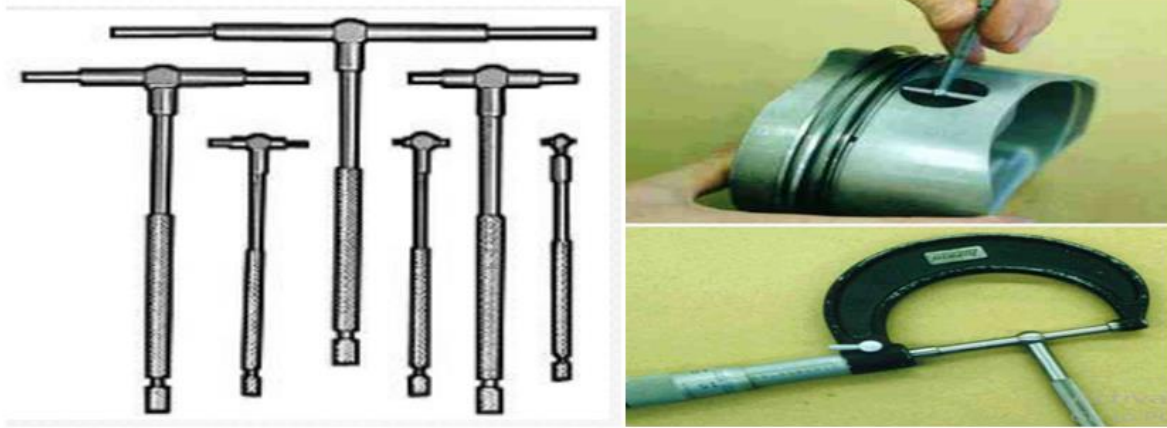


Fig.20

5.4.3 **Dial Indicators:** The dial indicators or dial gauges are generally used for testing flatness of surfaces and parallelism of bars and rods. They are also used for testing the machine tools.



Fig.21

5.5 Ammeter, Voltmeter and Mega-Ohmmeter

5.5.1 Ammeter:

- ✓ Measures current (A)
- ✓ connected **in series** (current must go through instrument)



5.5.2 Voltmeter:

- ✓ measures potential difference (V)
- ✓ connected **in parallel**



5.5.3 Ohmmeter:

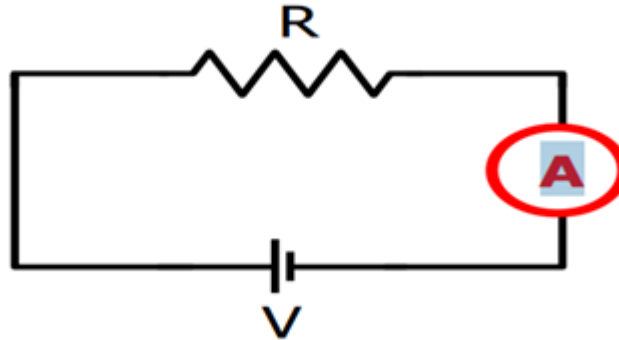
- ✓ measures resistance of an isolated resistor (not in a working circuit)



- **Effect of Ammeter on circuit**

Measuring current in a simple circuit: connect ammeter in series

Are we measuring the correct current? (The current in the circuit without ammeter)



Measuring current in a simple circuit: connect ammeter in series

Are we measuring the correct current? (The current in the circuit without ammeter)

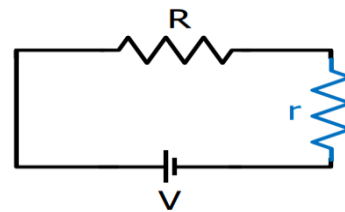
- Any ammeter has **some resistance r**.

- current in presence of ammeter is

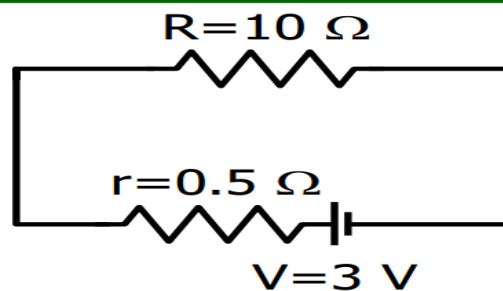
$$I = \frac{V}{R + r}$$

- current without the ammeter would be

$$I = \frac{V}{R}$$



Example: an ammeter of resistance 10 mΩ is used to measure the current through a 10 Ω resistor in series with a 3 V battery that has an internal resistance of 0.5 Ω. What is the relative (percent) error caused by the ammeter?

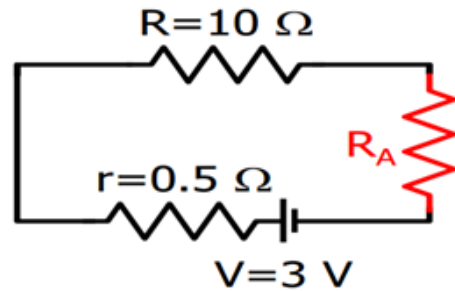


Actual current **without** ammeter

$$I = \frac{V}{R+r}, \quad I = \frac{3}{10+0.5} \text{ A}, \quad I = 0.2857 \text{ A} = 285.7 \text{ mA}$$

Current with ammeter:

- $I = \frac{V}{R+r+R_A}$,
- $I = \frac{3}{10+0.5+0.01} \text{ A}$,
- $I = 0.2854 \text{ A} = 285.4 \text{ mA}$
- $\% \text{ Error} = \frac{0.2857 - 0.2854}{0.2857} \times 100$
- $\% \text{ Error} = 0.1 \%$



5.5 PROTRACTOR

The measuring instruments used to measure the angle of the work pieces. There are two types of protractor. These are:

- A. Plain bevel protractor
- B. Vernier protractor

5.5.1 Plain bevel protractor: is one of the common protractors used in general mechanic work shop. It made from tool steel, hardened & tempered. The tool has two parts, these are

- A. Protractor, which is graduated in degrees from 0 degree to 90 degree on either side of the 90 degree mark.
- B. A blade, which is longer & held on to the protractor by a knurled lock nut.
 - The blade can be set at a various angles. The plain bevel protractor has an accuracy of degree, & hence it is not convenient for accurate (precision) work



Fig . 22 plain bevel protractor.

5.5.2 Vernier protractor: is another type of measuring instruments which is fitted to the vernier scale enabling angles to read to within 5 minutes of arc. This protractor is used to measure angle from 0 degree to 108 degree. It consists of:

- A. A Protractor dial graduated in degrees
- B. A base with a vernier scale attached
- C. A sliding blade which can be extended & set in all direction

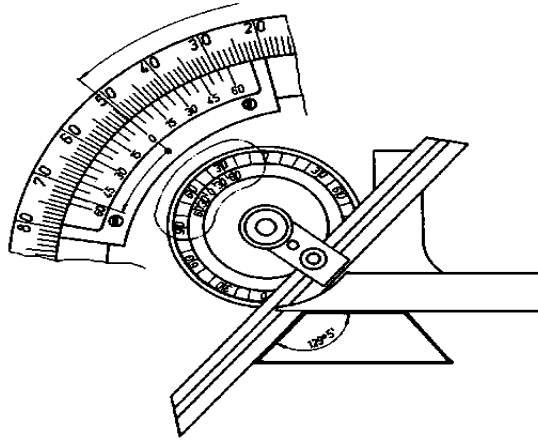


Fig. 23

• **READING THE VERNIER PROTRACTOR**

- A. Read the number of whole degree between the zero on the main scale & zero on the vernier scale.
- B. Count the number of division of spaces from zero on the vernier scale to the point where a vernier line coincides with a line on the main scale
- C. Multiply this number by five (each division on the vernier represents 5minutes).then add to the whole number of degrees

E.g From the figure, we get the following results,

- D. The number of whole degree is 60 degree

The coinciding mark of the vernier scale & main scale is on the fourth line which is $4 \times 5 \text{ minute} = 20 \text{ minute}$. Therefore the reading is 60 degree, 20 minute

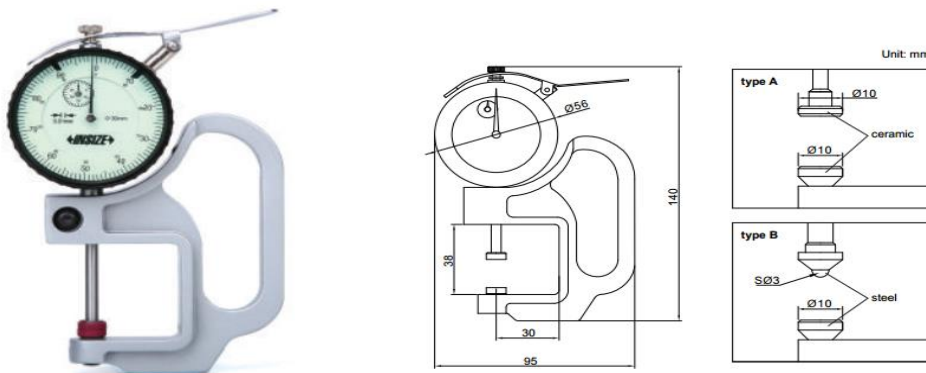


Fig.24 THICKNESS GAUGE



Code	Range	Accuracy	Type	Graduation
2366-30	0-30mm	A	±0.035mm	0.01mm
2366-30B	0-30mm	B	±0.035mm	0.01mm

STRAIGHT EDGE

Check flatness and straightness, as well as for marking Graduation on the beveled edge
 Made of hardened tool steel Chrome plated

Code	Size(L)	W	H	Straightness
50mm	4700-50	5	20	2.2µm
75mm	4700-75	5	25	2.3µm
100mm	4700-100	5	25	2.4µm
125mm	4700-125	5	25	2.5µm
150mm	4700-150	6	30	2.6µm
200mm	4700-200	6	30	2.8µm
250mm	4700-250	8	40	3.0µm
300mm	4700-300	8	40	3.2µm
400mm	4700-400	10	50	3.6µm
500mm	4700-500	10	50	4.0µm

(mm)

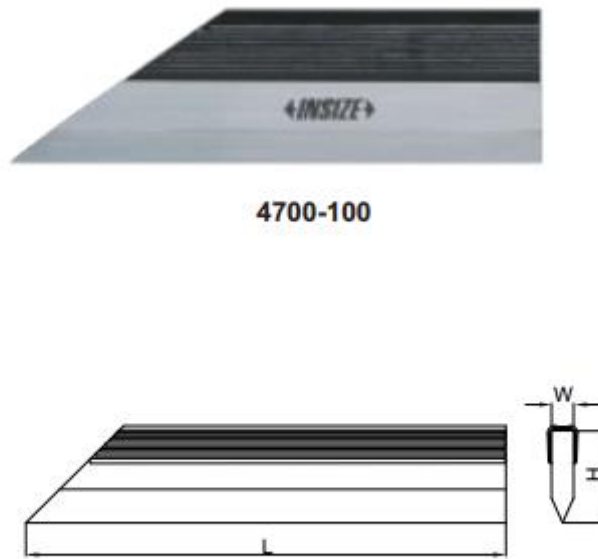


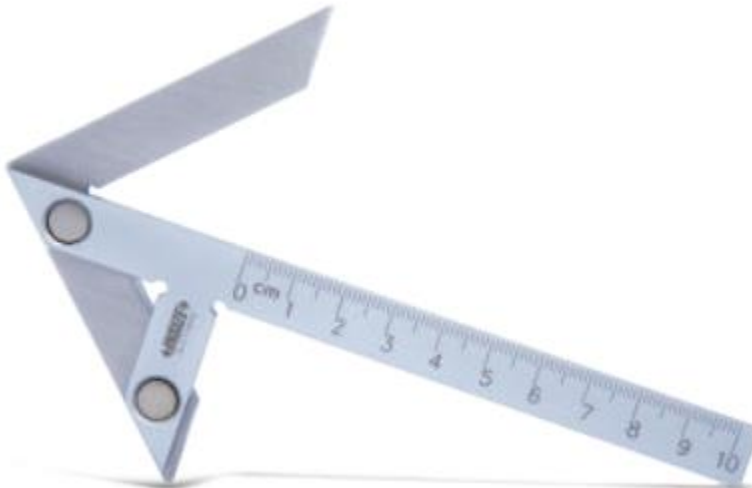
Fig .25

CENTER MARKING GAUGE

Marking the center of round plates and shafts

Made of stainless steel

Satin chrome plated



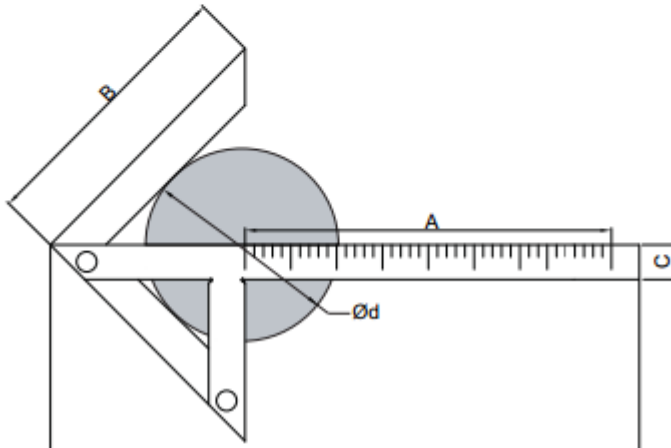
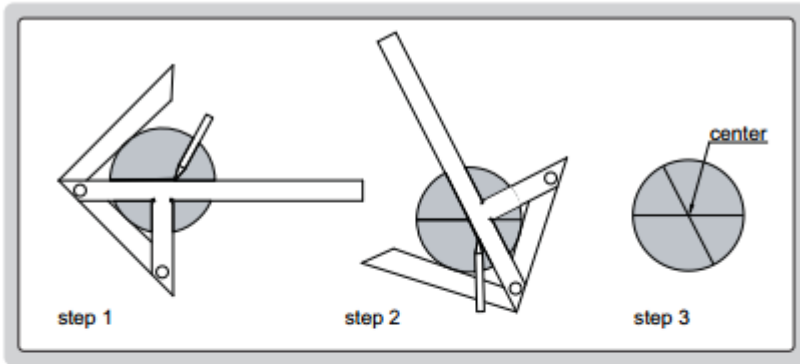


Fig.26

**Self-Check-5****Reading instruments**

Directions: choose the best answer for the following question (2 point each)

1. You measure the outside of the pipe with the vernier caliper. You hold the fixed jaw of the caliper in one hand what do you hold in the other hand?
A. Thimbel B. The sliding jaw C. The locking nuts D. fixed jaw
2. You measure the outside of the pipe with the vernier caliper. You hold the fixed jaw of the caliper in one hand What must be loosened so that the sliding jaw will move?
A. The locking nuts B. . fixed jaw C. sliding jaw D. None
3. You measure the outside of the pipe with the vernier caliper. You hold the fixed jaw of the caliper in one hand what can happen if you use too much pressure during the measurement?
A. You may get inaccurate measurements B. You may get accurate measurements
C. You may unable to read D. All
4. What part of the caliper is used to make fine adjustments after the caliper is in place?
A. The locking nuts B. sliding jaw C. The adjustment control D. fixed jaw
5. As you gage the tube, you check the diameter in several places. What are you trying to determine?
A T he amount of out-of-roundness B.T he amount of-roundness C .Both A&B D. None

Note: Satisfactory rating - 5 points

Unsatisfactory - below 5 points

You can ask you teacher for the copy of the correct answers

**Operation Sheet No. 4****Title:** Reading instruments**Purpose:** - Reading a Steel Ruler**Demands:** Measure Work piece and Obtain Accurate **measurements** to limit of the accuracy of the tool/ Instruments**Materials/Tools/ Equipment Needed:**

12. Students Guide
13. Steel ruler
14. Object to measure
15. Pencil or pen
16. Paper

Activities:

1. Place your ruler against the object, making sure that the first line of the ruler's gauge lines up exactly with your object's leading edge. Some gauges don't start right at the edge of the ruler, so make sure this slight gap is not included in your measurement.
2. Since rulers measure left-to-right, you will normally start at the object's left edge. But if the object is fixed in a place that won't accommodate the ruler, it may be necessary to flip the ruler around and read it from right to left. Make sure to place the unit gauge you're most comfortable with (e.g., inches) against the object's edge.
3. Read the gauge carefully. If you are measuring to determine the object's overall length, record the closest graduation marking that lines up with the end of the object.



4. To measure an object for cutting, mark the edge of the object with a fine pencil line at the desired dimension. Remember that sloppy marks will decrease accuracy, so avoid wide, slanting lines that obscure your measurement.

Performance Standard:**To get the full accuracy out of a rule**

- ✓ To get the full accuracy out of a rule, it is important to use it correctly. Never use the end of the rule to align with the edge of the work for a measurement (Figure 1). The end of a rule is often rounded off from misuse, and a true measurement will not be made.

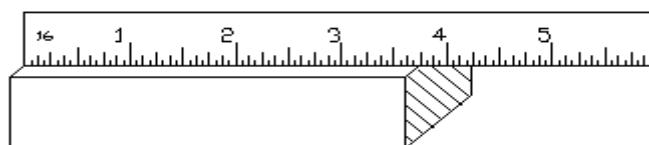


Figure 1

- ✓ Even if the workpiece is held firmly against a reference surface such as an angle plate (Figure 2), this will not assure an accurate measurement if the end of the rule is worn off.

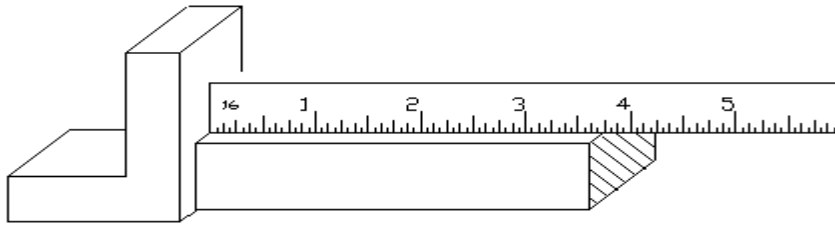


Figure 2.

- ✓ To offset this, use an inch graduation as a reference point on the rule (Figure 3). Precision and reliable measurements are possible this way. With the graduation directly on the edge of the work and by not using the end of the rule, wear is inconsequential.

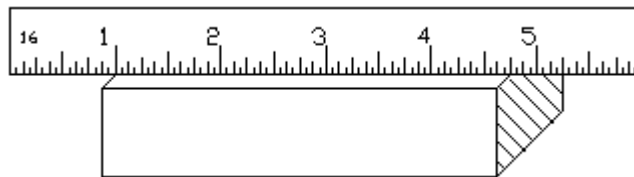


Figure 3

- ✓ When measuring a length, the rule must be kept in a straight line parallel to the centerline of the work. If it is tilted, the measurement will be longer than the actual part. See Figure 4.

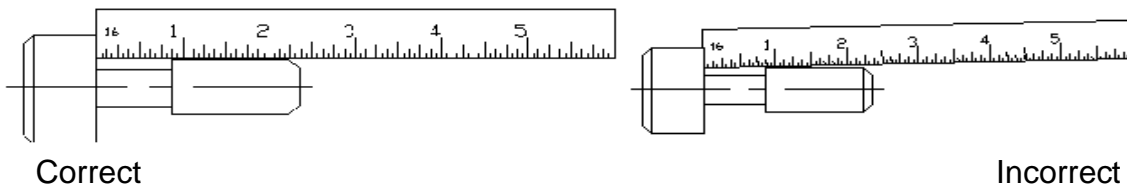


Figure 4.

- ✓ One other important factor in using the rule is to be aware of parallax. This is an observation error from the person measuring or holding at the part in relation to the part being held.



Figure 5.

The figure on the left is an incorrect way of measuring, and parallax is greatly increased because of the thickness of the rule. The graduations do not come in direct contact with the work. The arrows pointing to the right and left will cause parallax, and even though the arrow pointing straight up is the correct way to view the rule, there is a chance for error in reading due to the thickness of the rule. The figure on the right is used with the rule on edge. As can be seen, the graduation comes in contact with the work which is the correct



way of measuring. Although the arrows pointing to the right and left will cause an improper reading, it will not be as great an error as when used like the figure on the left. The proper way is to view the graduation straight up as the center arrow.





LAP Test	Carry-out measurements and calculations
-----------------	------------------------------------------------

Name: _____ Date: _____

Time started: _____ Time finished: _____

Instructions: Given necessary templates, tools and materials you are required to perform the following tasks within --- hour.

Task 1- trigonometric functions, algebraic computations

Task 2- Applications of Basic numerical computation

Task 3- Applications of Basic appropriate, formulae

Task 4- Reading instruments



This learning guide is developed to provide you the necessary information regarding the following **content coverage** and topics:

- Carrying out transposition of formulae involving the four fundamental operations.
- Solving equations involving one unknown
- Computing percentages
- Computing ratio and proportion

This guide will also assist you to attain the learning outcome stated in the cover page. Specifically, **upon completion of this Learning Guide, you will be able to:**

- Carry. transposition of formulae out to isolate the variable required , involving the four fundamental operations
- Solve. equations involving one unknown correctly
- . Compute percentages using Appropriate formula.
- . Compute ratio and proportion using appropriate formula.

Learning Instructions:

1. Read the specific objectives of this Learning Guide.
2. Follow the instructions described below.
3. Read the information written in the “Information Sheets”. Try to understand what are being discussed. Ask your trainer for assistance if you have hard time understanding them.
4. Accomplish the “Self-checks” which are placed following all information sheets.
5. Ask from your trainer the key to correction (key answers) or you can request your trainer to correct your work. (You are to get the key answer only after you finished answering the Self-checks).
6. If you earned a satisfactory evaluation proceed to “Operation sheets
7. Perform “the Learning activity performance test” which is placed following “Operation sheets” ,
8. If your performance is satisfactory proceed to the next learning guide,
9. If your performance is unsatisfactory, see your trainer for further instructions or go back to “Operation sheets”.



Information Sheet-1	Carrying out transposition of formulae involving the four fundamental operations.
----------------------------	------------------------------------------------------------------------------------------

1. CALCULATIONS ON ALJEBRIC EXPRESSION

1.1 Transposition of formula: is similar to solving equations .the basic rule which you must obey is " do to the left what you do to the right"

Eg. $Y = 4x - 3$, find the value of x

-add 3 to both sides

$$3 + y = 4x - 3 + 3$$

$$= y + 3 = 4x + 0$$

$$= y + 3 = 4x$$

-divide both sides by 4.

$$Y + 3/4 = 4x/4 \Rightarrow x = y + 3/4 \Rightarrow \frac{1}{4}(y + 3) \Rightarrow x = \frac{1}{4}y + \frac{3}{4}$$

Eg. Find the value of y from the given equation. $3y = 6 - ay$

$$ay + 3y = 6 - ay$$

$$ay + 3y = 6 - ay + ay$$

$$6 = ay + 3y$$

$$6/a + 3 = y(a + 3)/a + 3$$

$$Y = 6/a + 3$$

EXERCISE FOUR

-Find the value of letters in bracket

$$Y = 3x - 10 \quad \text{--} \quad (x) \quad Y = 7 - 2z$$

A. $Y = 5/x + 1 \quad \text{--} \quad (x)$

B. $C^2 = a^2 + b^2 \quad \text{--} \quad (b)$

C. $Y = y + x \quad \text{--} \quad (x)$

D. $A = 1/3b + 5 \quad \text{--} \quad (b)$

E. $A = b - c + d \quad \text{--} \quad (d)$

F. $Y = x + 1/x \quad \text{--} \quad (x)$

G. $Y = x/z \quad \text{--} \quad (z)$

H. $P = f - t/f + t \quad \text{--} \quad (f)$

Transposition of formulae

1.1.1 Transposition of Equations with Addition and Subtraction

= equals

- minus

+ plus

- **Concept of equality**

An equation can be compared to a pair of scales, which always remains in equilibrium. Thus we can transpose the two sides.

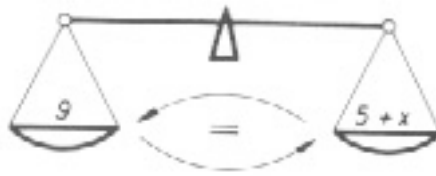


Fig.1

Thus $9 = 5 + x$
 $5 + x = 9$

Note

The commutation rule can be used.

- **Alterations**

We must always do the same thing on both sides, in order to maintain equilibrium

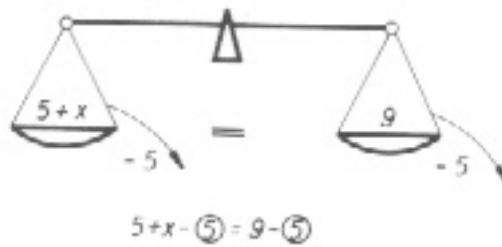


Fig 2

Note

Add the same

We must treat both sides in the same fashion

We can transpose the two sides

We should isolate the value sought on the left side-



Fig. 4

Following the basic rule

+ becomes -

- becomes +

1. **Example**

A cyclist covers a distance bounded by kilometer stone 4,8 and kilometer stone 56,4.
 How many kilometers have be traveled?

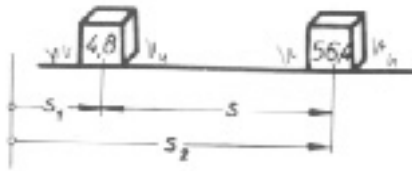


Fig.5

Find s
 Given $s_1 = 4.8 \text{ km}$ preliminary consideration
 That $s_2 = 56.4 \text{ km}$ a clarifying sketch helps

Solution $s_2 = s_1 + s$
 $s = s_2 - s_1$
 $s = 56.4 \text{ km} - 4.8 \text{ km} = 51.6 \text{ km}$

Note
 The numbering of the kilometer stones starts at zero.

1.1.2 Transposition of Equations with Multiplication and Division

= equal
 x multiplied by
 --- divided by

- **Concept of equality**

Always keep the equilibrium –scales in a state of balance.

$$20 = 4 \times X$$

$$4 \times X = 20$$



Fig.6

Note
 The communication rule can be used.

- **Alterations**

We must always do the same thing on both sides, in order to maintain equilibrium.

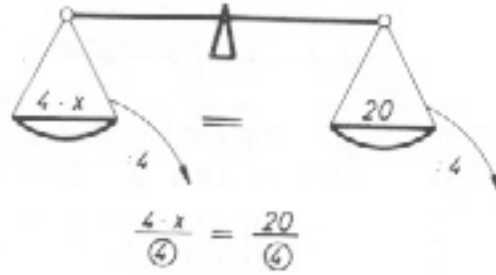


Fig.7

Note

Multiply by the same amount on both sides or
Divide by the same amount on both sides

- **Basic Rule**

We derive the following relationship from the diagram below:

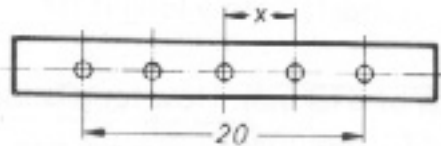


Fig.8

$$4 \times X = 20$$

$$X = 20/4 = 5$$

Result

When sides are changed, the sign also changes

Rule

x becomes /

/ becomes x

- **Summary**

We must treat both sides in the same fashion

We can transpose the two sides

We should isolate the value sought on the left side-

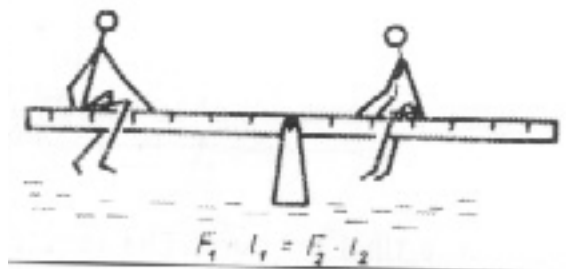


Fig.9



Following the basic rule
x becomes /
/ becomes x

1. Example

A 385 mm long flat steel rail is to have six holes drilled in it, with the same distances between their center and edges. Calculate the spacing of the holes in mm

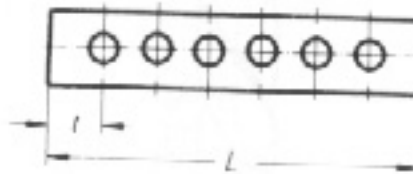


Fig 10

Find t
Given $L = 385 \text{ mm}$ preliminary consideration
That $n = 6$ clarifying sketch helps
Solution $L = (n + 1) \times t$
 $t = \frac{L}{n + 1}$
 $= \frac{385 \text{ mm}}{6 + 1}$
 $t = 55 \text{ mm}$

Note

A different distance from the edges influences the spacing equation

**Self-Check-1****Transposition**

Directions: choose the best answer for the following question (2 point each)

1. Transposition means do to the left what you do to the right.
A. True B. False
2. During transposition alterations means.
 - A. Always Add the same amount to both sides
 - B. Always Subtract the same amount from both sides
 - C. Add or Subtract the same amount from both sides
 - D. None

Note: Satisfactory rating - 2 points

Unsatisfactory - below 2 points

You can ask you teacher for the copy of the correct answers



Operation Sheet 1

Transposition

Operation Sheet No. 1

Title: - Perform calculations on algebraic expressions

Purpose: - perform calculations on algebraic expressions using the four fundamental operations with emphasis in Transposition.

Materials/Tools/ Equipment Needed:

1. Students Guide
1. Paper
2. Pen
3. Mathematical tables

Activities:

1. Perform Simple calculations on algebraic expressions using the four fundamental operations
2. Carry out Transposition of formulae to isolate the variable required, involving the four fundamental operations.
3. Construct appropriate formulae to enable problems to be solved

Performance Standard:

The trainees should be able to solve problems concerning the applications of algebraic expressions using the four fundamental operations

Information:

Illustrating the Basic Steps in Solving and in Presenting Solutions of Mathematical Problems

Basic Steps

1. Statement of the Problem
2. Comprehension

Read the text of the problem slowly and carefully and visualize the situation clearly. If possible, make a sketch.

3. Framework

Write down neatly the values which have been given and which are to be found, using symbols and dimensions.

4. Basic Equation

Relate the situation recognized to the relevant Basic Equation, Only then solve for the required value.

5. Illustration

6. Solve correctly the questions given the evaluation section of the lesson.

**Notes:**

Make sure that the calculation proceeds step by step. Formulate the answer — at least in your head — as a complete sentence.

In addition it is a good idea to do a rough calculation before the final one. Besides this, always check the dimensions by carrying and shortening the units of measurement.

Remarks:

The emphasis in the lesson is the capability of the students to solve application problems. It is therefore recommended that due attention should be given to the exercises with the close supervision of the instructor. In mathematics, there is no substitute for practice.

The teacher shall always set a deadline for finishing a task. But fast students should be given a chance to solve more calculation problems and in so doing acquire more experience.

The teacher should act as a student's consultant, which is an active role. Thus, he shall go around in the class, look at the students' solutions while they do them and give advice.

Summary:

Read – comprehend - sketch

Relate the situation to the basic equation

**2.1 EQUATIONS WITH ONE UNKNOWN variable**

Eg. $7 = 2x - 13$ --- the unknown is x . The equation is a linear equation. $13 + 7 = 2x - 13$
 $+13 = 20 = 2x + 0, x = 10$

2.1.1 When unknown occurs twice: $5x + 7 = 2x + 40 \Rightarrow 5x - 2x = 40 - 7 \Rightarrow 3x = 33, x = 11$

2.1.2 Equation with fractions: $= \frac{1}{2}x = \frac{3x}{8} + 13 \Rightarrow \frac{x}{2} = \frac{3x + 104}{8} \Rightarrow 2(3x + 104) = 8x \Rightarrow$

$6x + 208 = 8x \Rightarrow 208 = 8x - 6x \Rightarrow 208 = 2x \Rightarrow x = 104$

.Exercise Solve the equation, $\frac{2}{5}x = \frac{3}{4}x - 28, x = (80)$. Equations with brackets:

$2(x - 3) = 5(x - 21) \Rightarrow 2x - 6 = 5x - 105 \Rightarrow 105 - 6 = 5x - 2x, 99 = 3x, x = 33$

- Exercise Solve the equations, $3(x + 7) = 2(x + 29) \text{ ----- } x = 37$

2.2 Equations with un known denominator:

.Eg. $3/2x = 5, x = 0.3$

.Exercise Solve the equations

A. $7/3x = 5, x = 7/15$

C. $5/X + 2 = 4/X - 3, X = 23$

B. $3/x + 7 = 1/x + 1, x = 2$

2.3 SYMULTANEOUS EQUATIONS

Eg. $3x + y = 8$

$3x + y = 8, 3(4) + y, 12 + y = 8, y = 4$

$2x - y = 12$

$5x = 20, x = 4$

Exercise $5x + 3y = 31$

$5x + 3y = 31$

$3x + y = 17$

$5(5) + 3y = 31$

$5x + 3y = 31$

$25 + 3y = 31$

$-9x - 3y = 51$

$3y = 31 - 25, y = 2$

$-4x = -20$

$X = 5$

.Exercise Solve these equations.

A. $3x - 5y = 16$

$4x + 3y = 31, x = 7, y = 1$

B. $2X + 7Y = 39$

$5X - 4Y = 10, X = 2, Y = 5$

**Self-Check-2****Written Test**

Directions: choose the best answer for the following question

Evaluate each algebraic expression when $x=-2$ and $y= 5$ (6 points)

A. $2y-3x$ B. $5x + x^2$ C. $5 - x^2$

1. Evaluate each algebraic expression when $x=2$ $y= -1$ (2 points)

A. $x^2 - 2xy + y^2$

2. Evaluate each algebraic expression when $3/x+7 = 1/x+1$, $x=2$ (2 points)

Note: Satisfactory rating - 5 points

Unsatisfactory - below 5 points

You can ask you teacher for the copy of the correct answers



Operation Sheet 2

equations involving one unknown

Operation Sheet No. 2

Title: - equations involving one unknown

Purpose: - Computing equations involving one unknown.

Materials/Tools/ Equipment Needed:

1. Students Guide
2. Paper
3. Pen
4. Mathematical tables

Activities:

1. Solve problems on the applications of equations;
2. Solve problems on the applications of equations involving one unknown.

Performance Standard:

The trainees should be able to solve problems concerning the applications of equation and Solve problems on the applications of one unknown;

Information:

Illustrating the Basic Steps in Solving and in Presenting Solutions of Mathematical Problems

Basic Steps

B. Statement of the Problem

C. Comprehension

Read the text of the problem slowly and carefully and visualize the situation clearly. If possible, make a sketch.

D. Framework

Write down neatly the values which have been given and which are to be found, using symbols and dimensions.

E. Basic Equation

Relate the situation recognized to the relevant Basic Equation, Only then solve for the required value.

F. Illustration

G. Solve correctly the questions given the evaluation section of the lesson.

Notes:

Make sure that the calculation proceeds step by step. Formulate the answer — at least in your head — as a complete sentence.

In addition it is a good idea to do a rough calculation before the final one. Besides this, always check the dimensions by carrying and shortening the units of measurement.

Remarks:

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The emphasis in the lesson is the capability of the students to solve application problems. It is therefore recommended that due attention should be given to the exercises with the close supervision of the instructor. In mathematics, there is no substitute for practice.

The teacher shall always set a deadline for finishing a task. But fast students should be given a chance to solve more calculation problems and in so doing acquire more experience.

The teacher should act as a student's consultant, which is an active role. Thus, he shall go around in the class, look at the students' solutions while they do them and give advice.

Summary:

Read – comprehend - sketch

Relate the situation to the basic equation



3.1 Percentage calculations

Percentage calculation procedures have many applications in machining, design, and metalworking problems. Although the procedures are relatively simple, it is easy to make mistakes in the manipulations of the numbers involved.

Ordinarily, 100 percent of any quantity is represented by the number 1.00, meaning the total quantity. Thus, if we take 50 percent of any quantity, or any multiple of 100 percent, it must be expressed as a decimal:

$$1\% = 0.01$$

$$10\% = 0.10$$

$$65.5\% = 0.655$$

$$145\% = 1.45$$

In effect, we are dividing the percentage figure, such as 65.5 percent, by 100 to arrive at the decimal equivalent required for calculations.

Let us take a percentage of a given number:

$$45\% \text{ of } 136.5 = 0.45 \times 136.5 = 61.425$$

$$33.5\% \text{ of } 235.7 = 0.335 \times 235.7 = 78.9595$$

Let us now compare two arbitrary numbers, 33 and 52, as an illustration:

$$\frac{52 - 33}{33} = 0.5758$$

Thus, the number 52 is 57.58 percent larger than the number 33. We also can say that 33 increased by 57.58 percent is equal to 52; that is, $0.5758 \times 33 + 33 = 52$. Now,

$$\frac{52 - 33}{52} = 0.3654$$

Thus, the number 52 minus 36.54 percent of itself is 33. We also can say that 33 is 36.54 percent less than 52, that is, $0.3654 \times 52 = 19$ and $52 - 19 = 33$. The number 33 is what percent of 52? That is, $33/52 = 0.6346$. Therefore, 33 is 63.46 percent of 52.

Example of a Practical Percentage Calculation. Aspring is compressed to 417 lbf and later decompressed to 400 lbf, or load. The percentage pressure drop is $(417 - 400)/417 = 0.0408$, or 4.08 percent. The pressure, or load, is then increased to 515 lbf. The percentage increase over 400 lbf is therefore $(515 - 400)/515 = 0.2875$, or 28.75 percent. Percentage problem errors are quite common, even though the calculations are simple. In most cases, if you remember that the divisor is the number of which you want the percentage, either increasing or decreasing, the simple errors can be avoided. Always back-check your answers using the percentages against the numbers.



The **percentage rate** gives the fraction of the base value in hundredths.
The **base value** is the value from which the percentage is to be calculated.
The **percent value** is the amount representing the percentage of the base value.

P_r percentage rate, in percent P_v percent value B_v base value.

1st example

Workpiece rough part weight 250 kg (base value); material loss 2% (percentage rate); material loss in kg = ? (percent value)

$$P_v = \frac{B_v \cdot P_r}{100\%} = \frac{250 \text{ kg} \cdot 2\%}{100\%} = 5 \text{ kg}$$

Percent value

$$P_v = \frac{B_v \cdot P_r}{100\%}$$

Percentage rate

$$P_r = \frac{P_v}{B_v} \cdot 100\%$$

2nd example

Rough weight of a casting 150 kg; weight after machining 126 kg; weight percent rate (%) of material loss?

$$P_r = \frac{P_v}{B_v} \cdot 100\% = \frac{150 \text{ kg} - 126 \text{ kg}}{150 \text{ kg}} \cdot 100\% = 16\%$$

**Self-Check-3****Compute percentage**

Directions choose the best answer for the following questions

1. Express each of the following percentages as fraction.(8 points)

A. $5\frac{1}{2}\%$ B.) 70% C.) 8% D. 40%

2. Express each of the following percentages as decimals.

A. 50% B.) 85% C. 7% D. $17\frac{1}{2}\%$

Note: Satisfactory rating - 8 points

Unsatisfactory - below 8 points

You can ask you teacher for the copy of the correct answers



Operation Sheet 3

Compute percentage

Operation Sheet No. 3

Title: - Compute percentage

Purpose: - Computing Percentages using appropriate formula.

Materials/Tools/ Equipment Needed:

3. Students Guide
4. Paper
5. Pen
6. Mathematical tables

Activities:

1. Solve problems on the applications of equations;
2. Solve problems on the applications of percentages;

Performance Standard:

The trainees should be able to solve problems concerning the applications of equation and Solve problems on the applications of percentages;

Information:

Illustrating the Basic Steps in Solving and in Presenting Solutions of Mathematical Problems.

Basic Steps

- i. Statement of the Problem
- ii. Comprehension
Read the text of the problem slowly and carefully and visualize the situation clearly. If possible, make a sketch.
- iii. Framework
Write down neatly the values which have been given and which are to be found, using symbols and dimensions.
- iv. Basic Equation
Relate the situation recognized to the relevant Basic Equation, Only then solve for the required value.
- v. Illustration
- vi. Solve correctly the questions given the evaluation section of the lesson.

Notes:

Make sure that the calculation proceeds step by step. Formulate the answer — at least in your head — as a complete sentence. In addition it is a good idea to do a rough calculation before the final one. Besides this, always check the dimensions by carrying and shortening the units of measurement.

**Remarks:**

The emphasis in the lesson is the capability of the students to solve application problems. It is therefore recommended that due attention should be given to the exercises with the close supervision of the instructor. In mathematics, there is no substitute for practice. The teacher shall always set a deadline for finishing a task. But fast students should be given a chance to solve more calculation problems and in so doing acquire more experience. The teacher should act as a student's consultant, which is an active role. Thus, he shall go around in the class, look at the students' solutions while they do them and give advice.

Summary:

Read – comprehend - sketch

Relate the situation to the basic equation



4.1. Ratios

A ratio is used to make comparisons between two similar terms. The items within a ratio are typically of the same units and the resulting comparison is dimensionless (i.e., no units).

Ratios are typically expressed in one of three ways, the first being the most common:

- A fraction (division):
- In words, using “to”: 5 to 6
- With a colon: 5:6

For instance, RU has 409 biology majors and 76 math majors. As a ratio the number of biology majors to math majors is

$$\frac{\# \text{ biology majors}}{\# \text{ math majors}} = \frac{409 \text{ students}}{76 \text{ students}} = 5.38..$$

The number of biology majors : math majors is approximately 5:1.

Ex.) The Energy Payback Ratio is used to evaluate power plants:

$$EPR = \frac{\text{energy generated}}{\text{energy consumed}}$$

What is the payback ratio when 2,800,000 GJ are consumed to generate 11,350,000 GJ in a plant powered by natural gas?

$$EPR = \frac{\text{energy generated}}{\text{energy consumed}} = \frac{11,359,000}{2,800,000} = 4.057 \approx \frac{4}{1}$$

The ratio is about 4:1

Ex.) In an experiment Mendel interbred true yellow round seed peas with true green wrinkled seed peas. The F₂ progeny produced were 315 yellow round seeds, 108 green round seeds, 101 yellow wrinkled seeds and 32 green wrinkled seeds. Approximate the ratio of phenotypes as A:B:C:D so that A+B+C+D=16



$$315 + 108 + 101 + 32 = 556$$

$$\frac{315}{556} = 0.5665467625899281,$$

$$\frac{101}{556} = 0.1816546762589928,$$

$$\frac{108}{556} = 0.1942446043165468$$

$$\frac{32}{556} = 0.0575539568345324$$

Multiplying by 16

$$\frac{315}{556} \cdot 16 = 9.064748201438849,$$

$$\frac{101}{556} \cdot 16 = 2.906474820143885,$$

$$\frac{108}{556} \cdot 16 = 3.107913669064748$$

$$\frac{32}{556} \cdot 16 = 0.920863309352518$$

Estimated the ratios 9: 3: 3: 1

4.2 Proportion

4.2.1 Introduction

Proportion is another way of expressing notions of part and whole. You might say that the proportion of village inhabitants who are children is a quarter, or that the proportion of fruit juice in the punch is two thirds, or that the proportion of sand in the concrete is three quarters. All these examples involve the fractions $\frac{1}{4}$, $\frac{2}{3}$, $\frac{3}{4}$. Problems involving proportions are best handled by manipulating fractions, generally, by division or multiplication. The task is to decide which fraction to manipulate, in what way, and at what stage!

4.2.2 Direct proportion

In a recipe the quantity of each ingredient needed depends upon the number of portions. As the number of portions increases, the quantity required increases. The quantity per portion is the same. This is called direct proportion. The quantity is said to be **directly proportional** to the number of portions. If 2 potatoes are required for one portion, 4 will be required for two portions etc. A useful method for direct proportion problems is to find the quantity for one and multiply by the number you want.

4.2.3 Inverse proportion

In Section 2.2 you saw that direct proportion described relationships between two quantities, where as one increased, so did the other. Sometimes as one quantity increases the other decreases instead of increasing. This is called indirect proportion. Team tasks are often an example of this. The time taken to do a job is indirectly proportional to the number of people in the team.

A difficulty with the real-life context of such problems is that, in many cases, it is hard to believe that people working in a team will work at the same rate regardless of the size of the team, unless the team work independently, i.e. 'in parallel'. The main idea behind this type of problem is that increasing the number of people working decreases the time taken to complete the task. (An obvious exception to this is decision-making in a committee: if two people can reach a decision in an hour, four people are liable to take twice as long!)



Such problems can be compared with certain problems involving speed: doubling the number of people working is the same as doubling the speed at which the team work. In either case the time is halved. It is useful to find out how long it would take one person to do the whole job, then divide by the number of people sharing the work. This is a good approach to most indirect proportion problems.



**Self-Check-4****ratio and proportion**

Directions: choose the best answer for the following question (2 point each)

Which one of the following is not used to express ratio

A. Fraction B. Bywords C. Colon D. None

1. Ratio is used to make comparisons between two different terms.(

A. True B. False

Note: Satisfactory rating - 2 points

Unsatisfactory - below 2 points

You can ask you teacher for the copy of the correct answers



Operation Sheet 4

ratio and proportion

Operation Sheet No. 4

Title: - Compute ratio and Proportion

Purpose: - Computing **ratio** using appropriate formula.

Materials/Tools/ Equipment Needed:

3. Students Guide
4. Paper
5. Pen
6. Mathematical tables

Activities:

1. Solve problems on the applications the equations;
2. Solve problems on the applications of ratio and Proportion;

Performance Standard:

The trainees should be able to solve problems concerning the applications of equation and Solve problems on the applications of percentages;

Information:

Illustrating the Basic Steps in Solving and in Presenting Solutions of Mathematical Problems

Basic Steps

- i. Statement of the Problem
- ii. Comprehension
Read the text of the problem slowly and carefully and visualize the situation clearly. If possible, make a sketch.
- iii. Framework
Write down neatly the values which have been given and which are to be found, using symbols and dimensions.
- iv. Basic Equation
Relate the situation recognized to the relevant Basic Equation, Only then solve for the required value.
- v. Illustration
- vi. Solve correctly the questions given the evaluation section of the lesson.

Notes:

Make sure that the calculation proceeds step by step. Formulate the answer — at least in your head — as a complete sentence.

In addition it is a good idea to do a rough calculation before the final one. Besides this, always check the dimensions by carrying and shortening the units of measurement.

**Remarks:**

The emphasis in the lesson is the capability of the students to solve application problems. It is therefore recommended that due attention should be given to the exercises with the close supervision of the instructor. In mathematics, there is no substitute for practice.

The teacher shall always set a deadline for finishing a task. But fast students should be given a chance to solve more calculation problems and in so doing acquire more experience.

The teacher should act as a student's consultant, which is an active role. Thus, he shall go around in the class, look at the students' solutions while they do them and give advice.

Summary:

Read – comprehend - sketch

Relate the situation to the basic equation



LAP Test	Carry-out measurements and calculations
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Name: _____ Date: _____

Time started: _____ Time finished: _____

Instructions: Given necessary templates, tools and materials you are required to perform the following tasks within --- hour.

Task 1- Perform calculations on algebraic expressions

Task 2- equations involving one unknown

Task 3- Compute percentage

Task 4- Compute ratio and Proportion



List of references:

1. HAND BOOK OF MACHINING AND METALWORKING CALCULATIONS Ronald A. Walsh
2. Mechanical and Metal Trades Hand Book 2nd English edition.
3. Calibration hand book of measuring instruments Alessandro Brunel
4. Tools and Rules For Precision Measuring Starrett
5. Quick Guide to Precision Measuring instruments Mitutoyo
6. Measuring instruments catalogue NO 2012 E
7. <http://phy.ntnu.edu.tw/~ntnu/java/index.php?topic=31.0>
8. Technical drawing grade 11th text book
9. Calibration hand book of measuring instruments Alessandro Brunel



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